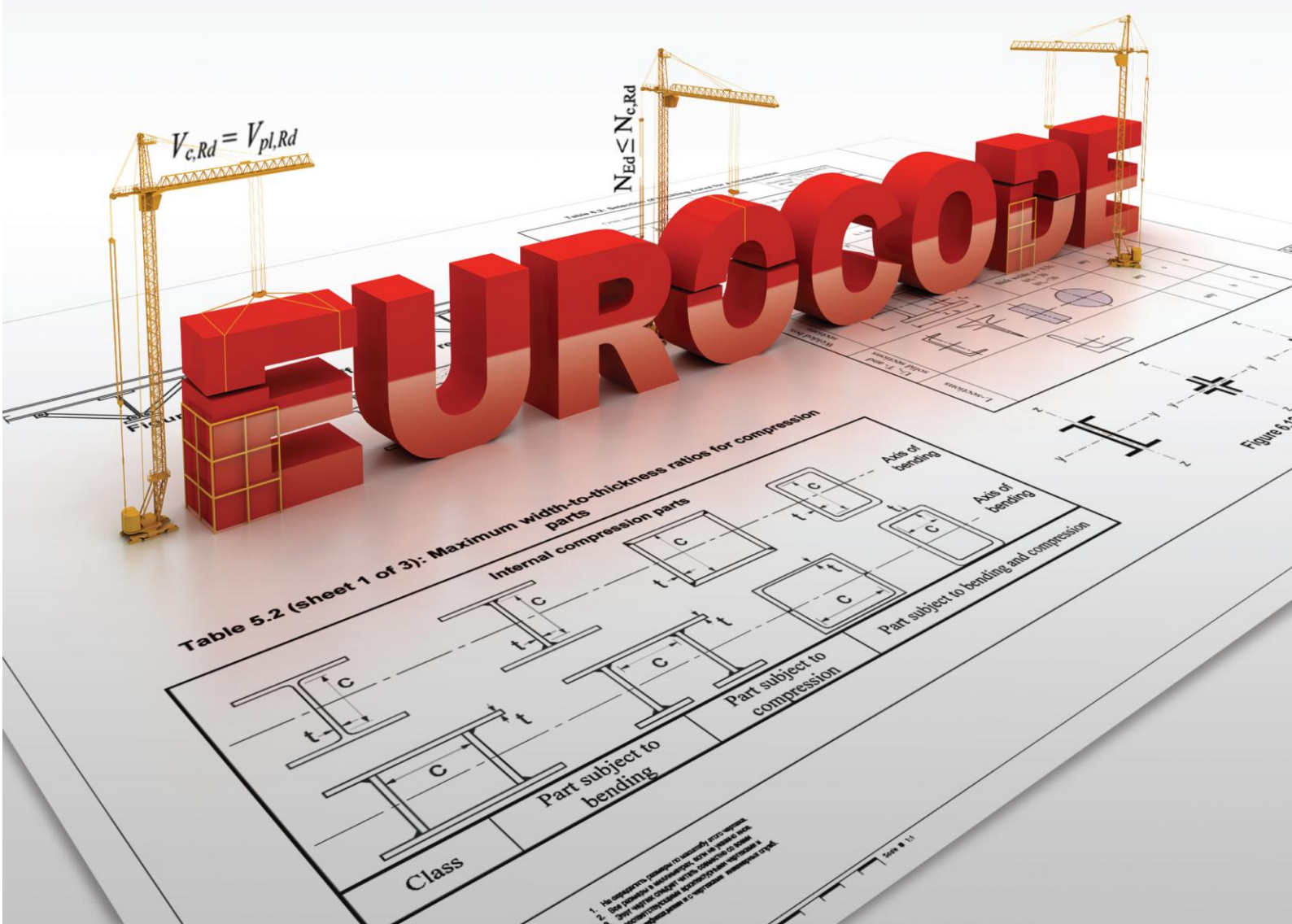


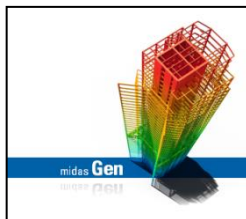
Design Examples using midas Gen to Eurocode 3

Integrated Design System for Building and General Structures



Introduction

This design example book provides a comprehensive guide for steel design as per Eurocode3-1-1:2005. Specifically, this guide will review the design algorithms implemented in midas Gen, and go through detailed verification examples and design tutorials. This book is helpful in understanding the Eurocode design concept and verifying design results using midas Gen.



CHAPTER 1 Why midas Gen

This chapter describes the main features and advantages of midas Gen and showcases prominent project applications.

Class	Part subject to bending	Part subject to compression	Part subject to bending and compression
Types distribution to parts (compression positive)			
1	$c/t \leq 72\epsilon$	$c/t \leq 33\epsilon$	values $\alpha > 0.5$: $c/t \leq \frac{390}{13\alpha - 1}$ values $\alpha \leq 0.5$: $c/t \leq \frac{50\epsilon}{13\alpha - 1}$
2	$c/t \leq 83\epsilon$	$c/t \leq 33\epsilon$	values $\alpha > 0.5$: $c/t \leq \frac{456}{13\alpha - 1}$ values $\alpha \leq 0.5$: $c/t \leq \frac{41.5\epsilon}{13\alpha - 1}$
Types distribution to parts (compression positive)			
3	$c/t \leq 52\epsilon$	$c/t \leq 42\epsilon$	values $\alpha > 0.5$: $c/t \leq \frac{42\epsilon}{13\alpha - 1}$ values $\alpha \leq 0.5$: $c/t \leq \frac{41.5\epsilon}{13\alpha - 1}$

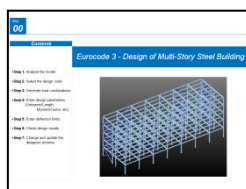
CHAPTER 2 Steel Design Algorithms

This chapter discusses the general design concept of EN1993-1-1 and how it has been implemented in midas Gen. This enables the user to understand the equations, formulas, program limitations and development scope of the midas Gen design features.

5.1 Cross-section resistance under combined bending and shear		
5.1.1 Material Properties		
5.1.2 Section Properties		
5.1.3 Analysis Model		

CHAPTER 3 Verification Examples

This chapter provides comparative results between design reports generated from midas Gen and design examples from reference books. Numerous worked examples for EN1993-1-1:2005 has been used to verify design results from midas Gen. 17 steel examples of beam and column members has been included.

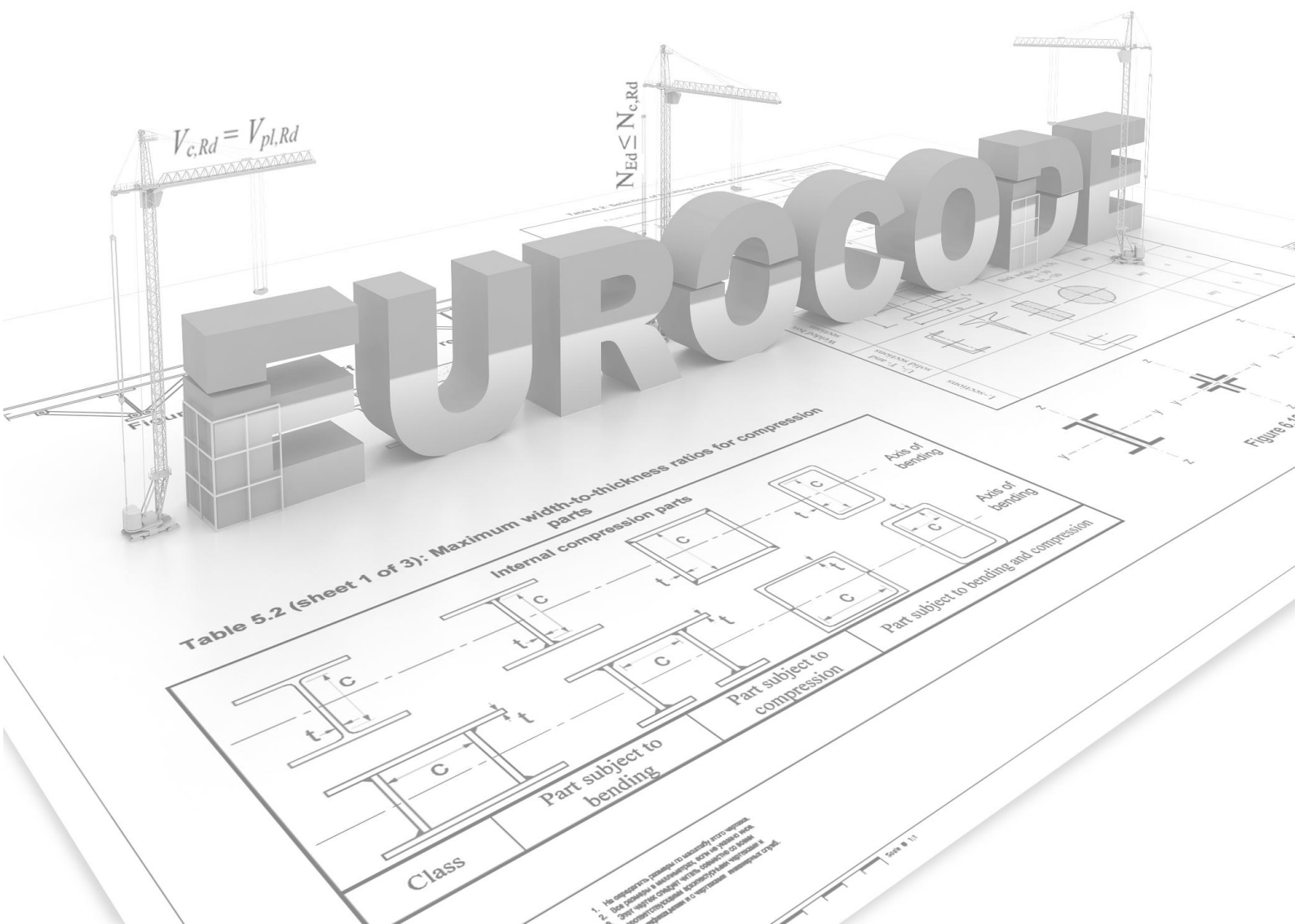


CHAPTER 4 Steel Design Tutorial

This chapter enables the user to get acquainted with the steel design procedure in midas Gen as per EN1993-1-1: 2005. It encompasses the overall design procedure, from generating load combinations to checking design results with updated sections.

Why midas Gen

Design Examples using midas Gen to Eurocode3



CHAPTER 1

Why midas Gen

01 Intuitive User Interface

The intuitive User Interface, contemporary Computer Graphics and substantially fast Solver Speed are some of the highlights of midas Gen. The user-oriented input/output features and significant analysis capabilities enable the practicing engineers and researchers to readily undertake structural analyses and designs for all types of buildings and even complex and long-span structures.

02 Advanced Analysis Features

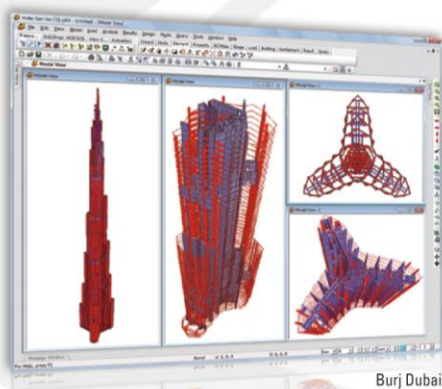
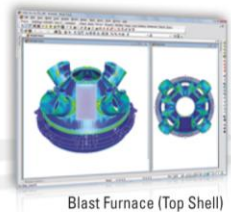
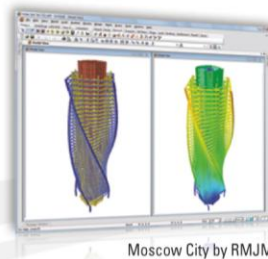
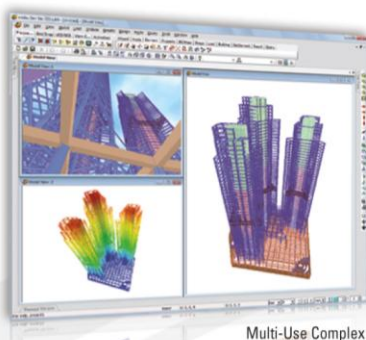
midas Gen offers conventional analysis capabilities as well as other analyses such as Geometric Nonlinear Analysis reflecting Large Displacement, Boundary Nonlinear Analysis, Pushover Analysis, Construction Simulated Analysis reflecting time dependent material properties, Heat of Hydration Analysis, etc.

03 Accurate and Practical Results

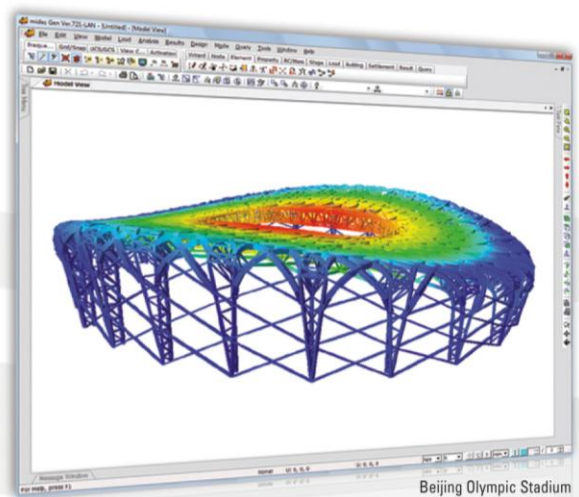
Diverse ranges of specialty finite elements in conjunction with the latest theories of structural analyses render accurate and practical results. It is prominent for providing convenience, efficiency, versatility and productivity.

04 Design Capabilities

midas Gen provides design capabilities using various standards of different countries reflecting conventional as well as unusual design conditions, leading to Optimal Design. midas Gen has been used for over 20 years and applied to over an uncountable number of projects successfully, thereby, demonstrating its credibility and stability.



midas **Gen**



Features

Comprehensive Design

- **Concrete:**
ACI318, Eurocode 2, BS8110, IS456 & IS13920,
CSA-A23.3, GB50010, AIJ-WSD, TWN-USD,
AIK-USD & WSD, KSCE-USD, KCI-USD
- **Steel:**
AISC-ASD & LRFD, AISI-CFSD, Eurocode 3,
BS5950, IS800, CSA-S16, GBJ17 & GB50017,
AIJ-ASD, TWN-ASD & LSD, AIK-ASD & LSD &
CFSD, KSCE-ASD, KSSC-ASD
- **SRC:**
SSRC, JGJ138, CECS28, AIJ-SRC, TWN-SRC,
AIK-SRC2K & SRC, KSSC-CFT
- **Footing Design:** ACI318, BS8110

Wind & Seismic loads auto-Generation

- **Wind load:**
IBC2000, UBC, ANSI, Eurocode 1, BS6399, IS875,
NBC, GB, Japan, Taiwan & Korea
- **Seismic Load:**
IBC2000, UBC, ATC 3-06, Eurocode 8, IS1893,
NBC, GB, Japan, Taiwan & Korea

High-rise Specific Functionality

- **3-D Column Shortening** Reflecting change in
modulus, creep and shrinkage
- **Construction Stage Analysis** accounting for
change in geometry, supports and loadings
- Building model **generation wizard**
- Automatic mass conversion
- Material stiffness changes for **cracked sections**

High-end Analysis Capabilities

- **P-Delta** & Large displacement analysis
- Dynamic Analysis (**Time History, Response
Spectrum**, etc.)
- Base Isolators & Dampers
- **Pushover** Nonlinear Analysis
- Inelastic Time History Analysis
- Staged **post-tensioning**
- Catenary Cable Structure

Intuitive User Interface

- Works Tree (Input summary with powerful
modeling capabilities)
- Models created and changed with ease
- Floor Loads defined by areas and on inclined plane
- Built-in **Section property Calculator**
- **Tekla Structures, Revit Structure & STAAD**
interfaces

Why midas Gen?

midas Gen is a Windows-based, **general-purpose** structural analysis and optimal design system.

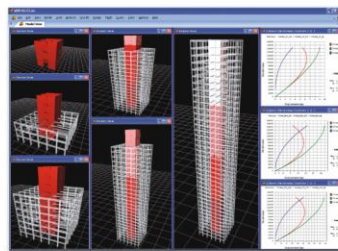
The **intuitive User Interface**, contemporary Computer Graphics and substantially fast **Solver Speed** are some of the highlights of midas Gen.

The user-oriented input/output features and significant analysis capabilities enable the **practicing engineers** and researchers to readily undertake structural **analysis and design** for even complex and large structures.

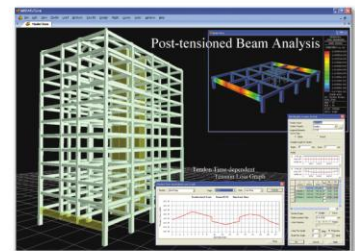
The fastest Multi-Frontal Solver and the latest analysis algorithms instantly bring accurate and practical analysis results.

In addition, midas Gen provides design capabilities using various standards of different countries leading to an Optimal Design Solution.

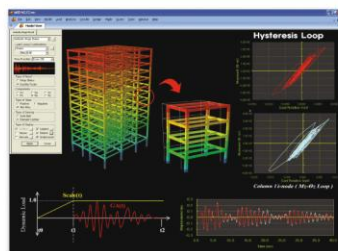
High-end Analysis Features



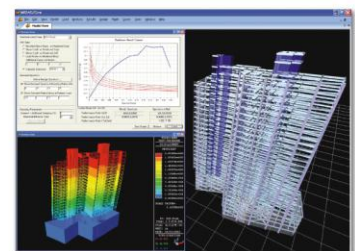
[Construction Stage Analysis]



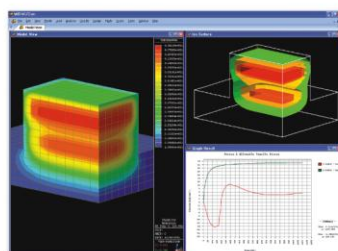
[Post-tension Analysis]



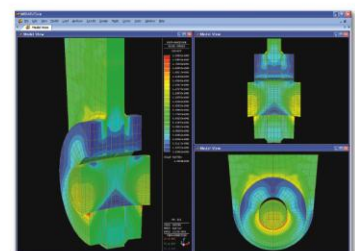
[Time History Analysis]



[Pushover Analysis]



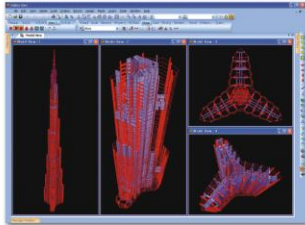
[Heat of Hydration Analysis]



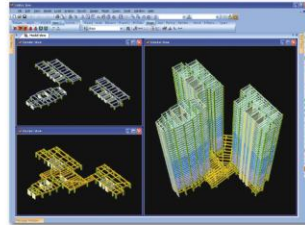
[Detail Analysis]

Project Applications

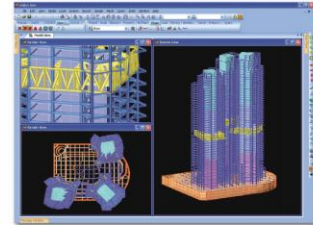
Buildings



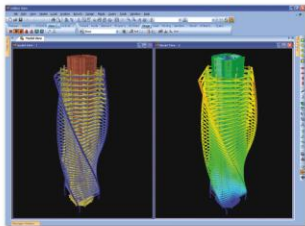
Burj Dubai



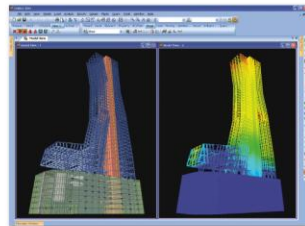
Venture Towers



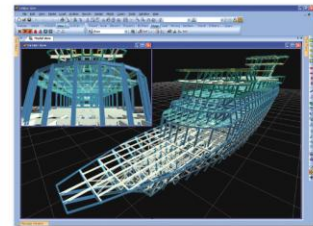
Multi-Use Complex



Moscow City by RMJM

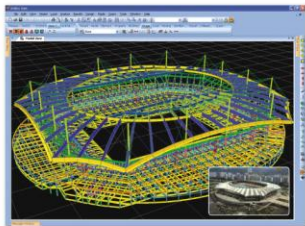


Office Building

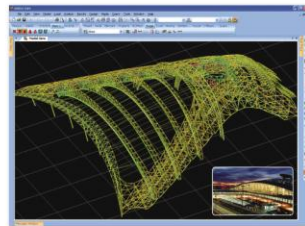


Resort Facility

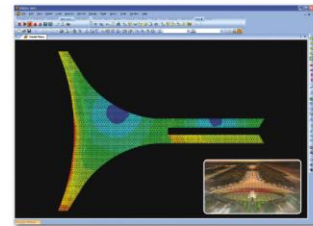
Specialty Structures



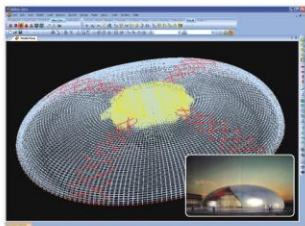
Seoul World Cup Stadium



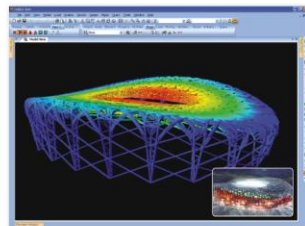
Incheon International Airport



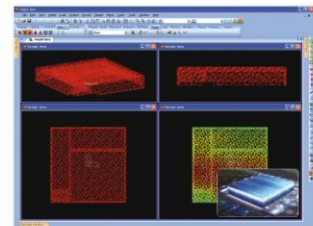
Beijing International Airport



Beijing National Theater

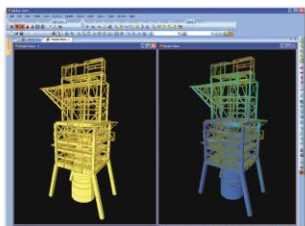


Beijing Olympic Stadium

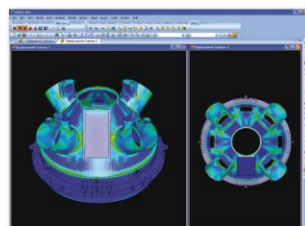


Beijing Olympic Aquatics Center

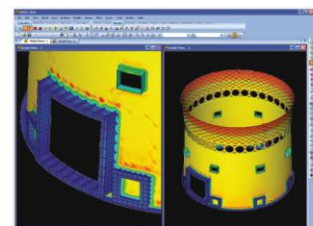
Plant Structures



India IISCO blast furnace tower



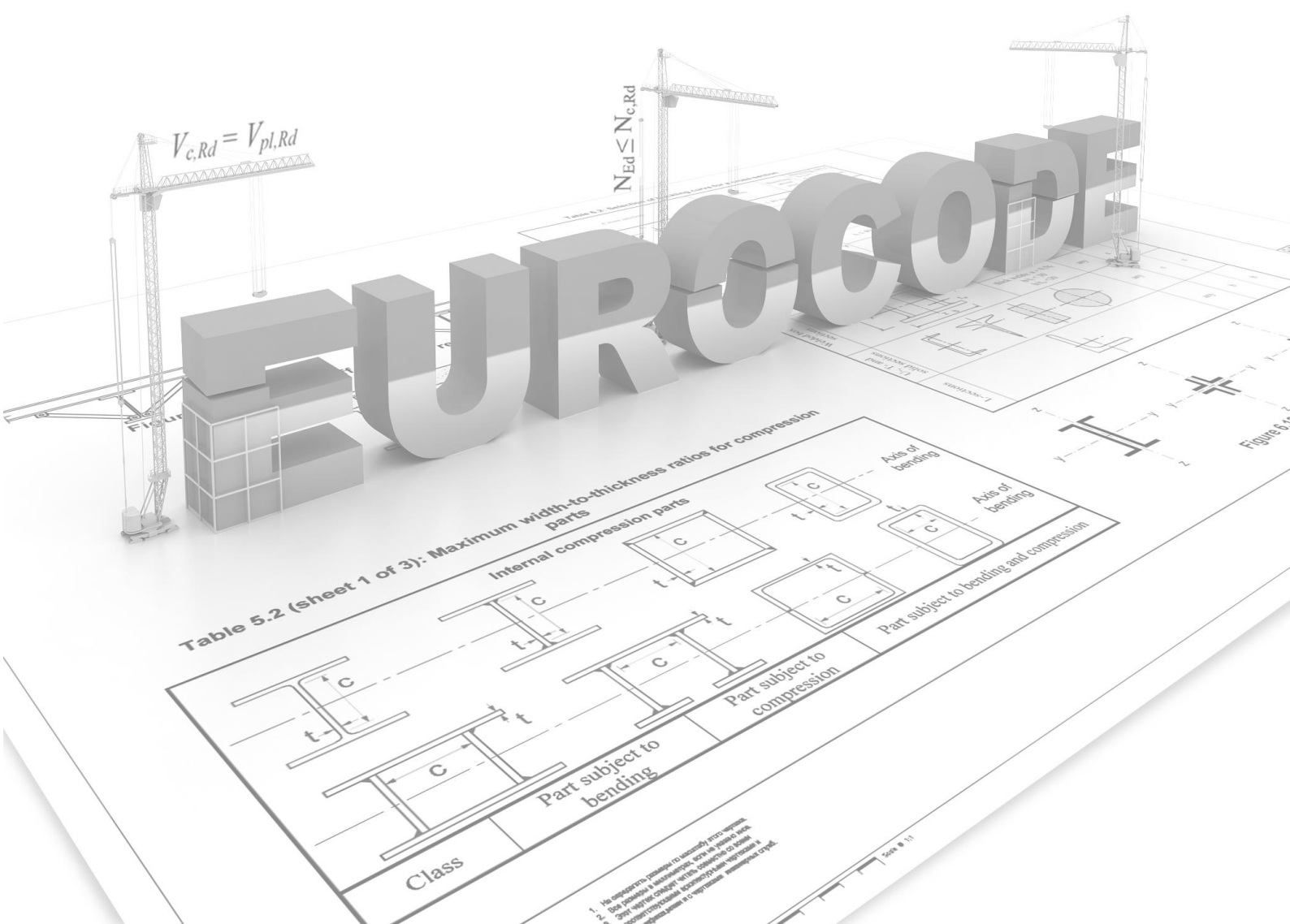
Blast Furnace (Top Shell)



Blast Furnace

Steel Design Algorithm

Design Examples using midas Gen to Eurocode3



CHAPTER 2

Steel Design Algorithm

as per EN1993-1-1:2005

2.1 Overview

- (1) General
 - Material Properties
 - Section table for the application of Ultimate Limit State Check
- (2) Ultimate Limit State Check
 - Resistance of cross-sections
 - Buckling resistance of members
- (3) Serviceability Limit State Check
 - Vertical deflections
 - Horizontal deflections
 - Dynamic effects

2.2 General

- (1) Material Properties
 - The nominal values of the yield strength (f_y) and the ultimate strength (f_u) for structural steel

Steel Grade	$t \leq 40\text{mm}$		$t > 40\text{mm}$	
	f_y (N/mm^2)	f_u (N/mm^2)	f_y (N/mm^2)	f_u (N/mm^2)
S235	235	360	215	360
S275	275	430	255	410
S355	355	510	355	470
S450	440	550	410	550

- Modulus of Elasticity = $210,000 \text{ N/mm}^2$
- Poisson's Ratio, ν , = 0.3
- Thermal Coefficient = $12 \times 10^{-6} / ^\circ\text{C}$
- Weight Density = 76.98 kN/m^3

(2) Section table for the application of Ultimate Limit State Check

Cross section		Limit States				
		Yielding	FB ⁽¹⁾	SB		LTB
				Strong axis	Weak axis	
I section	Doubly Symmetric	✓	✓	✓	N/A	✓
	Singly Symmetric	✓	✓	✓	N/A	N/A
	Box	✓	✓	✓	✓ ⁽²⁾	N/A
	Angle	✓	✓	N/A	N/A	N/A
	Channel	✓	✓	✓	N/A	N/A
	Tee	✓	✓	N/A	N/A	N/A
	Double Angle	✓	✓	N/A	N/A	N/A
	Double Channel	✓	✓	✓	N/A	N/A
	Pipe	✓	✓	N/A	N/A	N/A
	Solid Rectangle	✓	✓	N/A	N/A	N/A
	Solid Round	✓	✓	N/A	N/A	N/A
	U-Rib	N/A	N/A	N/A	N/A	N/A

**Note**

FB: Flexural Buckling, **SB:** Shear Buckling, **LTB:** Lateral-Torsional Buckling

(1) Torsional Buckling and Torsional-Flexural Buckling are not evaluated.

(2) The thickness of two webs should be identical, and the member type should be “column” for the weak axis shear buckling check.

2.3 Ultimate Limit State Check

(1) Resistance of cross-sections

- Tension

$$N_{pl,Rd} = \frac{Af_y}{\gamma_{M0}}$$

- Design tension resistance

- The design ultimate resistance of the net cross-section at holes for fasteners is not considered in midas Gen.

- Compression

- Design compression resistance

$$N_{c,Rd} = \frac{Af_y}{\gamma_{M0}} \quad \text{For class 1,2 and 3 cross sections}$$

$$N_{c,Rd} = \frac{A_{eff} f_y}{\gamma_{M0}} \quad \text{For class 4 cross sections}$$

- In the case of unsymmetrical Class 4 sections, the additional moment due to the eccentricity of the centroidal axis of the effective section is considered in midas Gen.

- Bending moment

- Design bending resistance

$$M_{c,Rd} = M_{pl,Rd} = \frac{W_{pl} f_y}{\gamma_{M0}} \quad \text{For class 1 or 2 cross sections}$$

$$M_{c,Rd} = M_{el,Rd} = \frac{W_{el,min} f_y}{\gamma_{M0}} \quad \text{For class 3 cross sections}$$

$$M_{c,Rd} = \frac{W_{eff,min} f_y}{\gamma_{M0}} \quad \text{For class 4 cross sections}$$

- Shear

- Design shear resistance in the absence of torsion

$$V_{pl,Rd} = \frac{A_v(f_y/\sqrt{3})}{\gamma_{M0}}$$

- The shear area A_v is calculated based on the clause 6.2.6 (3) as per EN1993-1-1
- Rolled I and H sections, load parallel to web: $A - 2bt_f + (t_w + 2r)t_f$
- but not less than Design elastic shear resistance is not applied.

- Shear Buckling

- The shear buckling resistance for webs without intermediate stiffeners is calculated, according to section 5 of EN 1993-1-5, if

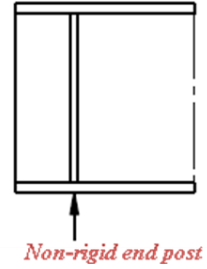
$$\frac{h_w}{t_w} > 72 \frac{\varepsilon}{\eta} \quad \varepsilon = \sqrt{\frac{235}{f_y [N/mm^2]}}$$

- For steel grades up to and including S460: $\eta = 1.20$
- For higher steel grades: $\eta = 1.00$
- Design resistance

$$V_{b,Rd} = V_{bw,Rd} + V_{bf,Rd} \leq \frac{\eta f_{yw} h_w t}{\sqrt{3} \gamma_{M1}}$$

$$V_{bw,Rd} = \chi_w f_{yw} \frac{h_w t}{\sqrt{3} \gamma_{M1}}$$

$$V_{bf,Rd} = \frac{b_f t_f^2 f_{yf}}{c \gamma_{M1}} \left(1 - \left(\frac{M_{Ed}}{M_{f,Rd}} \right)^2 \right)$$



- Stiffener design to resist shear buckling is not provided in midas Gen.
- Stiffener type for end supports is assumed as a non-rigid end post.
- It is assumed that the length of an unstiffened plate, 'a' is the same as the unbraced length.
- Torsion
 - The torsional resistance is not checked.
- Bending and Shear
 - The effect of shear force on the moment resistance is considered.
 - Where the shear force is less than half the plastic shear resistance, its effect on the moment resistance is neglected.
 - Where $V_{ED} \geq 0.5V_{pl,Rd}$

I-cross-sections with equal flanges and bending about the major axis

$$M_{y,V,Rd} = \frac{\left[W_{pl,y} - \frac{\rho A_w^2}{4t_w} \right] f_y}{\gamma_{M0}}$$

$$\text{but, } M_{y,V,Rd} \leq M_{y,c,Rd}$$

$$\rho = \left(\frac{2V_{ED}}{V_{pl,Rd}} - 1 \right)^2 \quad \text{Torsion is not considered when calculating } \rho$$

For the other cases

$$M_{V,Rd} = (1 - \rho) M_{c,Rd}$$

- Bending and Axial Force

- The effect of axial force on the moment resistance is considered.
- Class 1 and 2 cross sections

For doubly symmetrical I- and H-sections, allowance is not made for the effect of the axial force on the plastic resistance moment about the y-y axis when both the following criteria are satisfied:

$$N_{Ed} \leq 0.25 N_{pl,Rd} \quad N_{Ed} \leq \frac{0.5 h_w t_w f_y}{\gamma_{M0}}$$

For doubly symmetrical I- and H-sections, allowance is not made for the effect of the axial force on the plastic resistance moment about the z-z axis when:

$$N_{Ed} \leq \frac{h_w t_w f_y}{\gamma_{M0}}$$

The following equations are used for standard rolled I or H sections and for welded I or H sections with equal flanges:

$$M_{N,y,Rd} = M_{pl,y,Rd} (1 - n)(1 - 0.5a) \quad \text{but} \quad M_{N,y,Rd} \leq M_{pl,y,Rd}$$

$$\text{for } n \leq a : M_{N,z,Rd} = M_{pl,z,Rd}$$

$$\text{for } n > a : M_{N,z,Rd} = M_{pl,z,Rd} \left[1 - \left(\frac{n-a}{1-a} \right)^2 \right]$$

$$\text{Where } n = N_{Ed} / N_{pl,Rd} \\ a = (A - 2bt_f) / A \quad \text{but } a \leq 0.5$$

- Bending and Axial Force

$$\left[\frac{M_{y,Ed}}{M_{N,y,Rd}} \right]^\alpha + \left[\frac{M_{z,Ed}}{M_{N,z,Rd}} \right]^\beta \leq 1 \quad \text{for Class 1\&2 sections} \\ \text{I and H section: } \alpha=2; \beta=5n \text{ but } \beta \geq 1$$

$$\frac{N_{Ed}}{N_{Rd}} + \frac{M_{y,Ed}}{M_{y,Rd}} + \frac{M_{z,Ed}}{M_{z,Rd}} \leq 1 \quad \text{for Class 1,2,3 \& 4 sections}$$

- Bending, Shear and Axial Force

- Where the shear force exceeds 50% of the plastic shear resistance, its effect on the moment of resistance is reflected in the formula above.
- $M_{pl,y,Rd}$ and $M_{pl,z,Rd}$ are replaced by $M_{y,v,Rd}$ and $M_{z,v,Rd}$ respectively in the following equations to consider shear effect in the above criterion a).

$$M_{N,y,Rd} = M_{pl,y,Rd} (1 - n) / (1 - 0.5 a_w)$$

$$M_{N,z,Rd} = M_{pl,z,Rd} (1 - n) / (1 - 0.5 a_r)$$

- $M_{y,Rd}$ and $M_{z,Rd}$ are replaced by $M_{y,v,Rd}$ and $M_{z,v,Rd}$ respectively in the above criterion b) to consider shear effect.

(2) Buckling resistance of members

- Uniform members in compression

For slenderness $\lambda \leq 0.2$ or for $\frac{N_{Ed}}{N_{cr}} \leq 0.04$ the buckling effects are ignored.

$$\bar{\lambda} = \sqrt{\frac{Af_y}{N_{cr}}} \text{ for Class 1,2 and 3 cross-sections} \quad \bar{\lambda} = \sqrt{\frac{A_{eff} f_y}{N_{cr}}} \text{ for Class 4 cross-section}$$

N_{cr} is the elastic critical force for the relevant buckling mode based on the gross cross sectional properties.

$$N_{cr} = \frac{\pi^2 EI}{L_e^2}$$

- Flexural buckling is checked for the L, C, I, T, Box, Pipe, Double L, and Double C section.
- Torsional and torsional-flexural buckling is not checked.
- Design buckling resistance

$$N_{b,Rd} = \frac{\chi A f_y}{\gamma_{M1}} \quad \text{for Class 1,2 and 3 cross-sections}$$

$$N_{b,Rd} = \frac{\chi A_{eff} f_y}{\gamma_{M1}} \quad \text{for Class 4 cross-sections}$$

$$\chi = \frac{1}{\Phi + \sqrt{\Phi^2 - \bar{\lambda}^2}} \quad \text{but } \chi \leq 1.0 \quad \Phi = 0.5 \left[1 + \alpha(\bar{\lambda} - 0.2) + \bar{\lambda}^2 \right]$$

Buckling Curve	a_0	a	b	c	d
Imperfection factor α	0.13	0.21	0.34	0.49	0.76

- Uniform members in bending
 - For the uniform and doubly symmetric I cross-sections only, the lateral torsional buckling check is provided.
 - It is assumed that the section is loaded through its shear center, and the boundary conditions at each end are both restrained against lateral movement and restrained against rotation about the longitudinal axis.
 - For slenderness $\bar{\lambda}_{LT} \leq \bar{\lambda}_{LT,0}$ or for $\frac{M_{ED}}{M_{cr}} \leq \bar{\lambda}_{LT,0}^2$ the lateral torsional buckling effects are ignored.

$$\bar{\lambda}_{LT} = \sqrt{\frac{W_y f_y}{M_{cr}}} \quad \bar{\lambda}_{LT,0} = 0.4$$

M_{cr} is the elastic critical moment for lateral-torsional buckling. The value of C_1 depends on the moment distribution along the member which is calculated based on the table in the following page

$$M_{cr} = C_1 \frac{\pi^2 E I_z}{L_{cr,LT}^2} \sqrt{\frac{I_w}{I_z} + \frac{L_{cr,LT}^2 G I_t}{\pi^2 E I_z}} \quad G = \frac{E}{2(1+\nu)} \quad I_w = \frac{I_z (h - t_f)^2}{4} : \text{Warping Constant}$$

- If the member type is column, C_1 is calculated based on the table below. EN 1993-1-1: 1992 Annex.



ψ	k	C_1
+1	1.0	1.000
	0.7	1.000
	0.5	1.000
+3/4	1.0	1.141
	0.7	1.270
	0.5	1.305
+1/2	1.0	1.323
	0.7	1.473
	0.5	1.514
+1/4	1.0	1.563
	0.7	1.739
	0.5	1.788

ψ	k	C_1
0	1.0	1.879
	0.7	2.092
	0.5	2.150
-1/4	1.0	2.281
	0.7	2.538
	0.5	2.609
-1/2	1.0	2.704
	0.7	3.009
	0.5	3.093
-3/4	1.0	2.927
	0.7	3.009
	0.5	3.093
-1	1.0	2.752
	0.7	3.063
	0.5	3.149

- If the member type is beam, C_1 is calculated based on the table below.

Conditions	Bending moment diagram	k	C_1
Case 1		1.0	1.132
		0.5	0.972
Class 2		1.0	1.285
		0.5	0.712
Case 3		1.0	Same as Case 1
		0.5	
Case 4		1.0	Same as Case 2
		0.5	
Case 5		1.0	Same as Case 1
		0.5	

- Design buckling Resistance

$$M_{b,Rd} = \chi_{LT} W_y \frac{f_y}{\gamma_{M1}}$$

$$W_y = W_{pl,y} \quad \text{for Class 1 or 2 cross-section}$$

$$W_y = W_{el,y} \quad \text{for Class 3 cross-section}$$

$$W_y = W_{eff,y} \quad \text{for Class 1 or 2 cross-section}$$

$$\chi_{LT} = \frac{1}{\Phi_{LT} + \sqrt{\Phi_{LT}^2 + \bar{\lambda}_{LT}^2}} \quad \text{but} \quad \chi_{LT} \leq 1.0$$

$$\Phi_{LT} = 0.5 \left[1 + \alpha_{LT} (\bar{\lambda}_{LT} - 0.2) + \bar{\lambda}_{LT}^2 \right]$$

Buckling Curve	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>
Imperfection factor α_{LT}	0.21	0.34	0.49	0.76

- The method in the Clause 6.3.2.3 and 6.3.2.4 of EC3 are not considered.

- Uniform members in bending and axial compression

- For members which are subjected to combined bending and axial compression, the resistance to lateral and lateral-torsional buckling is verified by the following criteria.

$$\frac{N_{Ed}}{\chi_y N_{Rk}} + k_{yy} \frac{M_{y,Ed} + \Delta M_{y,Ed}}{\chi_{LT} \frac{M_{y,Rk}}{\gamma_{M1}}} + k_{yz} \frac{M_{z,Ed} + \Delta M_{z,Ed}}{\chi_{LT} \frac{M_{z,Rk}}{\gamma_{M1}}} \leq 1$$

$$\frac{N_{Ed}}{\chi_z N_{Rk}} + k_{zy} \frac{M_{y,Ed} + \Delta M_{y,Ed}}{\chi_{LT} \frac{M_{y,Rk}}{\gamma_{M1}}} + k_{zz} \frac{M_{z,Ed} + \Delta M_{z,Ed}}{\chi_{LT} \frac{M_{z,Rk}}{\gamma_{M1}}} \leq 1$$

K_{yy} , k_{yz} , k_{zy} , k_{zz} are the interaction factors. These values are obtained from Annex A in EN 1993-1-1: 2005.

C_{my} , C_{mz} , C_{mLT} in Annex A can be either user defined or auto-calculated.

Vales for $N_{Rk} = f_y A_i$, $M_{i,Rk} = f_y W_i$ and $\Delta M_{i,Ed}$

Class	1	2	3	4
A_j	A	A	A	A_{eff}
W_y	$W_{pl,y}$	$W_{pl,y}$	$W_{el,y}$	$W_{eff,y}$
W_z	$W_{pl,z}$	$W_{pl,z}$	$W_{el,z}$	$W_{eff,z}$
$\Delta M_{y,Ed}$	0	0	0	e_{Ny}, N_{Ed}
$\Delta M_{z,Ed}$	0	0	0	e_{Nz}, N_{Ed}

- When the design axial force, N_{Ed} is larger than $N_{cr,z}$ or $N_{cr,TF}$, the criteria above are not applied.

- General method of the clause 6.3.4 is not considered.

2.4 Serviceability Limit State Check

(1) Vertical Deflection

- Vertical deflection can be checked for beam member.
- Remaining total deflection (w_{\max}) caused by the permanent and variable actions is automatically checked based on the serviceability load combinations.
- The default limit value is set to $L/250$
- The deflection due to the variable actions can be checked manually by adding load combination consisting of variable actions and changing the limit value

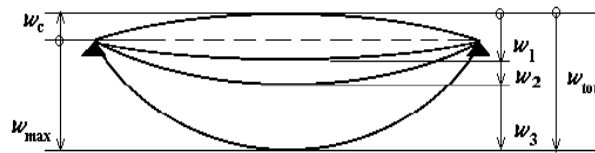


Figure A1.1 - Definitions of vertical deflections

(2) Horizontal Deflection

- Horizontal deflection can be checked for column members.
- Horizontal displacement over a story height H_i is automatically checked based on the serviceability load combinations.
- The default limit value is set to $H_i/300$.
- Overall horizontal displacement over the building height H should be checked separately.

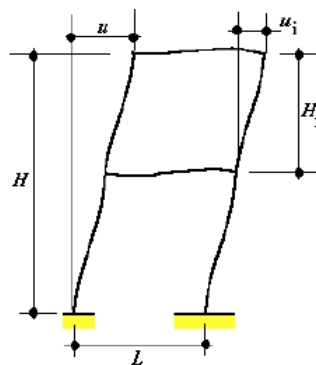


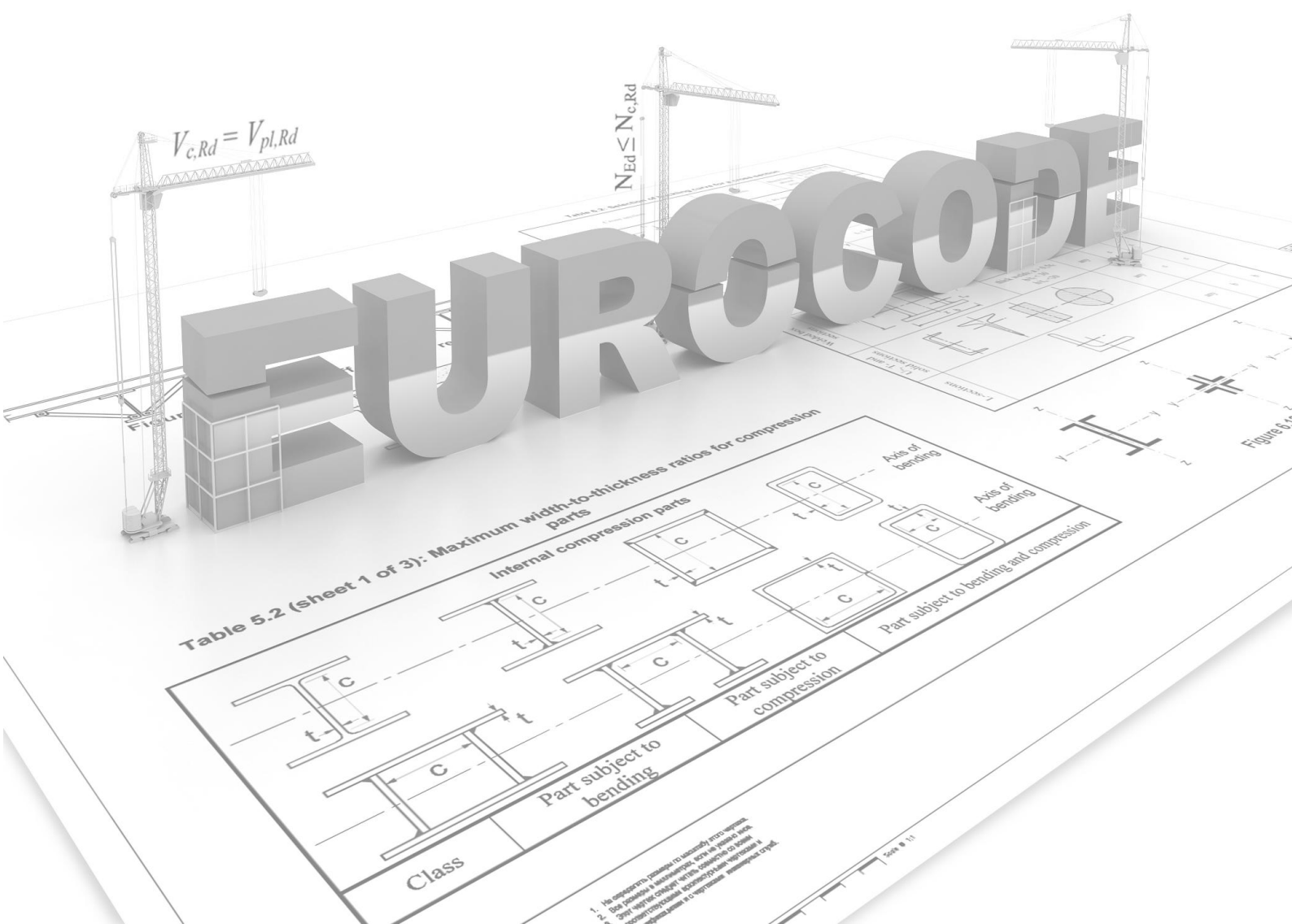
Figure A1.2 - Definition of horizontal displacements

(3) Dynamic effects

- The vibration of structures is not checked.

Verification Examples

Design Examples using midas Gen to Eurocode3

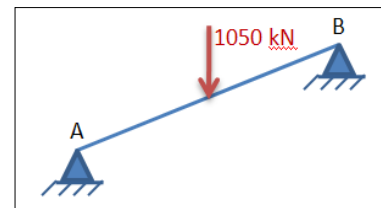


CHAPTER 3

Steel Design Verification Examples

3.1 Cross-section resistance under combined bending and shear

A short-span (1.4m), simply supported, laterally restrained beam is to be designed to carry a central point load of 1050 kN, as shown in the right figure. The arrangement of the figure results in a maximum design shear force VED of 525 kN and a maximum design bending moment MED of 367.5 kNm. In this example a 406 x 178 x 74 UB in grade S275 steel is assessed for its suitability for this application.

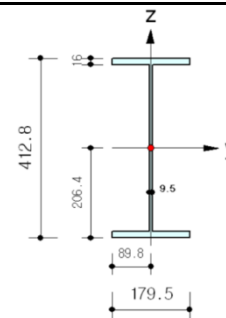


3.1.1 Material Properties

Material	S275	$f_y = 275 \text{ N/mm}^2$	$E_s = 210 \text{ GPa}$
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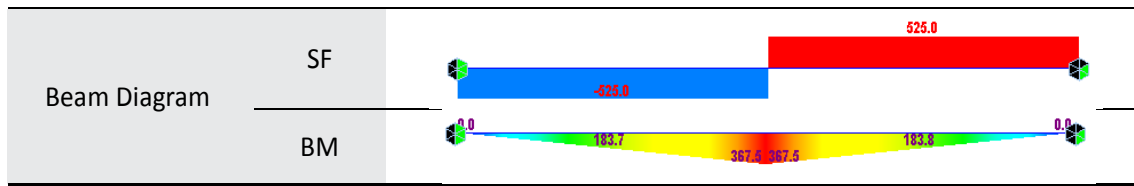
3.1.2 Section Properties

Section Name	406 x 178 x 74 UB
Depth (H)	412.8mm
Width (B)	179.5mm
Flange Thickness (T_f)	16.0 mm
Web Thickness (T_w)	9.5 mm
Gross sectional area (A)	9450.0mm ²
Shear area (A_{sz})	4184.0 mm ²



3.1.3 Analysis Model

Loading condition	
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3.1.4 Comparison of Design Results

	midas Gen	Example book	Error (%)
Shear resistance	689.25kN	689.2kN	0.01%
Bending resistance	412.50kNm	412.0kNm	0.12%
Combined resistance	386.55kNm	386.8kNm	0.06%

3.1.5 Detailed comparison

midas Gen	Example book
<p>1. Cross-section classification</p> <p>(). Determine classification of compression outstand flanges.</p> <p>[Eurocode3:05 Table 5.2 (Sheet 2 of 3), EN 1993-1-5]</p> <ul style="list-style-type: none"> - $e = \text{SQRT} (235/f_y) = 0.92$ - $b/t_f = \text{BTR} = 4.67$ - $\sigma_1 = 0.278 \text{ kN/mm}^2$. - $\sigma_2 = 0.278 \text{ kN/mm}^2$. - $\text{BTR} < 9 \cdot e$ (Class 1 : Plastic). <p>(). Determine classification of bending Internal Parts.</p> <p>[Eurocode3:05 Table 5.2 (Sheet 1 of 3), EN 1993-1-5]</p> <ul style="list-style-type: none"> - $e = \text{SQRT}(235/f_y) = 0.92$ - $d/t_w = \text{HTR} = 37.94$ - $\sigma_1 = 558989.618 \text{ KPa}$. - $\sigma_2 = -558989.618 \text{ KPa}$. - $\text{HTR} < 72 \cdot e$ (Class 1 : Plastic). <p>2. Check Bending Moment Resistance</p> <p>(). Calculate plastic resistance moment about major axis.</p> <p>[Eurocode3:05 6.1, 6.2.5]</p> <ul style="list-style-type: none"> - $W_{ply} = 0.0015 \text{ m}^3$. - $M_{c,Rd} = W_{ply} \cdot f_y / \text{Gamma}_{M0} = 412.50 \text{ kN-m}$. <p>(). Check ratio of moment resistance ($M_{Edy}/M_{c,Rdy}$).</p> <p>$M_{Edy} \quad 367.50$</p> <p>- $\frac{\quad}{M_{c,Rdy} \quad 412.50} = 0.891 < 1.000 \rightarrow \text{O.K.}$</p> <p>3. Shear resistance of cross-section</p> <p>(). Calculate shear area.</p> <p>[Eurocode3:05 6.2.6, EN1993-1-5:04 5.1 NOTE 2]</p> <ul style="list-style-type: none"> - $\eta = 1.2$ ($F_y < 460 \text{ MPa}$.) 	<p>1. Cross-section classification (clause 5.5.2)</p> <p>$\epsilon = \sqrt{235/f_y} = \sqrt{235/275} = 0.92$</p> <p>Outstand flange in compression (Table 5.2, sheet 2):</p> <p>$C = (b - t_w - 2r)/2 = 74.8 \text{ mm}$</p> <p>$c/t_f = 74.8/16.0 = 4.68$</p> <p>Limit for Class 1 flange $= 9\epsilon = 8.32$</p> <p>$4.68 < 8.32 \therefore$ flange is Class 1</p> <p>Web – internal part in bending (Table 5.2, sheet 1):</p> <p>$C = h - 2t_f - 2r = 360.4 \text{ mm}$</p> <p>$c/t_w = 360.4/9.5 = 37.94$</p> <p>Limit for Class 1 web $= 72\epsilon = 66.56$</p> <p>$37.94 < 66.56 \therefore$ web is Class 1</p> <p>Therefore, the overall cross – section classification is Class 1.</p> <p>2. Bending resistance of cross – section (clause 6.2.5)</p> <p>$M_{c,y,Rd} = \frac{W_{pl,y} f_y}{\gamma_{M0}}$ for Class 1 or 2 cross –sections</p> <p>The design bending resistance of the cross-section</p> <p>$M_{c,y,Rd} = \frac{275 \times 10^3 \times 275}{1.00} = 412 \times 10^6 \text{ N mm} = 412 \text{ KNm}$</p> <p>$412 \text{ KNm} > 367.5 \text{ KNm}$</p> <p>$\therefore$ cross-section resistance in bending is acceptable.</p> <p>3. Shear resistance of cross-section of cross-section (clause 6.2.6)</p> <p>$V_{pl,Rd} = \frac{A_v (f_y/3)}{\gamma_{M0}}$</p>

- $r = 10.2000 \text{ mm}$.
- $A_{vy} = \text{Area} - h_w \cdot t_w = 5832.4000 \text{ mm}^2$.
- $A_{vz1} = \eta \cdot h_w \cdot t_w = 4341.1200 \text{ mm}^2$.
- $A_{vz2} = \text{Area} - 2 \cdot B \cdot t_f + (t_w + 2 \cdot r) \cdot t_f = 4184.4000 \text{ mm}^2$.
- $A_{vz} = \text{MAX}[A_{vz1}, A_{vz2}] = 4341.1200 \text{ mm}^2$.

(). Calculate plastic shear resistance in local-z direction (V_{pl,Rdz}). [Eurocode3:05 6.1, 6.2.6]

- $V_{pl,Rdz} = [A_{vz} \cdot f_y / \text{SQRT}(3)] / \Gamma_{M0} = 689.25 \text{ kN}$.

(). Shear Buckling Check. [Eurocode3:05 6.2.6]

- $HTR < 72 \cdot e / \eta$ ----> No need to check!

(). Check ratio of shear resistance (V_{Edz}/V_{pl,Rdz}).
(LCB = 1, POS = J)

- Applied shear force : $V_{Edz} = 525.00 \text{ kN}$.
- $$\frac{V_{Edz}}{V_{pl,Rdz}} = \frac{525.00}{689.25} = 0.762 < 1.000 \text{ ----> O.K.}$$

4. Check Interaction of Combined Resistance

(). Calculate Major reduced design resistance of bending and

shear. [Eurocode3:05 6.2.8 (6.30)]

- In case of $V_{Edz} / V_{pl,Rdz} > 0.5$ (equal flanges)
- $\rho = \{2 \cdot (V_{Edz} / V_{pl,Rdz}) - 1\}^2 = 0.274$
- $M_{y,V,Rd1} = [W_{ply} - \{\rho \cdot A_w^2 / (4 \cdot t_w)\}] \cdot f_y / \Gamma_{M0} = 386.55 \text{ kN-m}$.
- $M_{y,Rd} = \text{MIN}[M_{y,V,Rd1}, M_{c,Rd}] = 386.55 \text{ kN-m}$.

(). Calculate Minor reduced design resistance of bending and

shear. [Eurocode3:05 6.2.8 (6.30)]

- In case of $V_{Edy} / V_{pl,Rdy} < 0.5$
- $M_{z,Rd} = M_{c,Rdz} = 73.42 \text{ kN-m}$.

(). Check general interaction ratio.

[Eurocode3:05 6.2.1 (6.2)] - Class1 or Class2

$$R_{max1} = \frac{N_{Ed}}{N_{Rd}} + \frac{M_{Edy}}{M_{y,Rd}} + \frac{M_{Edz}}{M_{z,Rd}} = 0.951 < 1.000 \text{ ----> O.K.}$$

(). Check interaction ratio of bending and axial force member.

[Eurocode3:05 6.2.9 (6.31 ~ 6.41)] - Class1 or Class2

- $n = N_{Ed} / N_{pl,Rd} = 0.000$
- $a = \text{MIN}[(\text{Area} - 2b \cdot t_f) / \text{Area}, 0.5] = 0.392$
- $\alpha = 2.000$
- $\beta = \text{MAX}[5 \cdot n, 1.0] = 1.000$

For a rolled I section, loaded parallel to the web, the shear area A_v is given by

$A_v = A - 2b t_f + (t_w + r) t_f$ (but not less than $\eta h_w t_w$)
 $\eta = 1.2$ (from EN 1993-1-5, though the UK National Annex may specify an alternative value).

$$h_w = (h - 2t_f) = 412.8 - (2 \times 16.0) = 380.8 \text{ mm}$$

$$\therefore A_v = 9450 - (2 \times 179.5 \times 16.0) + (9.5 + 10.2) \times 16.0 = 4184 \text{ mm}^2$$

(but not less than $1.2 \times 380.8 \times 9.5 = 4341 \text{ mm}^2$)

$$V_{p1,Rd} = \frac{4341 \times (275/3)}{1.00} = 689200 \text{ N} = 689.2 \text{ kN}$$

Shear buckling need not be considered, provided

$$\frac{h_w}{t_w} \leq 72 \frac{\epsilon}{\eta} \quad \text{for unstiffened webs}$$

$$72 \frac{\epsilon}{\eta} = 72 \times \frac{0.92}{1.2} = 55.5$$

$$\text{Actual } h_w/t_w = 380.8/9.5 = 40.1$$

$40.1 \leq 55.5 \quad \therefore$ no shear buckling check required

$689.2 > 525 \text{ kN} \quad \therefore$ shear resistance is acceptable

4. Resistance of cross-section to combined bending and shear (clause 6.2.8)

The applied shear force is greater than half the plastic shear resistance of the cross-section, therefore a reduced moment resistance $M_{y,V,Rd}$ must be calculated. For an I section (with equal flanges) and bending about the major axis, clause 6.2.8(5) and equation (6.30) may be utilized.

$$M_{y,V,Rd} = \frac{(W_{pl,y} - \rho A_w^2 / (4 t_w)) f_y}{\Gamma_{M0}} \quad \text{but } M_{y,V,Rd} \leq M_{y,c,Rd}$$

$$\rho = \left(\frac{2V_{Ed}}{V_{pl,Rd}} - 1 \right)^2 = \left(\frac{2 \times 525}{689.2} - 1 \right)^2 = 0.27$$

$$A_w = h_w t_w = 380.8 \times 9.5 = 3617.6 \text{ mm}^2$$

$$\Rightarrow M_{y,V,Rd} = \frac{1501000 - 0.27 \times 3617.6^2 / (4 \times 9.5) \times 275}{1.0} = \mathbf{386.8 \text{ kN}}$$

$$386.8 \text{ kNm} > 376.5 \text{ kNm}$$

\therefore cross-section resistance to combined bending and shear is acceptable

Conclusion

A $406 \times 178 \times 74 \text{ UB}$ in grade S275 steel is suitable for the arrangement and loading shown by Fig. 6.13

- $N_{Ed} < 0.25 \cdot N_{pl_Rd} = 649.69 \text{ kN}$.
- $N_{Ed} < 0.5 \cdot h_w \cdot t_w \cdot f_y / \Gamma_{M0} = 497.42 \text{ kN}$.
Therefore, No allowance for the effect of axial force.
- $M_{ny_Rd} = M_{ply_Rd} = \mathbf{386.55 \text{ kN-m}}$.
- $R_{maxy} = M_{Edy} / M_{ny_Rd} = 0.951 < 1.000 \rightarrow \text{O.K.}$

- $N_{Ed} < h_w \cdot t_w \cdot f_y / \Gamma_{M0} = 1675.52 \text{ kN}$.
Therefore, No allowance for the effect of axial force.
- $M_{nz_Rd} = M_{plz_Rd} = 73.42 \text{ kN-m}$.
- $R_{maxz} = M_{Edz} / M_{nz_Rd} = 0.000 < 1.000 \rightarrow \text{O.K.}$

- $R_{max2} = \text{MAX}[R_{maxy}, R_{maxz}] = 0.951 < 1.000 \rightarrow \text{O.K.}$

[Reference]

L.Gardner and D.A.Nethercot, Designers' Guide to
EN 1993-1-1, The Steel Construction Institute,
Thomas Telford, 53-55 (Example 6.5)

3.2 Cross-section resistance under combined bending and compression

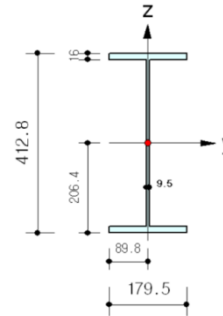
A member is to be designed to carry a combined major axis moment and an axial force. In this example, a cross-sectional check is performed to determine the maximum bending moment that can be carried by a $457 \times 191 \times 98$ UB in grade S235 steel, in the presence of an axial force of 1400 kN.

3.2.1 Material Properties

Material	S275	$f_y = 275 \text{ N/mm}^2$	$E_s = 210 \text{ GPa}$
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3.2.2 Section Properties

Section Name	406 x 178 x 74 UB
Depth (H)	412.8 mm
Width (B)	179.5 mm
Flange Thickness (T_f)	16.0 mm
Web Thickness (T_w)	9.5 mm
Gross sectional area (A)	9450.0 mm ²
Shear area (A_{sz})	4184.0 mm ²



3.2.3 Comparison of Design Results

	midas Gen	Example book	Error (%)
Shear resistance	689.25 kN	689.2 kN	0.01%
Bending resistance	412.50 kNm	412.0 kNm	0.12%
Combined resistance	386.55 kNm	386.8 kNm	0.06%

3.2.4 Detailed comparison

midas Gen	Example book
1. Cross-section classification (). Determine classification of compression outstand flanges. [Eurocode3:05 Table 5.2 (Sheet 2 of 3), EN 1993-1-5] -. $e = \text{SQRT}(235/f_y) = 1.00$ -. $b/t = \text{BTR} = 4.11$ -. $\sigma_1 = 112000.000 \text{ KPa}$. -. $\sigma_2 = 112000.000 \text{ KPa}$. -. $\text{BTR} < 9 \cdot e$ (Class 1: Plastic). (). Determine classification of compression Internal Parts. [Eurocode3:05 Table 5.2 (Sheet 1 of 3), EN 1993-1-5] -. $e = \text{SQRT}(235/f_y) = 1.00$	1. Cross-section classification under pure compression (clause 5.5.2) $\epsilon = \sqrt{235/f_y} = \sqrt{235/235} = 1.00$ Outstand flanges (Table 5.2, sheet 2): $C = (b - t_w - 2r)/2 = 80.5 \text{ mm}$ $c/t_f = 80.5/19.6 = 4.11$ Limit for Class 1 flange = $9\epsilon = 9.0$ $9.0 > 4.11 \quad \therefore$ flange is Class 1 Web – internal part in bending (Table 5.2, sheet 1): $C = h - 2t_f - 2r = 407.6 \text{ mm}$ $c/t_w = 407.6/11.4 = 35.75$

- $d/t = HTR = 35.75$
- $\sigma_1 = 112000.000 \text{ KPa}$.
- $\sigma_2 = 112000.000 \text{ KPa}$.
- $HTR < 38 \cdot e$ (**Class 2 : Compact**).

2. Check Axial and Bending Resistance

(). Check slenderness ratio of axial compression member (Kl/i). [Eurocode3:05 6.3.1]

- $Kl/i = 32.3 < 200.0 \rightarrow \text{O.K.}$

(). Calculate axial compressive resistance ($N_{c,Rd}$).

[Eurocode3:05 6.1, 6.2.4]

- $N_{c,Rd} = f_y \cdot \text{Area} / \gamma_{M0}$
= **2937.50 kN**

(). Check ratio of axial resistance ($N_{Ed}/N_{c,Rd}$).

$$N_{Ed} = 1400.00$$

- $\frac{N_{Ed}}{N_{c,Rd}} = \frac{1400.00}{2937.50} = 0.477 < 1.000 \rightarrow \text{O.K.}$

(). Calculate plastic resistance moment about major axis.

[Eurocode3:05 6.1, 6.2.5]

- $W_{ply} = 0.0022 \text{ m}^3$.
- $M_{c,Rd} = W_{ply} \cdot f_y / \gamma_{M0} = 524.05 \text{ kN-m}$.

- $N_{Ed} > 0.25 \cdot N_{pl,Rd} = 695.92 \text{ kN}$.

- $N_{Ed} > 0.5 \cdot h_w \cdot t_w \cdot f_y / \gamma_{M0} = \mathbf{573.31 \text{ kN}}$.

Therefore, Allowance for the effect of axial force.

3. Check Interaction of Combined Resistance

(). Calculate Major reduced design resistance of bending and shear. [Eurocode3:05 6.2.8 (6.30)]

- In case of $V_{Edz} / V_{pl,Rdz} < 0.5$
- $M_{y,Rd} = M_{c,Rd} = \mathbf{524.05 \text{ kN-m}}$.

(). Calculate Minor reduced design resistance of bending and shear. [Eurocode3:05 6.2.8 (6.30)]

- In case of $V_{Edy} / V_{pl,Rdy} < 0.5$
- $M_{z,Rd} = M_{c,Rdz} = 89.06 \text{ kN-m}$.

(). Check interaction ratio of bending and axial force member.

[Eurocode3:05 6.2.9 (6.31 ~ 6.41)] - Class1 or Class2

- $n = N_{Ed} / N_{pl,Rd} = 0.477$
- $a = \text{MIN}[(\text{Area} - 2b \cdot t_f) / \text{Area}, 0.5] = 0.395$
- $\alpha = 2.000$
- $\beta = \text{MAX}[5 \cdot n, 1.0] = 2.383$
- $N_{Ed} > 0.25 \cdot N_{pl,Rd} = 695.92 \text{ kN}$.
- $N_{Ed} > 0.5 \cdot h_w \cdot t_w \cdot f_y / \gamma_{M0} = 573.31 \text{ kN}$.
- Therefore, Allowance for the effect of axial force.
- $M_{ny,Rd} = \text{MIN}[M_{ply,Rd} \cdot (1-n) / (1-0.5 \cdot a), M_{ply,Rd}]$
= **341.88 kN-m**.

Limit for Class 2 web = $38 \cdot e = 38.0$

$38.0 > 35.75 \therefore \text{web is Class 2}$

Under pure compression, the overall cross-section classification is therefore Class 2.

2. Bending and axial force (clause 6.2.9.1)

No reduction to the plastic resistance moment due to the effect of axial force is required when both of the following criteria are satisfied.

$$N_{Ed} \leq 0.25 N_{pl,Rd}$$

And

$$N_{Ed} = \frac{0.5 h_w t_w f_y}{\gamma_{M0}}$$

$$N_{Ed} = 1400 \text{ kN}$$

$$N_{pl,Rd} = \frac{A f_y}{\gamma_{M0}} = \frac{12500 \times 235}{1.0} = \mathbf{2937.5 \text{ kN}}$$

$$0.25 N_{pl,Rd} = 733.9 \text{ kN}$$

$733.9 \text{ kN} < 1400 \text{ kN} \therefore \text{equation (6.33) is not satisfied}$

$$\frac{0.5 h_w t_w f_y}{\gamma_{M0}} = \frac{0.5 \times [467.2 - (2 \times 19.6)] \times 11.4 \times 235}{1.0} = \mathbf{573.3 \text{ kN}}$$

$573.3 \text{ kN} < 1400 \text{ kN} \therefore \text{equation (6.34) is not satisfied}$

Therefore, allowance for the effect of axial force on the plastic moment resistance of the cross-section must be made.

3. Reduced plastic moment resistance (clause 6.2.9.1(5))

$$M_{N,y,Rd} = M_{pl,y,Rd} \frac{1-n}{1-0.5a} \quad \text{but } M_{N,y,Rd} \leq M_{pl,y,Rd}$$

Where

$$n = N_{Ed} / M_{pl,y,Rd} = 1400 / 2937.5 = 0.48$$

$$a = (A - 2bt_f) / A = [12500 - (2 \times 192.8 \times 19.6)] / 12500 = 0.40$$

$$M_{pl,y,Rd} = \frac{W_{pl,y} f_y}{\gamma_{M0}} = \frac{2232000 \times 235}{1.0} = \mathbf{524.5 \text{ kNm}}$$

$$\Rightarrow M_{N,y,Rd} = 524.5 \times \frac{1-0.48}{1-(0.5 \times 0.40)} = \mathbf{342.2 \text{ kNm}}$$

Conclusion

In order to satisfy the cross-sectional checks of clause 6.2.9, the maximum bending moment that can be carried by a $457 \times 191 \times 98 \text{ UB}$ in grade S235 steel, in the presence of an axial force 1400 kN is 342.2 kNm.

[Reference]

L.Gardner and D.A.Nethercot, Designers' Guide to EN 1993-1-1, The Steel Construction Institute, Thomas Telford, 57-59 (Example 6.6)

3.3 Buckling resistance of a compression member

A circular hollow section (CHS) member is to be used as an internal column in a multi-storey building. The column has pinned boundary conditions at each end, and the inter-storey height is 4m, as shown in the right figure. The critical combination of actions results in a design axial force of 1630 kN. Assess the suitability of a hot-rolled 244.5 x 10 CHS in grade S275 steel for this application.

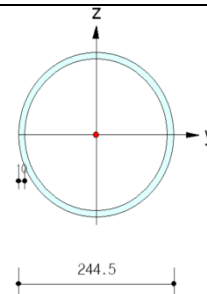


3.3.1 Material Properties

Material	S275	$f_y = 275 \text{ N/mm}^2$	$E_s = 210 \text{ GPa}$
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3.3.2 Section Properties

Section Name	244.5 X 10 CHS
Thickness (T)	10.0 mm
Gross sectional area (A)	7370 mm^2
Modulus of Elasticity ($W_{el,y}$)	$415\,000 \text{ mm}^3$
Modulus of Elasticity ($W_{pl,y}$)	$550\,000 \text{ mm}^3$
Moment of Inertia (I)	$50\,750\,000 \text{ mm}^4$



3.3.3 Analysis Model

Loading condition	
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3.3.4 Comparison of Design Results

	midas Gen	Example book	Error (%)
Shear resistance	2026.75 kN	2026.8 kN	0.00%
Bending resistance	1836.70 kNm	1836.5 kNm	0.06%

3.3.5 Detailed comparison

midas Gen	Example book
<p>1. Class of Cross Section (). Determine classification of tublar section(hollow pipe). [Eurocode3:05 Table 5.2 (Sheet 3 of 3)] - . e = $\sqrt{235/f_y} = 0.92$ - . d/t = DTR = 24.45 - . DTR < 50 * e^2 (Class 1 : Plastic).</p> <p>2. Check Axial Resistance (). Check slenderness ratio of axial compression member (Kl/i) [Eurocode3:05 6.3.1] - . Kl/i = 48.2 < 200.0 ---> O.K.</p> <p>(). Calculate axial compressive resistance (Nc_Rd). [Eurocode3:05 6.1, 6.2.4] - . Nc_Rd = fy * Area / Gamma_M0 = 2026.75 kN.</p> <p>(). Check ratio of axial resistance (N_Ed/Nc_Rd). $\frac{N_{Ed}}{N_{c,Rd}} = \frac{1630.00}{2026.75} = 0.804 < 1.000 \text{ ---> O.K.}$</p> <p>(). Calculate buckling resistance of compression member (Nb_Rdy, Nb_Rdz). [Eurocode3:05 6.3.1.1, 6.3.1.2] - . Beta_A = Aeff / Area = 1.000 - . Lambda1 = Pi * SQRT(Es/fy) = 86.815 - . Lambda_by = {(KLy/iy)/Lambda1} * SQRT(Beta_A) = 0.555 - . Ncry = Pi^2 * Es * Ryy / KLy^2 = 6571.49 kN. - . Lambda_by > 0.2 and N_Ed/Ncry > 0.04 --> Need to check. - . Alphay = 0.210 - . Phiy = 0.5 * [1 + Alphay*(Lambda_by-0.2) + Lambda_by^2] = 0.691 - . Xiy = MIN [1 / [Phiy + SQRT(Phiy^2 - Lambda_by^2)], 1.0] = 0.906 - . Nb_Rdy = Xiy * Beta_A * Area * fy / Gamma_M1 = 1836.70 kN. - . Lambda_bz = {(KLz/iz)/Lambda1} * SQRT(Beta_A) = 0.555 - . Ncrz = Pi^2 * Es * Rzz / KLz^2 = 6571.49 kN. - . Lambda_bz > 0.2 and N_Ed/Ncrz > 0.04 --> Need to check. - . Alphaz = 0.210 - . Phiz = 0.5 * [1 + Alphaz*(Lambda_bz-0.2) + Lambda_bz^2] = 0.691 - . Xiz = MIN [1 / [Phiz + SQRT(Phiz^2 - Lambda_bz^2)], 1.0] = 0.906 - . Nb_Rdz = Xiz * Beta_A * Area * fy / Gamma_M1 = 1836.70 kN.</p>	<p>1. Cross-section classification (clause 5.5.2) $\epsilon = \sqrt{235/f_y} = \sqrt{235/275} = 0.92$ Tubular sections (Table 5.2, sheet 3): d/t = 244.5/10.0 = 24.5 Limit for Class 1 section = 50 ϵ^2 = 42.7 42.7 > 24.5 \therefore section is Class 1</p> <p>2. Cross Section Compression resistance (clause 6.2.4) $N_{c,Rd} = \frac{A f_y}{\gamma_{M0}} \quad \text{for Class 1,2 or 3 cross-sections}$ $\therefore N_{c,Rd} = \frac{7370 \times 275}{1.00} = 2026.8 \times 10^3 \text{ N} = \mathbf{2026.8 \text{ KN}}$ 2026.8 > 1630 KN \therefore cross-section resistance is acceptable</p> <p>3. Member Buckling resistance in compression (clause 6.3.1) $N_{b,Rd} = \frac{\chi A f_y}{\gamma_{M1}} \quad \text{for Class 1,2 or 3 cross-sections}$ $\chi = \frac{1}{\phi + \sqrt{\phi^2 - \lambda^2}} \quad \text{but } \chi \leq 1.0$ where $\phi = 0.5[1 + \alpha(\lambda - 0.2) + \lambda^2]$ and $\lambda = \sqrt{\frac{A f_y}{N_{cr}}} \quad \text{for Class 1,2 or 3 cross-sections}$ <p><i>Elastic critical force and non-dimensional slenderness for flexural buckling</i> $N_{cr} = \frac{\pi^2 EI}{L_{cr}^2} = \frac{\pi^2 \times 210000 \times 50730000}{4000^2} = \mathbf{6571 \text{ KN}}$ $\therefore \lambda = \sqrt{\frac{7370 \times 275}{6571 \times 10^3}} = 0.56$</p> <p><i>Selection of buckling curve and imperfection factor α</i> For a hot-rolled CHS, use buckling curve a (Table 6.5 (Table 6.2 of EN 1993-1-1)). For curve buckling curve a, $\alpha = 0.21$ (Table 6.4 (Table 6.1 of EN 1993-1-1)).</p> <p><i>Buckling curves</i> $\phi = 0.5[1 + 0.21 \times (0.56 - 0.2) + 0.56^2] = \mathbf{0.69}$ $\chi = \frac{1}{0.69 + \sqrt{0.69^2 - 0.56^2}}$ $N_{b,Rd} = \frac{0.91 \times 7370 \times 275}{1.0} = 1836.5 \times 10^3 \text{ N} = \mathbf{1836.5 \text{ KN}}$ 1836.5 > 1630 KN \therefore buckling resistance is acceptable</p> </p>

(). Check ratio of buckling resistance ($N_{Ed}/N_{b,Rd}$).

-. $N_{b,Rd} = \text{MIN}[N_{b,Rdy}, N_{b,Rdz}] = 1836.70 \text{ kN}$.

$N_{Ed} \quad 1630.00$

-. $\frac{N_{Ed}}{N_{b,Rd}} = \frac{1630.00}{1836.70} = 0.887 < 1.000 \rightarrow \text{O.K.}$

$N_{b,Rd} \quad 1836.70$

Conclusion

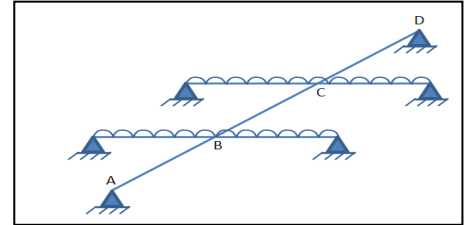
The chosen cross-section, $244.5 \times 10 \text{ CHS}$, in grade S275 steel is acceptable.

[Reference]

L.Gardner and D.A.Nethercot, Designers' Guide to EN 1993-1-1, The Steel Construction Institute, Thomas Telford, 66-68 (Example 6.7)

3.4 I-section beam design under shear force and bending moment

A simply supported primary beam is required to span 10.8m and to support two secondary beams as shown in Fig.6.24. The secondary beams are connected through pin plates to the web of the primary beam, and full lateral restraint may be assumed at these points. Select a suitable member for the primary beam assuming grade S275 steel.

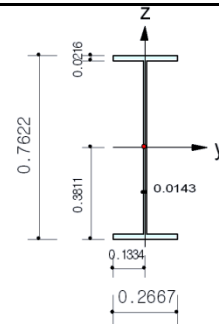


3.4.1 Material Properties

Material	S275	$f_y = 275 \text{ N/mm}^2$	$E_s = 210 \text{ GPa}$
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3.4.2 Section Properties

Section Name	762 X 267 X 173 UB
Depth (H)	762.2 mm
Width (B)	266.7 mm
Flange Thickness (T_f)	21.6 mm
Web Thickness (T_w)	14.3 mm
Gross sectional area (A)	22 000 mm ²
Shear area (A_{sz})	11 500.2 mm ²



3.4.3 Analysis Model

Loading condition		
Beam Diagram	SF	
	BM	

3.4.4 Comparison of Design Results

	midas Gen	Example book	Error (%)
Shear resistance	1958.93kN	1959.00kN	0.00%
Bending resistance	1705.00kNm	1704.00kNm	0.06%
Combined resistance	1511.41kN	1469.00kN	2.81%

3.4.5 Detailed comparison

midas Gen	Example book
<p>1. Cross-section classification</p> <p>(). compression outstand flanges (Flange)</p> <ul style="list-style-type: none"> - $e = \sqrt{235/f_y} = 0.92$ - $b/t = BTR = 5.08$ - $\sigma_1 = 228745.362 \text{ KPa}$. - $\sigma_2 = 228745.362 \text{ KPa}$. - $BTR < 9 \cdot e$ (Class 1 : Plastic). <p>(). bending Internal Parts (Web)</p> <ul style="list-style-type: none"> - $e = \sqrt{235/f_y} = 0.92$ - $d/t = HTR = 47.97$ - $\sigma_1 = 588373.896 \text{ KPa}$. - $\sigma_2 = -588373.896 \text{ KPa}$. - $HTR < 72 \cdot e$ (Class 1 : Plastic). <p>2. Shear resistance of cross-section</p> <p>(). Calculate shear area.</p> <p>[Eurocode3:05 6.2.6, EN1993-1-5:04 5.1 NOTE 2]</p> <ul style="list-style-type: none"> - $\eta = 1.2$ ($F_y < 460 \text{ MPa}$.) - $r = 0.0165 \text{ m}$. - $A_v = \text{Area} - h_w \cdot t_w = 0.0117 \text{ m}^2$. - $Avz1 = \eta \cdot h_w \cdot t_w = 0.0123 \text{ m}^2$. - $Avz2 = \text{Area} - 2 \cdot B \cdot t_f + (t_w + 2 \cdot r) \cdot t_f = 0.0115 \text{ m}^2$. - $Avz = \text{MAX}[Avz1, Avz2] = 0.0123 \text{ m}^2$. <p>(). Plastic shear resistance (V_{pl_Rdz})</p> <p>[Eurocode3:05 6.1, 6.2.6]</p> <ul style="list-style-type: none"> - $V_{pl_Rdz} = [Avz \cdot f_y / \sqrt{3}] / \Gamma_{M0}$ - $= 1958.93 \text{ kN}$. - $Avz = 1.23380 \text{e-}002$ - $F_y = 2.75000 \text{e+}005$ - $\Gamma_{M0} = 1.00$ <p>(). Shear Buckling Check [Eurocode3:05 6.2.6]</p> <ul style="list-style-type: none"> - $HTR < 72 \cdot e / \eta$ ---> No need to check! - $e = \sqrt{235/f_y} = 0.92$ - $d/t = HTR = 47.97$ 	<p>1. Cross-section classification</p> <p>$\epsilon = \sqrt{235/f_y} = \sqrt{235/275} = 0.92$</p> <p>Outstand flanges (Table 5.2, sheet 2):</p> <p>$C = (b - t_w - 2r)/2 = 109.7 \text{ mm}$</p> <p>$c/t_f = 109.7/21.6 = 5.08$</p> <p>Limit for Class 1 flange $= 9\epsilon = 8.32$</p> <p>$8.32 > 5.08 \quad \therefore \text{flange is Class 1}$</p> <p>Web – internal part in bending (Table 5.2, sheet 1):</p> <p>$C = h - 2t_f - 2r = 686.0 \text{ mm}$</p> <p>$c/t_w = 686.0/14.3 = 48.0$</p> <p>Limit for Class 1 web $= 72\epsilon = 66.6$</p> <p>$66.6 > 48.0 \quad \therefore \text{web is Class 1}$</p> <p>2. Shear resistance of cross-section</p> <p>$V_{p1,Rd} = \frac{A_v(f_y/3)}{\gamma_{M0}}$</p> <p>For a rolled I section, loaded parallel to the web, the shear area A_v, is given by</p> <p>$A_v = A - 2bt_f + (t_w + r) t_f$ (but not less than $\eta h_w t_w$)</p> <p>$\eta = 1.2$ (from Eurocode 3 –part 1.5, though the UK National Annex may specify an alternative value).</p> <p>$h_w = (h - 2t_f) = 762.2 - (2 \times 21.6) = 719.0 \text{ mm}$</p> <p>$\therefore A_v = 22000 - (2 \times 266.7 \times 21.6) + (14.3 + 16.5) \times 21.6 = 9813 \text{ mm}^2$</p> <p>(but not less than $1.2 \times 719.0 \times 14.3 = 12338 \text{ mm}^2$)</p> <p>$V_{p1,Rd} = \frac{12338 \times (275/3)}{1.00} = 1959000 \text{ N} = 1959 \text{ KN}$</p> <p>Shear buckling need not be considered, provided</p> <p>$\frac{h_w}{t_w} \leq 72 \frac{\epsilon}{\eta}$ for unstiffened webs</p> <p>$72 \frac{\epsilon}{\eta} = 72 \times \frac{0.92}{1.2} = 55.5$</p> <p>Actual $h_w/t_w = 719.0/14.3 = 50.3$</p> <p>$50.3 \leq 55.5 \quad \therefore \text{no shear buckling check required}$</p>

(). Check ratio of shear resistance ($V_{Edz}/V_{pl,Rdz}$).

(LCB = 1, POS = J)

- Applied shear force : $V_{Edz} = 493.17$ kN.

$$-\frac{V_{Edz}}{V_{pl,Rdz}} = \frac{493.17}{1958.93} = 0.252 < 1.000 \rightarrow \text{O.K.}$$

3. Bending resistance of cross-section

(). Plastic resistance moment about major axis.

[Eurocode3:05 6.1, 6.2.5]

- $W_{ply} = 0.0062$ m³.

$$-\text{Mc}_{Rdy} = W_{ply} \cdot f_y / \gamma_{M0} = 1705.00 \text{ kN-m.}$$

(). Ratio of moment resistance (M_{Edy}/Mc_{Rdy}).

$$-\frac{M_{Edy}}{\text{Mc}_{Rdy}} = \frac{1232.94}{1705.00} = 0.723 < 1.000 \rightarrow \text{O.K.}$$

(). Plastic resistance moment about minor axis.

[Eurocode3:05 6.1, 6.2.5]

- $W_{plz} = 0.0008$ m³.

$$-\text{Mc}_{Rdz} = W_{plz} \cdot f_y / \gamma_{M0} = 221.92 \text{ kN-m.}$$

(). Ratio of moment resistance (M_{Edz}/Mc_{Rdz}).

$$-\frac{M_{Edz}}{\text{Mc}_{Rdz}} = \frac{0.00}{221.92} = 0.000 < 1.000 \rightarrow \text{O.K.}$$

4. Combined bending and shear resistance

(). Major reduced design resistance of bending and shear [Eurocode3:05 6.2.8 (6.30)]

- In case of $V_{Edz} / V_{pl,Rdz} < 0.5$
 - $M_{y,Rd} = \text{Mc}_{Rdy} = 1705.00$ kN-m.

(). Minor reduced design resistance of bending and shear [Eurocode3:05 6.2.8 (6.30)]

- In case of $V_{Edy} / V_{pl,Rdy} < 0.5$
 - $M_{z,Rd} = \text{Mc}_{Rdz} = 221.92$ kN-m.

(). General interaction ratio [Eurocode3:05 6.2.1 (6.2)] - Class1 or Class2

$$-\text{Rmax1} = \frac{N_{Ed}}{N_{Rd}} + \frac{M_{Edy}}{M_{y,Rd}} + \frac{M_{Edz}}{M_{z,Rd}} = 0.723 < 1.000 \rightarrow \text{O.K.}$$

(). Interaction ratio of bending and axial force member [Eurocode3:05 6.2.9 (6.31 ~ 6.41)]

- Class1 or Class2

- Alpha = 2.000

- Beta = MAX[5*n, 1.0] = 1.000

1959 > 493.2 KN

∴ shear resistance is acceptable

3. Bending resistance of cross-section

$$M_{c,y,Rd} = \frac{W_{pl,y} f_y}{\gamma_{M0}} \quad \text{for Class 1 or 2 cross-sections}$$

EN 1993-1-1 recommends a numerical value of $\gamma_{M0} = 1.00$ (through for buildings to be constructed in the UK, reference should be made to the National Annex). The design bending resistance of the cross-section

$$M_{c,y,Rd} = \frac{6198 \times 10^3 \times 275}{1.00} = 1704 \times 10^6 \text{ Nmm} = 1704 \text{ kNm}$$

1704 kNm > 1362 kNm

∴ cross-section resistance in bending is acceptable

4. Combined bending and shear resistance

Clause 6.2.8 states that provided the shear force V_{Ed} is less than half the plastic shear resistance $V_{pl,Rd}$ its effect on the moment resistance may be neglected except where shear buckling reduces the section resistance. In this case, there is no reduction for shear buckling (see above), and maximum shear force ($V_{Ed}=493.2$ kN) is less than half the plastic shear resistance ($V_{pl,Rd}=1959$ kN). Therefore, resistance under combined bending and shear is **acceptable**.

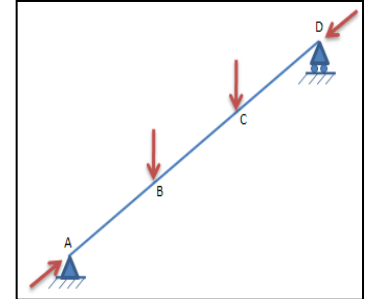
- $n = N_{Ed} / N_{pl_Rd} = 0.000$
- $a = \text{MIN}[(\text{Area} - 2b \cdot t_f) / \text{Area}, 0.5] = 0.476$
- $M_{ny_Rd} = \text{MIN}[M_{ply_Rd} \cdot (1-n) / (1-0.5 \cdot a), M_{ply_Rd}] = 1705.00 \text{ kN-m.}$
- $R_{maxy} = M_{Edy} / M_{ny_Rd} = 0.723 < 1.0 \rightarrow$
O.K.
- In case of $n < a$
- $M_{nz_Rd} = M_{plz_Rd} = 221.92 \text{ kN-m.}$
- $R_{maxz} = M_{Edz} / M_{nz_Rd} = 0.0 < 1.0 \rightarrow$ O.K.
- $R_{max2} = \max[R_{maxy}, R_{maxz}] = 0.723 < 1.0 \rightarrow$
O.K.
- $R_{max} = \max[R_{max1}, R_{max2}] = 0.723 < 1.0 \rightarrow$ **O.K**

[Reference]

L.Gardner and D.A.Nethercot, Designers' Guide to EN 1993-1-1, The Steel Construction Institute, Thomas Telford, 74-79 (Example 6.8)

3.5 Member resistance under combined major axis bending and axial compression

A rectangular hollow section (RHS) member is to be used as a primary floor beam of 7.2 m span in a multi-storey building. Two design point loads of 58 kN are applied to the primary beam (at locations B and C) from secondary beams, as shown in the right figure. The secondary beams are connected through fin plates to the webs of the primary beam, and full lateral and torsional restraint may be assumed at these points. The primary beam is also subjected to a design axial force of 90 kN.



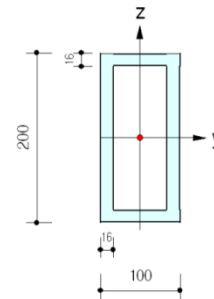
Assess the suitability of a hot-rolled 200 X 100 X 16 RHS in grade S355 steel for this application. In this example the interaction factors k_{ij} (for member checks under combined bending and axial compression) will be determined using alternative method 1 (Annex A)

3.5.1 Material Properties

Material	S355	$f_y = 355 \text{ N/mm}^2$	$E_s = 210 \text{ GPa}$
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3.5.2 Section Properties

Section Name	200 X 100 X 16 RHS
Depth (H)	200.0 mm
Width (B)	100.0 mm
Flange Thickness (T_f)	16.0 mm
Web Thickness (T_w)	16.0 mm
Gross sectional area (A)	8300.0 mm ²
Shear area (A_{sz})	5533.3 mm ²



3.5.3 Analysis Model

Loading condition		
Beam Diagram	SF	
	BM	

3.5.4 Comparison of Design Results

	midas Gen	Example book	Error (%)
Axial resistance	2999.75kN	2946.50 kN	1.78%
Shear resistance	1154.60kN	1134.00kN	1.78%
Bending resistance	179.28kNm	174.30 kNm	2.78%
Buckling resistance	1247.29kN	1209.00kN	3.07%

3.5.5 Detailed comparison

midas Gen	Example book
<p>1. Cross-section classification</p> <p>(). Determine classification of compression Internal Parts.</p> <p>[Eurocode3:05 Table 5.2 (Sheet 1 of 3), EN 1993-1-5]</p> <ul style="list-style-type: none"> - $e = \sqrt{235/f_y} = 0.81$ - $d/t = HTR = 3.25$ - $\sigma_1 = 0.376 \text{ kN/mm}^2$. - $\sigma_2 = 0.376 \text{ kN/mm}^2$. - $HTR < 33 \cdot e$ (Class 1 : Plastic). <p>(). Determine classification of bending and compression Internal Parts.</p> <p>[Eurocode3:05 Table 5.2 (Sheet 1 of 3), EN 1993-1-5]</p> <ul style="list-style-type: none"> - $e = \sqrt{235/f_y} = 0.81$ - $d/t = HTR = 9.50$ - $\sigma_1 = 0.624 \text{ kN/mm}^2$. - $\sigma_2 = -0.603 \text{ kN/mm}^2$. - $\Psi = [2 \cdot (N_{sd}/A) \cdot (1/f_y)] - 1 = -0.940$ - $\alpha = 0.524 > 0.5$ - $HTR < 396 \cdot e / (13 \cdot \alpha - 1)$ (Class 1 : Plastic). <p>2. Check Axial Resistance.</p> <p>(). Check slenderness ratio of axial compression member (Kl/i). [Eurocode3:05 6.3.1]</p> <ul style="list-style-type: none"> - $Kl/i = 64.3 < 200.0 \rightarrow \text{O.K.}$ <p>(). Calculate axial compressive resistance ($N_{c,Rd}$). [Eurocode3:05 6.1, 6.2.4]</p> <ul style="list-style-type: none"> - $N_{c,Rd} = f_y \cdot \text{Area} / \gamma_{M0} = \mathbf{2999.75 \text{ kN.}}$ <p>(). Check ratio of axial resistance ($N_{Ed}/N_{c,Rd}$).</p> <p>$N_{Ed} \quad 90.00$</p> <p>- $\frac{\text{-----}}{N_{c,Rd} \quad 2999.75} = \text{-----} = 0.030 < 1.000 \rightarrow \text{O.K.}$</p>	<p>1. Cross-section classification (clause 5.5.2)</p> <p>$\epsilon = \sqrt{235/f_y} = \sqrt{235/355} = 0.81$</p> <p>For a RHS the compression width c may be taken as h (or b) – 3t.</p> <p>Flange-internal part in compression (Table 5.2, sheet 1):</p> <p>$C = b - 3t = 100 - (3 \times 16.0) = 52.0 \text{ mm}$</p> <p>$c/t = 52.0/16.0 = 3.25$</p> <p>Limit for Class 1 flange $= 33\epsilon = 26.85$</p> <p>$26.85 > 3.25 \quad \therefore \text{flange is Class 1}$</p> <p>Web – internal part in compression (Table 5.2, sheet 1):</p> <p>$C = h - 3t = 200.0 - (3 \times 16.0) = 152.0 \text{ mm}$</p> <p>$c/t = 152.0/16.0 = 9.50$</p> <p>Limit for Class 1 web $= 33\epsilon = 26.85$</p> <p>$26.85 > 9.50 \quad \therefore \text{web is Class 1}$</p> <p>The overall cross-section classification is therefore Class 1 (under pure compression).</p> <p>2. Compression resistance of cross-section (clause 6.2.4)</p> <p>The design compression resistance of the cross-section</p> <p>$N_{c,Rd}$</p> <p>$N_{c,Rd} = \frac{A f_y}{\gamma_{M0}} \quad \text{for class 1,2 and 3 cross-sections}$</p> <p>$= \frac{8300 \times 355}{1.00} = 2946500 \text{ N} = \mathbf{2946.5 \text{ KN}}$</p> <p>$2946.5 \text{ KN} > 90 \text{ KN} \quad \therefore \text{acceptable}$</p>

3. Check Bending Moment Resistance About Major Axis

(). Calculate plastic resistance moment about major axis.

[Eurocode3:05 6.1, 6.2.5]

$$- W_{ply} = 0.0005 \text{ m}^3.$$

$$- M_{c,Rd} = W_{ply} * f_y / \gamma_{M0} = 179.28 \text{ kN-m}.$$

(). Check ratio of moment resistance ($M_{Ed}/M_{c,Rd}$).

$$M_{Ed} \quad 139.20$$

$$- \frac{\quad}{\quad} = \frac{\quad}{\quad} = 0.776 < 1.000 \rightarrow \text{O.K.}$$

$$M_{c,Rd} \quad 179.28$$

4. Shear resistance of cross-section

(). Calculate shear area.

[Eurocode3:05 6.2.6, EN1993-1-5:04 5.1 NOTE 2]

$$- A_{vy} = \text{Area} * B/(B+h) = 0.0028 \text{ m}^2.$$

$$- A_{vz} = \text{Area} * h/(B+h) = 0.0056 \text{ m}^2.$$

(). Calculate plastic shear resistance in local-z direction ($V_{pl,Rdz}$).

[Eurocode3:05 6.1, 6.2.6]

$$- V_{pl,Rdz} = [A_{vz} * f_y / \sqrt{3}] / \gamma_{M0} = 1154.60 \text{ kN}$$

(). Shear Buckling Check. [Eurocode3:05 6.2.6]

$$- HTR < 72 * e / \eta \rightarrow \text{No need to check!}$$

(). Check ratio of shear resistance ($V_{Edz}/V_{pl,Rdz}$).

$$(LCB = 1, POS = J)$$

$$- \text{Applied shear force : } V_{Edz} = 58.00 \text{ kN.}$$

$$V_{Edz} \quad 58.00$$

$$- \frac{\quad}{\quad} = \frac{\quad}{\quad} = 0.050 < 1.000 \rightarrow \text{O.K.}$$

$$V_{pl,Rdz} \quad 1154.60$$

5. CHECK INTERACTION OF COMBINED RESISTANCE

(). Calculate Major reduced design resistance of bending and shear. [Eurocode3:05 6.2.8 (6.30)]

$$- \text{In case of } V_{Edz} / V_{pl,Rdz} < 0.5$$

$$- M_{y,Rd} = M_{c,Rd} = 179.28 \text{ kN-m}.$$

(). Calculate Minor reduced design resistance of bending and shear. [Eurocode3:05 6.2.8 (6.30)]

$$- \text{In case of } V_{Edy} / V_{pl,Rdy} < 0.5$$

$$- M_{z,Rd} = M_{c,Rd} = 105.44 \text{ kN-m}.$$

(). Check general interaction ratio.

[Eurocode3:05 6.2.1 (6.2)] - Class1 or Class2

3. Bending resistance of cross-section (clause 6.2.5)

Maximum bending moment

$$M_{y,Ed} = 2.4 \times 58 = 139.2 \text{ kN}$$

The design major axis bending resistance of the cross-section.

$$M_{c,y,Rd} = \frac{W_{pl,y} f_y}{\gamma_{M0}} \quad \text{for Class 1 or 2 cross-sections}$$

$$= \frac{491000 \times 355}{1.00} = 174.3 \times 10^6 \text{ Nmm}$$

$$= 174.3 \text{ kNm}$$

$$174.3 \text{ kNm} > 139.2 \text{ kNm} \quad \therefore \text{acceptable}$$

4. Shear resistance of cross-section (clause 6.2.6)

Maximum shear force

$$V_{ED} = 58.0 \text{ kN}$$

The design plastic shear resistance of the cross-section

$$V_{pl,Rd} = \frac{A_v (f_y / 3)}{\gamma_{M0}}$$

Or a rolled RHS of uniform thickness, loaded parallel to the depth, the shear area A_v is given by

$$A_v = Ah / (b + h) = 8300 \times 200 / (100 + 200)$$

$$= 5533.3 \text{ mm}^2$$

Shear buckling need to not be considered, provided

$$\frac{h_w}{t_w} \leq 72 \frac{\epsilon}{\eta} \quad \text{for unstiffened webs}$$

$\eta = 1.2$ (from EN 1993-1-5, though the UK National Annex may specify an alternative value).

$$h_w = (h - 2t) = 200 - (2 \times 16.0) = 168 \text{ mm}$$

$$72 \frac{\epsilon}{\eta} = 72 \times \frac{0.81}{1.2} = 48.8$$

$$\text{Actual } h_w / t_w = 200 / 16.0 = 12.5$$

$$12.5 \leq 48.8 \quad \therefore \text{no shear buckling check required}$$

$$1134 > 58.0 \text{ kN} \quad \therefore \text{shear resistance is acceptable}$$

5. Cross-section resistance under Bending, Shear and axial force (clause 6.2.10)

Provided the shear force V_{ED} is less than 50% of the design plastic shear resistance $V_{pl,Rd}$ and provided shear buckling is not a concern, then the cross-section need only satisfy the requirements for bending and axial force (clause 6.2.9).

In this case $V_{ED} < 0.5 V_{pl,Rd}$, and shear buckling is not a concern (see above). Therefore, cross-section only need be checked for bending and axial force.

No reduction to the major axis plastic resistance moment

$$\begin{aligned}
 & \frac{N_{Ed}}{N_{Rd}} + \frac{M_{Edy}}{M_{Rd}} + \frac{M_{Edz}}{M_{Rd}} \\
 & = 0.806 < 1.000 \rightarrow \text{O.K.}
 \end{aligned}$$

(). Check interaction ratio of bending and axial force member.

[Eurocode3:05 6.2.9 (6.31 ~ 6.41)] - Class1 or Class2

- $n = N_{Ed} / N_{pl,Rd} = 0.030$
- $\alpha = \min[1.66/(1-1.13 \cdot n^2), 6.0] = 1.662$
- $\beta = \min[1.66/(1-1.13 \cdot n^2), 6.0] = 1.662$
- $N_{Ed} < 0.25 \cdot N_{pl,Rd} = \mathbf{749.94 \text{ kN.}}$
- $N_{Ed} < 0.5 \cdot h_w \cdot t_w \cdot f_y / \gamma_{M0} = 477.12 \text{ kN.}$
Therefore, No allowance for the effect of axial force.
- $M_{ny,Rd} = M_{ply,Rd} = 179275.00 \text{ kN-mm.}$
- $R_{maxy} = M_{Edy} / M_{ny,Rd} = 0.776 < 1.000 \rightarrow \text{O.K.}$
- $N_{Ed} < h_w \cdot t_w \cdot f_y / \gamma_{M0} = \mathbf{954.24 \text{ kN.}}$
Therefore, No allowance for the effect of axial force.
- $M_{nz,Rd} = M_{plz,Rd} = 105435.00 \text{ kN-mm.}$
- $R_{maxz} = M_{Edz} / M_{nz,Rd} = 0.000 < 1.000 \rightarrow \text{O.K.}$
- $R_{max2} = \max[R_{maxy}, R_{maxz}] = 0.776 < 1.000 \rightarrow \text{O.K.}$

(). Calculate buckling resistance of compression member (Nb_Rdy, Nb_Rdz). [Eurocode3:05 6.3.1.1, 6.3.1.2]

- $\beta_A = A_{eff} / A_{area} = 1.000$
- $\lambda_1 = \pi \cdot \sqrt{E_s / f_y} = 76.409$
- $\lambda_{by} = \{(K_L y / i_y) / \lambda_1\} \cdot \sqrt{\beta_A} = 1.404$
- $N_{cry} = \pi^2 \cdot E_s \cdot I_{yy} / K_L y^2 = \mathbf{1522.48 \text{ kN.}}$
- $\lambda_{by} > 0.2$ and $N_{Ed} / N_{cry} > 0.04$
--> Need to check.
- $\alpha_{ph} = 0.210$
- $\phi_{iy} = 0.5 \cdot [1 + \alpha_{ph} \cdot (\lambda_{by} - 0.2) + \lambda_{by}^2] = \mathbf{1.613}$
- $\chi_{iy} = \min[1 / [\phi_{iy} + \sqrt{\phi_{iy}^2 - \lambda_{by}^2}], 1.0] = \mathbf{0.416}$
- $N_{b,Rdy} = \chi_{iy} \cdot \beta_A \cdot A_{area} \cdot f_y / \gamma_{M1} = \mathbf{1247.29 \text{ kN.}}$
- $\lambda_{bz} = \{(K_L z / i_z) / \lambda_1\} \cdot \sqrt{\beta_A} = 0.842$
- $N_{crz} = \pi^2 \cdot E_s \cdot I_{zz} / K_L z^2 = 4227.99 \text{ kN.}$
- $\lambda_{bz} < 0.2$ or $N_{Ed} / N_{crz} < 0.04$
--> No need to check.

due to the effect of axial force is required when both of the following criteria are satisfied:

$$\begin{aligned}
 N_{ED} & \leq 0.25 N_{p1,Rd} \\
 N_{ED} & \leq \frac{0.5 h_w t_w f_y}{\gamma_{M0}}
 \end{aligned}$$

$$0.25 N_{p1,Rd} = 0.25 \times 2946.5 = \mathbf{736.64 \text{ KN}}$$

736.64 KN > 90KN \therefore equation (6.33) is satisfied

$$\frac{0.5 h_w t_w f_y}{\gamma_{M0}} = \frac{0.5 \times 168.0 \times (2 \times 16.0) \times 355}{\gamma_{M0}} = \mathbf{954.2 \text{ KN}}$$

954.2 KN > 90KN \therefore equation (6.34) is satisfied

Therefore, no allowance for the effect of axial force on the major axis plastic moment resistance of the cross-section need be made.

6.Member buckling resistance in compression (clause 6.3.1)

$$N_{b,Rd} = \frac{\chi A f_y}{\gamma_{M1}} \quad \text{for Class 1,2 or 3 cross-sections}$$

$$\chi = \frac{1}{\phi + \sqrt{\phi^2 - \lambda^2}} \quad \text{but } \chi \leq 1.0$$

where

$$\Phi = 0.5[1 + \alpha(\lambda - 0.2) + \lambda^2]$$

and

$$\lambda = \sqrt{\frac{A f_y}{N_{cr}}} \quad \text{for Class 1,2 or 3 cross-sections}$$

Elastic critical force and non-dimensional slenderness for flexural buckling

For buckling about the major (y-y) axis, L_{cr} should be taken as the full length of the beam(AD), which is 7.2 m. For buckling about the minor (z-z)axis, L_{cr} should be taken as the maximum length between points of lateral restraint, which is 2.4 m. Thus,

$$N_{cr,y} = \frac{\pi^2 E I}{L_{cr}^2} = \frac{\pi^2 \times 210000 \times 36780000}{7200^2} = 1470 \times 10^3 = \mathbf{1470 \text{ KN}}$$

$$\therefore \lambda = \sqrt{\frac{8300 \times 355}{1470 \times 10^3}} = 1.42$$

$$N_{cr,z} = \frac{\pi^2 E I}{L_{cr}^2} = \frac{\pi^2 \times 210000 \times 11470000}{2400^2} = 4127 \times 10^3 = \mathbf{4127 \text{ KN}}$$

$$\therefore \lambda = \sqrt{\frac{8300 \times 355}{4127 \times 10^3}} = 0.84$$

Selection of buckling curve and imperfection factor α

For a hot-rolled RHS, use buckling curve a (Table 6.5 (Table 6.2 of EN 1993-1-1)).

For curve buckling curve a, $\alpha = 0.21$ (Table 6.4 (Table 6.1

(). Calculate equivalent uniform moment factors (C_{my}, C_{mz}, C_{mLT}). [Eurocode3:05 Annex A. Table A.1, A.2]

- $C_{my,0} = 0.989$
- $C_{mz,0} = 1.005$
- C_{my} (Default or User Defined Value) = 1.000
- C_{mz} (Default or User Defined Value) = 1.000
- C_{mLT} (Default or User Defined Value) = 1.000

(). Check interaction ratio of bending and axial compression member. [Eurocode3:05 6.3.1, 6.2.9.3 (6.61, 6.62), Annex A]

- $k_{yy} = 1.046$
- $k_{yz} = 0.609$
- $k_{zy} = 0.681$
- $k_{zz} = 1.035$
- $\chi_{iy} = 0.416$
- $\chi_{iz} = 0.771$
- $\chi_{iLT} = 1.000$
- $N_{Rk} = A \cdot f_y = 2999.75 \text{ kN}$.
- $M_{y,Rk} = W_{ply} \cdot f_y = 179.28 \text{ kN-m}$.
- $M_{z,Rk} = W_{plz} \cdot f_y = 105.44 \text{ kN-m}$.
- $N_{Ed} \cdot e_{Ny} = 0.0$ (Not Slender)
- $N_{Ed} \cdot e_{Nz} = 0.0$ (Not Slender)

$$- R_{max_LT1} = \frac{N_{Ed}}{\chi_{iy} \cdot N_{Rk} / \gamma_{M1} + M_{Edy} + N_{Ed} \cdot e_{Ny}}$$

of EN 1993-1-1))

Buckling curves : major (y-y) axis

$$\phi_y = 0.5 \times [1 + 0.21 \times (1.42 - 0.2) + 1.42^2] = 1.63$$

$$\therefore \chi_y = \frac{1}{1.63 + \sqrt{1.63^2 - 1.42^2}} = 0.41$$

$$N_{b,y,Rd} = \frac{0.41 \times 8300 \times 355}{1.0} = 1209 \times 10^3 = 1209 \text{ KN}$$

$$1209 \text{ KN} > 90 \text{ KN}$$

\therefore major axis flexural buckling resistance is acceptable

Buckling curve: minor (z-z) axis

$$\phi_z = 0.5 \times [1 + 0.21 \times (0.84 - 0.2) + 0.84^2] = 0.92$$

$$\therefore \chi_z = \frac{1}{0.92 + \sqrt{0.92^2 - 0.84^2}} = 0.77$$

$$N_{b,z,Rd} = \frac{0.77 \times 8300 \times 355}{1.0} = 2266 \times 10^3 = 2266 \text{ KN}$$

$$2266 \text{ KN} > 90 \text{ KN}$$

\therefore minor axis flexural buckling resistance is acceptable

7.Member buckling resistance in combined bending and axial compression (clause 6.3.3)

Non-dimensional slenderness

From the flexural buckling check:

$$\lambda_y = 1.42 \text{ and } \lambda_z = 0.84 \therefore \lambda_{max} = 1.42$$

From the lateral torsional buckling check:

$$\lambda_{LT} = 0.23 \text{ and } \lambda_0 = 0.23$$

Equivalent uniform moment factors C_{mi}

$$C_{my,0} = 0.79 + 0.21 \psi_y + 0.36(\psi_y - 0.33) \frac{N_{ED}}{N_{cr,y}} = 0.79 + (0.21 \times 1.0) + 0.36 \times (1.0 - 0.33) \frac{90}{1470} = 1.01$$

$C_{mz,0} = C_{mz}$ need not be considered since $M_{z,ED} = 0$.

$$\epsilon_y = \frac{M_{y,ED}}{N_{ED}} \frac{A}{W_{el,y}} \text{ for class 1,2 and 3 cross-sections} = \frac{139.2 \times 10^6}{90 \times 10^3} \frac{8300}{368000} = 34.9$$

$$\alpha_{LT} = 1 - \frac{I_T}{I_y} \geq 1.0 = 1 - \frac{29820000}{36780000} = 0.189$$

$$C_{my} = C_{mz,0} + (1 - C_{my,0}) \frac{\sqrt{\epsilon_y} \alpha_{LT}}{1 + \sqrt{\epsilon_y} \alpha_{LT}} = 1.01 + (1 - 1.01) \frac{\sqrt{34.9} \times 0.189}{1 + (\sqrt{34.9} \times 0.189)} = 1.01$$

$$C_{mLT} = C_{my}^2 \frac{\alpha_{LT}}{\sqrt{[1 - (N_{Ed}/N_{cr,z})][1 - (N_{Ed}/N_{cr,T})]}} = 1.01^2 \frac{0.189}{\sqrt{[1 - (904127)]}[1 - (90415502)]}} \geq 1.0 \text{ (but } \geq 1.0) \therefore C_{mLT} = 1.00$$

Interaction factors k_{ij}

$$k_{yy} = C_{my} C_{mLT} \frac{\mu_y}{1 - N_{ED}/N_{cr,y}} \frac{1}{C_{yy}} = 1.01 \times 1.00 \times \frac{0.96}{1 - 90/1470} \times \frac{1}{0.98} = 1.06$$

$$\begin{aligned}
 &+ k_{yy} * \frac{X_{LT} * M_{y,Rk} / \Gamma_{M1}}{M_{Edz} + N_{Ed} * e_{Nz}} \\
 &+ k_{yz} * \frac{M_{z,Rk} / \Gamma_{M1}}{M_{Edz} + N_{Ed} * e_{Nz}} \\
 &= 0.885 < 1.000 \rightarrow \text{O.K.} \\
 \\
 &- \text{. Rmax_LT2} = \frac{N_{Ed}}{X_{yz} * N_{Rk} / \Gamma_{M1} + M_{Edy} + N_{Ed} * e_{Ny}} \\
 &+ k_{zy} * \frac{X_{LT} * M_{y,Rk} / \Gamma_{M1}}{M_{Edz} + N_{Ed} * e_{Nz}} \\
 &+ k_{zz} * \frac{M_{z,Rk} / \Gamma_{M1}}{M_{Edz} + N_{Ed} * e_{Nz}} \\
 &= 0.568 < 1.000 \rightarrow \text{O.K.} \\
 \\
 &- \text{. Rmax} = \text{MAX} [\text{MAX}(\text{Rmax1}, \text{Rmax2}), \\
 &\quad \text{MAX}(\text{Rmax_LT1}, \text{Rmax_LT2})] \\
 &= 0.885 < 1.000 \rightarrow \text{O.K.}
 \end{aligned}$$

$$\begin{aligned}
 k_{zy} &= C_{my} C_{mLT} \frac{\mu_y}{1 - N_{ED} / N_{cr,y}} \frac{1}{C_{zy}} 0.6 \sqrt{\frac{W_y}{W_z}} \\
 &= 1.01 \times 1.00 \times \frac{0.99}{1 - 90/1470} \times \frac{1}{0.95} \times 0.6 \times \\
 &\quad \sqrt{\frac{1.33}{1.27}} = \mathbf{0.69}
 \end{aligned}$$

Check compliance with interaction formulae (equations (6.61) and (6.62))

$$\begin{aligned}
 &\frac{N_{ED}}{X_y N_{RK} / \gamma_{M1}} + k_{yy} \frac{M_{y,ED}}{X_{LT} M_{y,RK} / \gamma_{M1}} + k_{zy} \frac{M_{z,Ed}}{M_{z,RK} / \gamma_{M1}} \leq 1 \\
 &\Rightarrow \frac{90}{(0.41 \times 2947)/1.0} + 1.06 \times \frac{139.2}{(0.97 \times 174.3)/1.0} \\
 &= 0.07 + 0.87 = 0.94
 \end{aligned}$$

$0.94 \leq 1.0$ \therefore equations (6.61) is satisfied

$$\begin{aligned}
 &\frac{N_{ED}}{X_z N_{RK} / \gamma_{M1}} + k_{zy} \frac{M_{y,ED}}{X_{LT} M_{y,RK} / \gamma_{M1}} + k_{zz} \frac{M_{z,Ed}}{M_{z,RK} / \gamma_{M1}} \leq 1 \\
 &\Rightarrow \frac{90}{(0.77 \times 2947)/1.0} + 0.69 \times \frac{139.2}{(0.97 \times 174.3)/1.0} \\
 &= 0.04 + 0.57 = 0.61
 \end{aligned}$$

$0.61 \leq 1.0$ \therefore equations (6.62) is satisfied

Therefore, a hot-rolled 200 × 100 × 16 RHS in grade S355 steel is suitable for this application.

[Reference]

L.Gardner and D.A.Nethercot, Designers' Guide to EN 1993-1-1, The Steel Construction Institute, Thomas Telford, 81-89 (Example 6.9)

3.6 Member resistance under combined bi-axial bending and axial compression

An H section member of length 4.2 m is to be designed as a ground floor column in a multi-storey building. The frame is moment resisting in-plane and pinned out-of-plane, with diagonal bracing provided in both directions. The column is subjected to major axis bending due to horizontal forces and minor axis bending due to eccentric loading from the floor beams. From the structural analysis, the design action effects of Fig.6.29 arise in the column.

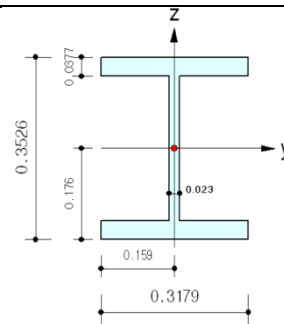
Assess the suitability of a hot-rolled 305 X 305 X 240H section in grade S275 steel for this application.

3.6.1 Material Properties

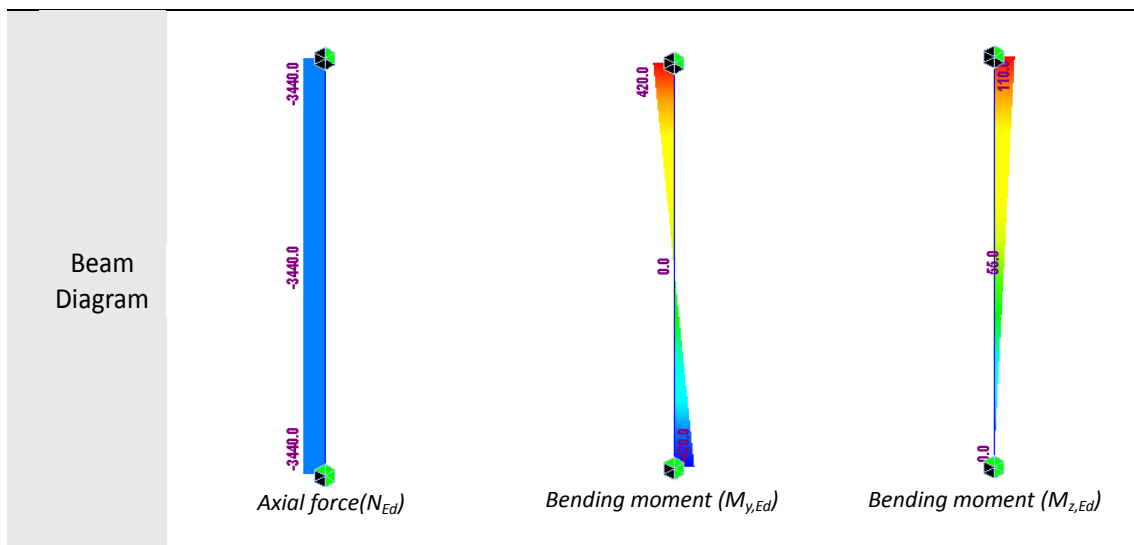
Material	S275	$f_y = 275 \text{ N/mm}^2$	$E_s = 210 \text{ GPa}$
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3.6.2 Section Properties

Section Name	305 X 305 X 240H
Depth (H)	352.5 mm
Width (B)	318.4 mm
Flange Thickness (T_f)	37.70 mm
Web Thickness (T_w)	23.0 mm
Gross sectional area (A)	30600.0 mm ²
Shear area (A_{sz})	8033.0 mm ²



3.6.3 Analysis Model



3.6.4 Comparison of Design Results

	midas Gen	Example book	Error (%)
Axial resistance	8415.00kN	8415.00kN	0.00%
Shear resistance	1168.75 kNm	1168.00kNm	0.06%
Bending resistance	1366.36kN	1275.00kN	6.69%
Reduced plastic moment resistance	770.79kNm	773.80kNm	0.39%

3.6.5 Detailed comparison

midas Gen	Example book
<p>1. Cross-section classification</p> <p>(). Determine classification of compression outstand flanges.</p> <p>[Eurocode3:05 Table 5.2 (Sheet 2 of 3), EN 1993-1-5]</p> <ul style="list-style-type: none"> - $e = \text{SQRT}(235/f_y) = 0.92$ - $b/t = \text{BTR} = 3.51$ - $\sigma_1 = 213390.031 \text{ KPa}$. - $\sigma_2 = 141865.416 \text{ KPa}$. - $\text{BTR} < 9 \cdot e$ (Class 1 : Plastic). <p>(). Determine classification of compression Internal Parts.</p> <p>[Eurocode3:05 Table 5.2 (Sheet 1 of 3), EN 1993-1-5]</p> <ul style="list-style-type: none"> - $e = \text{SQRT}(235/f_y) = 0.92$ - $d/t = \text{HTR} = 10.73$ - $\sigma_1 = 201819.634 \text{ KPa}$. - $\sigma_2 = 23016.967 \text{ KPa}$. - $\text{HTR} < 33 \cdot e$ (Class 1 : Plastic). <p>2. Check Axial Resistance.</p> <p>(). Check slenderness ratio of axial compression member (Kl/i). [Eurocode3:05 6.3.1]</p> <ul style="list-style-type: none"> - $Kl/i = 51.6 < 200.0 \rightarrow \text{O.K.}$ <p>(). Calculate axial compressive resistance (Nc_Rd).</p> <p>[Eurocode3:05 6.1, 6.2.4]</p> <ul style="list-style-type: none"> - $N_{c_Rd} = f_y \cdot \text{Area} / \gamma_{M0} = \mathbf{8415.00 \text{ kN}}$. <p>(). Check ratio of axial resistance (N_Ed/Nc_Rd).</p> <p>$N_{Ed} = 3440.00$</p> <ul style="list-style-type: none"> - $\frac{N_{Ed}}{N_{c_Rd}} = \frac{3440.00}{8415.00} = 0.518 < 1.000 \rightarrow \text{O.K.}$ <p>3. Check Bending Moment Resistance About Major Axis</p> <p>(). Calculate plastic resistance moment about major axis.</p> <p>[Eurocode3:05 6.1, 6.2.5]</p>	<p>Cross-section classification (clause 5.5.2)</p> <p>$\epsilon = \sqrt{235/f_y} = \sqrt{235/275} = 0.92$</p> <p>Outstand flanges (Table 5.2, sheet 2):</p> <p>$C = (b - t_w - 2r)/2 = 132.5 \text{ mm}$</p> <p>$c/t_f = 132.5/37.7 = 3.51$</p> <p>Limit for Class 1 flange $= 9\epsilon = 8.32$</p> <p>$8.32 > 3.51 \quad \therefore \text{flange is Class 1}$</p> <p>Web – internal part in bending (Table 5.2, sheet 1):</p> <p>$C = h - 2t_f - 2r = 246.7 \text{ mm}$</p> <p>$c/t_w = 246.7/23.0 = 10.73$</p> <p>Limit for Class 1 web $= 33\epsilon = 30.51$</p> <p>$30.51 > 10.73 \quad \therefore \text{web is Class 1}$</p> <p>The overall cross-section classification is therefore Class 1.</p> <p>Compression resistance of cross-section (clause 6.2.4)</p> <p>The design compression resistance of the cross-section</p> <p>$N_{c_Rd} = \frac{A f_y}{\gamma_{M0}} \quad \text{for class 1,2 and 3 cross-sections}$</p> <p>$= \frac{30600 \times 275}{1.00} = 8415000 \text{ N} = \mathbf{8415 \text{ KN}}$</p> <p>$8415 \text{ KN} > 34400 \text{ KN} \quad \therefore \text{acceptable}$</p> <p>Bending resistance of cross-section (clause 6.2.5)</p> <p>major (y-y) axis</p> <p>Maximum bending moment</p> <p>$M_{y_Ed} = 420.0 \text{ KN}$</p> <p>The design major axis bending resistance of the cross-section.</p>

- Wply = 0.0043 m³.
- Mc_Rdy = Wply * fy / Gamma_M0 = **1168.75 kN-m**.

(). Check ratio of moment resistance (M_Edy/Mc_Rdy).

$$\frac{M_{Edy}}{Mc_{Rdy}} = \frac{420.00}{1168.75} = 0.359 < 1.000 \rightarrow \text{O.K.}$$

(). Calculate plastic resistance moment about minor axis.

- [Eurocode3:05 6.1, 6.2.5]
- Wplz = 0.0020 m³m³.
- Mc_Rdz = Wplz * fy / Gamma_M0 = **536.25kN-m**.

(). Check ratio of moment resistance (M_Edz/Mc_Rdz).

$$\frac{M_{Edz}}{Mc_{Rdz}} = \frac{110.00}{536.25} = 0.205 < 1.000 \rightarrow \text{O.K.}$$

3. Shear resistance of cross-section

(). Calculate shear area.

- [Eurocode3:05 6.2.6, EN1993-1-5:04 5.1 NOTE 2]
- eta = 1.2 (Fy < 460 MPa.)
- r = 0.0152 m.
- Avy = Area - hw*tw = 0.0242 m².
- Avz1 = eta*hw*tw = 0.0076 m².
- Avz2 = Area - 2*B*tf + (tw + 2*r)*tf = 0.0086 m².
- Avz = MAX[Avz1, Avz2] = 0.0086 m².

(). Calculate plastic shear resistance in local-z direction (Vpl_Rdz). [Eurocode3:05 6.1, 6.2.6]

$$V_{pl,Rdz} = [Avz * fy / \sqrt{3}] / \Gamma_{M0} = \mathbf{1366.36kN}.$$

(). Check ratio of shear resistance (V_Edz/Vpl_Rdz).

(LCB = 1, POS = J)

$$\frac{V_{Edz}}{V_{pl,Rdz}} = \frac{200.00}{1366.36} = 0.146 < 1.000 \rightarrow \text{O.K.}$$

(). Calculate plastic shear resistance in local-y direction (Vpl_Rdy). [Eurocode3:05 6.1, 6.2.6]

$$V_{pl,Rdy} = [Avy * fy / \sqrt{3}] / \Gamma_{M0} = \mathbf{3846.51 kN}.$$

(). Check ratio of shear resistance (V_Edy/Vpl_Rdy).

(LCB = 1, POS = J)

$$\frac{V_{Edy}}{V_{pl,Rdy}} = \frac{26.19}{3846.51} = 0.007 < 1.000 \rightarrow \text{O.K.}$$

(). Shear Buckling Check. [Eurocode3:05 6.2.6]

- HTR < 72*e/Eta → **No need to check!**

$$M_{c,y,Rd} = \frac{W_{pl,y} f_y}{\gamma_{M0}} \quad \text{for Class 1 or 2 cross-sections}$$

$$= \frac{4247000 \times 275}{1.00} = 1168 \times 10^6 \text{ Nmm}$$

$$= \mathbf{1168 \text{ KNm}}$$

$$1168 \text{ KNm} > 420.0 \text{ KNm} \quad \therefore \text{acceptable}$$

minor (z-z) axis

Maximum bending moment

$$M_{y,Ed} = 110.0 \text{ KN}$$

The design minor axis bending resistance of the cross-section

$$M_{c,z,Rd} = \frac{W_{pl,z} f_y}{\gamma_{M0}} = \frac{1915000 \times 275}{1.00} = 536.5 \times 10^6 \text{ Nmm}$$

$$= \mathbf{536.5 \text{ KNm}}$$

$$536.5 \text{ KNm} > 110.0 \text{ KNm} \quad \therefore \text{acceptable}$$

Shear resistance of cross-section (clause 6.2.6)

The design plastic shear resistance of the cross-section

$$V_{p1,Rd} = \frac{A_v (f_y / 3)}{\gamma_{M0}}$$

Load parallel to web

Maximum shear force

$$V_{ED} = 840/4.2 = 200.0 \text{ KN}$$

For a rolled H section, loaded parallel to the web, the shear area A_v is given by

$$A_v = A - 2bt_f + (t_w + r) t_f \quad (\text{but not less than } \eta h_w t_w)$$

$\eta = 1.2$ (from Eurocode 3 –part 1.5, though the UK National Annex may specify an alternative value).

$$h_w = (h - 2t_f) = 352.5 - (2 \times 37.7) = 277.1 \text{ mm}$$

$$\therefore A_v = 30600 - (2 \times 318.4 \times 37.7) + (23.0 + 15.2) \times 37.7$$

$$= 8033 \text{ mm}^2$$

$$(\text{but not less than } 1.2 \times 277.1 \times 23.0 = 7648 \text{ mm}^2)$$

$$V_{p1,Rd} = \frac{8033 \times (275/3)}{1.00} = 1275000 \text{ N} = \mathbf{1275KN}$$

$$1275 \text{ KN} > 200 \text{ KN} \quad \therefore \text{acceptable}$$

Load parallel to flanges

Maximum shear force

$$V_{ED} = 110/3.7 = 26.2 \text{ KN}$$

No guidance on the determination of the shear area for a rolled I or H section loaded parallel to the flanges is presented in EN 1993-1-1, though it may be assumed that adopting the recommendations provided for a welded I or H section would be acceptable.

The shear area A_v is therefore taken as

$$A_w = A - \sum (h_w t_w) = 30600 - (277.1 \times 23.0)$$

$$= 24227 \text{ mm}^2$$

$$V_{p1,Rd} = \frac{24227 \times (275/3)}{1.00} = 3847000 \text{ N} = \mathbf{3847KN}$$

$$3847 \text{ KN} > 26.2 \text{ KN} \quad \therefore \text{acceptable}$$

Shear buckling

Shear buckling need not be considered, provided

Note.

When calculating shear area for H sections, following equation was applied as per EN1993-1-1:2005, sub clause 6.2.6(3) a).

$$A_v = A - 2bt_f + (t_w + 2r)t_f$$

However, in the example book, following equation was applied.

$$A_v = A - 2bt_f + (t_w + r)t_f$$

For this reason, the difference in shear resistance occurred.

5. Check Interaction of Combined Resistance**(). Check interaction ratio of bending and axial force member.**

[Eurocode3:05 6.2.9 (6.31 ~ 6.41)] - Class1 or Class2

$$n = N_{Ed} / N_{pl,Rd} = 0.410$$

$$a = \min[(Area - 2bt_f) / Area, 0.5] = 0.214$$

$$\alpha = 2.000$$

$$\beta = \max[5n, 1.0] = 2.051$$

$$N_{Ed} > 0.25 N_{pl,Rd} = 1653.88 \text{ kN.}$$

$$N_{Ed} > 0.5 h_w t_w f_y / \gamma_{M0} = 876.64 \text{ kN.}$$

Therefore, Allowance for the effect of axial force.

$$M_{ny,Rd} = \min[M_{ply,Rd} (1-n) / (1-0.5a), M_{ply,Rd}] = 770.79 \text{ kN-m.}$$

$$R_{maxy} = M_{Edy} / M_{ny,Rd} = 0.545 < 1.000 \rightarrow \text{O.K.}$$

$$N_{Ed} > h_w t_w f_y / \gamma_{M0} = 2873.87 \text{ kN.}$$

Therefore, Allowance for the effect of axial force.

- In case of $n > a$

$$M_{nz,Rd} = M_{plz,Rd} * [1 - ((n-a)/(1-a))^2] = 501.60 \text{ kN-m.}$$

$$R_{maxz} = M_{Edz} / M_{nz,Rd} = 0.219 < 1.000 \rightarrow \text{O.K.}$$

$$R_{max2} = \left[\frac{|M_{Edy}|^\alpha}{M_{ny,Rd}^\alpha} + \frac{|M_{Edz}|^\beta}{M_{nz,Rd}^\beta} \right]^{1/(\alpha+\beta)} = 0.341 < 1.000 \rightarrow \text{O.K.}$$

(). Calculate buckling resistance of compression member

(Nb_Rdy, Nb_Rdz). [Eurocode3:05 6.3.1.1, 6.3.1.2]

$$\beta_A = A_{eff} / Area = 1.000$$

$$\lambda_{b1} = \pi \sqrt{E_s / f_y} = 86.815$$

$$\lambda_{by} = \{ (KLy / i_y) / \lambda_{b1} \} \sqrt{\beta_A} = 0.234$$

$$N_{cry} = \pi^2 E_s R_{yy} / KLy^2 = 153942.81 \text{ kN.}$$

$$\lambda_{by} < 0.2 \text{ or } N_{Ed} / N_{cry} < 0.04 \rightarrow \text{No need to check.}$$

$$\lambda_{bz} = \{ (KLz / i_z) / \lambda_{b1} \} \sqrt{\beta_A} = 0.594$$

$$N_{crz} = \pi^2 E_s R_{zz} / KLz^2 = 23851.54 \text{ kN.}$$

$$\lambda_{bz} > 0.2 \text{ and } N_{Ed} / N_{crz} > 0.04 \rightarrow \text{Need to check.}$$

$$\alpha_{phaz} = 0.490$$

$$\frac{h_w}{t_w} \leq 72 \frac{\epsilon}{\eta} \text{ for unstiffened webs}$$

$\eta = 1.2$ (from Eurocode 3 –part 1.5, though the UK National Annex may specify an alternative value).

$$72 \frac{\epsilon}{\eta} = 72 \times \frac{0.92}{1.2} = 55.5$$

$$\text{Actual } h_w / t_w = 277.1 / 23.0 = 12.0$$

$$12.0 \leq 55.5 \therefore \text{no shear buckling check required}$$

Cross-section resistance under Bending, Shear and axial force (clause 6.2.10)

Reduced plastic moment resistances (clause 6.2.9.1(5))

major (y-y) axis:

$$M_{N,y,Rd} = M_{pl,y,Rd} \frac{1-n}{1-0.5a} \quad (\text{but } M_{N,y,Rd} \leq M_{pl,y,Rd})$$

Where

$$n = N_{Ed} / N_{pl,y,Rd} = 34400 / 8415 = 0.41$$

$$a = (A - 2bt_f) / A = [30600 - (2 \times 318.4 \times 37.7)] / 30600 = 0.22$$

$$\Rightarrow M_{N,y,Rd} = 1168 \times \frac{1-0.41}{1-(0.5 \times 0.22)} = 773.8 \text{ kNm}$$

$$773.8 \text{ kNm} > 720 \text{ kNm} \therefore \text{acceptable}$$

minor (z-z) axis

$$\text{For } n > a \quad M_{N,z,Rd} = M_{pl,z,Rd} \left[1 - \left(\frac{n-a}{1-a} \right)^2 \right]$$

$$\Rightarrow M_{N,z,Rd} = 536.5 \times \left[1 - \left(\frac{0.41-0.22}{1-0.22} \right)^2 \right] = 503.9 \text{ kNm}$$

$$503.9 \text{ kNm} > 110 \text{ kNm} \therefore \text{acceptable}$$

Cross-section check for bi-axial bending (with reduced moment resistance)

$$\left(\frac{M_{y,Ed}}{M_{N,y,Rd}} \right)^\alpha + \left(\frac{M_{z,Ed}}{M_{N,z,Rd}} \right)^\beta \leq 1$$

For I and H sections:

$$\alpha = 2 \text{ and } \beta = 5n \text{ (but } \beta \geq 1) = (5 \times 0.41) = 2.04$$

$$\Rightarrow \left(\frac{420}{773.8} \right)^2 + \left(\frac{110}{536.5} \right)^{2.04} = 0.33$$

$$0.33 \leq 1 \therefore \text{acceptable}$$

Member buckling resistance in compression (clause 6.3.1)

$$N_{b,Rd} = \frac{\chi A f_y}{\gamma_{M1}} \quad \text{for Class 1,2 or 3 cross-sections}$$

$$\chi = \frac{1}{\phi + \sqrt{\phi^2 - \lambda^2}} \quad \text{but } \chi \leq 1.0$$

$$\text{where, } \phi = 0.5 [1 + \alpha (\lambda - 0.2) + \lambda^2]$$

$$\text{and } \lambda = \sqrt{\frac{A f_y}{N_{cr}}} \quad \text{for Class 1,2 or 3 cross-sections}$$

Elastic critical force and non-dimensional slenderness for flexural buckling

For buckling about the major (y-y) axis:

$$L_{cr} = 0.7L = 0.7 \times 4.2 = 2.94 \text{ m} \quad (\text{see Table 6.6})$$

For buckling about the minor (z-z) axis:

$$\begin{aligned} - \text{Phiz} &= 0.5 * [1 + \text{Alphaz} * (\text{Lambda_bz} - 0.2) + \text{Lambda_bz}^2] \\ &= 0.773 \\ - \text{Xiz} &= \text{MIN} [1 / [\text{Phiz} + \text{SQRT}(\text{Phiz}^2 - \text{Lambda_bz}^2)], 1.0] \\ &= 0.789 \\ - \text{Nb_Rdz} &= \text{Xiz} * \text{Beta_A} * \text{Area} * f_y / \text{Gamma_M1} = 6640.85 \text{ kN.} \end{aligned}$$

(). Check ratio of buckling resistance ($N_{Ed}/N_{b,Rd}$).

$$\begin{aligned} - \text{Nb_Rd} &= \text{MIN} [\text{Nb_Rdy}, \text{Nb_Rdz}] = \mathbf{6640.85 \text{ kN.}} \\ \text{N_Ed} &3440.00 \\ - \frac{\text{N_Ed}}{\text{Nb_Rd}} &= \frac{3440.00}{6640.85} = 0.518 < 1.000 \rightarrow \text{O.K.} \end{aligned}$$

$$\begin{aligned} L_{cr} &= 1.0L = 1.0 \times 4.2 = 4.20 \text{ m} \quad (\text{see Table 6.6}) \\ N_{cr,y} &= \frac{\pi^2 EI_y}{L_{cr}^2} = \frac{\pi^2 \times 210000 \times 642.0 \times 10^6}{2940^2} = 153943 \times 10^3 \text{ N} \\ &= \mathbf{153943 \text{ KN}} \end{aligned}$$

$$\therefore \lambda = \sqrt{\frac{30600 \times 275}{153943 \times 10^3}} = 0.23$$

$$\begin{aligned} N_{cr,z} &= \frac{\pi^2 EI_y}{L_{cr}^2} = \frac{\pi^2 \times 210000 \times 203.1 \times 10^6}{4200^2} = 23863 \times 10^3 \text{ N} \\ &= \mathbf{23863 \text{ KN}} \end{aligned}$$

$$\therefore \lambda = \sqrt{\frac{30600 \times 275}{23863 \times 10^3}} = 0.59$$

Buckling curves : major (y-y) axis

$$\phi_y = 0.5 \times [1 + 0.34 \times (0.23 - 0.2) + 0.23^2] = 0.53$$

$$\therefore \chi_y = \frac{1}{0.53 + \sqrt{0.53^2 - 0.23^2}} = 0.99$$

$$N_{b,y,Rd} = \frac{0.99 \times 30600 \times 275}{1.0} = 8314 \times 10^3 = 8314 \text{ KN}$$

$$8314 \text{ KN} > 3440 \text{ KN}$$

\therefore major axis flexural buckling resistance is acceptable

Buckling curve: minor (z-z) axis

$$\phi_z = 0.5 \times [1 + 0.49 \times (0.59 - 0.2) + 0.59^2] = 0.77$$

$$\therefore \chi_y = \frac{1}{0.77 + \sqrt{0.77^2 - 0.59^2}} = 0.79$$

$$N_{b,y,Rd} = \frac{0.79 \times 30600 \times 275}{1.0} = 6640 \times 10^3 = \mathbf{6640 \text{ KN}}$$

6640 KN > 3440 KN \therefore minor axis flexural buckling resistance is acceptable

[Reference]

L.Gardner and D.A.Nethercot, Designers' Guide to EN 1993-1-1, The Steel Construction Institute, Thomas Telford, 89-97 (Example 6.10)

3.7 I-section beam design under shear force and bending moment

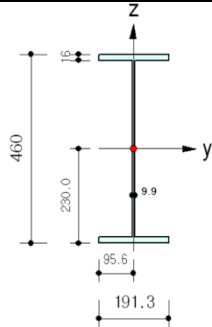
The 457 X 191 UB 82 compression member of S275 steel of Figure 3.28a is simply supported about both principle axes at each end ($L_{cr,y} = 12.0$ m), and has a central brace which prevents lateral deflections in the minor principle plane ($L_{cr,z} = 6.0$ m). Check the adequacy of the member for a factored axial compressive load corresponding to a nominal dead of 160 kN and a nominal imposed load of 230 kN.

3.7.1 Material Properties

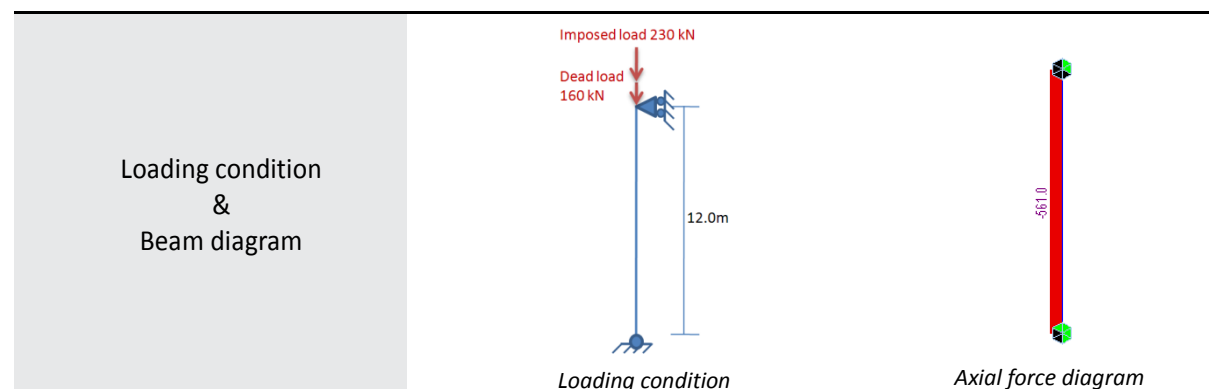
Material	S275	$f_y = 275 \text{ N/mm}^2$	$E_s = 210 \text{ GPa}$
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3.7.2 Section Properties

Section Name	457 X 191 UB 82
Depth (H)	460.0 mm
Width (B)	191.3 mm
Flange Thickness (T_f)	16.0 mm
Web Thickness (T_w)	9.9 mm
Gross sectional area (A)	10 400.0 mm ²
Effective area (A_{eff})	10 067.0 mm ²



3.7.3 Analysis Model



3.7.4 Comparison of Design Results

	midas Gen	Example book	Error (%)
Compression resistance	2768.45 kN	2765.00 kN	0.12%
Buckling resistance	845.80 kNm	844.00 kNm	0.21%

3.7.5 Detailed comparison

midas Gen	Example book
<p>1. Cross-section classification</p> <p>(). Determine classification of compression outstand flanges.</p> <p>[Eurocode3:05 Table 5.2 (Sheet 2 of 3), EN 1993-1-5]</p> <ul style="list-style-type: none"> - $e = \text{SQRT}(235/f_y) = 0.92$ - $b/t = \text{BTR} = 5.03$ - $\sigma_1 = 0.054 \text{ kN/mm}^2$. - $\sigma_2 = 0.054 \text{ kN/mm}^2$. - $\text{BTR} < 9 \cdot e$ (Class 1 : Plastic).. <p>(). Determine classification of compression Internal Parts.</p> <p>[Eurocode3:05 Table 5.2 (Sheet 1 of 3), EN 1993-1-5]</p> <ul style="list-style-type: none"> - $e = \text{SQRT}(235/f_y) = 0.92$ - $d/t = \text{HTR} = 41.17$ - $\sigma_1 = 0.054 \text{ kN/mm}^2$. - $\sigma_2 = 0.054 \text{ kN/mm}^2$. - $\text{HTR} > 42 \cdot e$ (Class 4 : Slender). <p>2. CALCULATE EFFECTIVE AREA.</p> <p>(). Calculate effective cross-section properties of web of Class 4 (Internal element).</p> <p>[Eurocode3 Part 1-5 4.4, Table 4.1, 4.2]</p> <ul style="list-style-type: none"> - $\text{RatT} = 41.1717$ - $\text{Lambda}_p = \text{RatT} / [28.4 \cdot \epsilon \cdot \text{SQRT}(k \cdot \sigma_1)] = \mathbf{0.7841}$ - $\text{Rho} = \text{MIN}[(\text{Lambda}_p - 0.055 \cdot (3 + \psi)) / \text{Lambda}_p^2, 1.0] = \mathbf{0.9175}$ - $\sigma_{\text{max}} = \text{MAX}(\sigma_1, \sigma_2) = 0.054 \text{ kN/mm}^2$. - $\sigma_{\text{min}} = \text{MIN}(\sigma_1, \sigma_2) = 0.054 \text{ kN/mm}^2$. - $r = 10.200 \text{ mm}$. - $A_r = 10.300 \text{ mm}^2$. - $d_c = 407.600 \text{ mm}$. - $d_{\text{eff1}} = 2 \cdot (\text{Rho} \cdot d_c) / [5 - \sigma_{\text{min}} / \sigma_{\text{max}}] + r = 197.187 \text{ mm}$. - $A_{\text{eff1}} = d_{\text{eff1}} \cdot t_w + 2 \cdot A_r = 1972.747 \text{ mm}^2$. 	<p>Classifying the section.</p> <p>For S275 steel with $t_f = 16 \text{ mm}$, $f_y = 275 \text{ N/mm}^2$ (EN 10025-2)</p> $\epsilon = (235/275)^{0.5} = 0.924$ $c_f / (t_f \epsilon) = [(191.3 - 9.9 - 2 \times 10.2) / 2] / (16.0 \times 0.924) = 5.44 < 1.4$ $c_w = (460.0 - 2 \times 1630 - 2 \times 10.2) = 407.6 \text{ mm}$ $c_w / (t_w \epsilon) = 407.6 / (9.9 \times 0.924) = 44.5 > 42$ <p>and so th web is Class 4(slender)</p> <p>Effective area.</p> $\lambda_p = \frac{\sqrt{f_y}}{\sqrt{\sigma_{cr}}} = \frac{b/t}{28.4 \epsilon \sqrt{k_\sigma}} = \frac{407.6/9.9}{28.4 \times 0.924 \times \sqrt{4.0}} = \mathbf{0.784}$ <p>Ec3-1-5 4.4(2)</p> $\rho = \frac{\lambda_p - 0.0055(3 + \phi)}{\lambda_p^2} = \frac{0.784 - 0.0055(3 + 1)}{0.784^2} = \mathbf{0.98}$ <p>Ec3-1-5 4.4(2)</p> $d - d_{\text{eff}} = (1 - 0.918) \times 407.6 = 33.6 \text{ mm}$ $A_{\text{eff}} = 104 \times 10^2 - 33.6 \times 9.9 = \mathbf{10067 \text{ mm}^2}$

- . zeff1 = deff1/2 + tf = 114.593 mm.
- . deff2 = (Rho*dc) - deff1 + r = 197.187 mm.
- . Aeff2 = deff2 * tw + 2*Ar = 1972.747 mm².
- . zeff2 = (h+2*r) - deff2/2 + tf = 345.407 mm.

(). Calculated effective cross-section properties of Class4 cross-section.

- . Aeff = **10067.0930** mm².
(for calculating axial resistance)
- . Aeffy = 10400.0000 mm².
- . Weffy = 1593520.8649 mm³.
- . Aeffz = 10400.0000 mm².
- . Weffz = 195538.8255 mm³.
- . eNy = 0.0000 mm.
- . eNz = 2.8422e-014 mm.

2. CHECK AXIAL RESISTANCE.

(). Check slenderness ratio of axial compression member (Kl/i). [Eurocode3:05 6.3.1]

- . Kl/i = 141.8 < 200.0 ---> O.K.

(). Calculate axial compressive resistance (Nc_Rd).

[Eurocode3:05 6.1, 6.2.4]

- . Nc_Rd = fy * Aeff / Gamma_M0 = **2768.45 kN**.

(). Check ratio of axial resistance (N_Ed/Nc_Rd).

- . $\frac{N_{Ed}}{N_{c,Rd}} = \frac{561.00}{2768.45} = 0.203 < 1.000 \text{ ---> O.K.}$

(). Calculate buckling resistance of compression member (Nb_Rdy, Nb_Rdz). [Eurocode3:05 6.3.1.1, 6.3.1.2]

- . Beta_A = Aeff / Area = 0.968
- . Lambda1 = Pi * SQRT(Es/fy) = 86.815
- . Lambda_by = {(KLy/iy)/Lambda1} * SQRT(Beta_A) = **0.723**
- . Ncry = Pi^2*Es*Ryy / KLy^2 = 5339.87 kN.
- . Lambda_by > 0.2 and N_Ed/Ncry > 0.04
--> Need to check.
- . Alphay = 0.210
- . Phiy = 0.5 * [1 + Alphay*(Lambda_by-0.2) + Lambda_by^2] = 0.817
- . Xiy = MIN [1 / [Phiy + SQRT(Phiy^2 - Lambda_by^2)], 1.0] = 0.836
- . Nb_Rdy = Xiy*Beta_A*Area*fy / Gamma_M1 = 2315.78 kN.
- . Lambda_bz = {(KLz/iz)/Lambda1} * SQRT(Beta_A) = **1.608**
- . Ncrz = Pi^2*Es*Rzz / KLz^2 = 1076.61 kN.
- . Lambda_bz > 0.2 and N_Ed/Ncrz > 0.04
--> Need to check.
- . Alphaz = 0.340
- . Phiz = 0.5 * [1 + Alphaz*(Lambda_bz-0.2) + Lambda_bz^2] = **2.031**
- . Xiz = MIN [1 / [Phiz + SQRT(Phiz^2 - Lambda_bz^2)], 1.0] = **0.306**
- . Nb_Rdz = Xiz*Beta_A*Area*fy / Gamma_M1

Cross-section compression resistance.

$$N_{c,Rd} = \frac{A_{eff} f_y}{\gamma_{M0}} = \frac{10067 \times 275}{1.0} = \mathbf{2768 \text{ KN}} > 561 \text{ KN} = N_{Ed}$$

Member buckling resistance.

$$\lambda_y = \sqrt{\frac{A_{eff} f_y}{N_{cr,y}}} = \frac{L_{cr,y}}{i_y} \sqrt{\frac{A_{eff}}{A}} = \frac{12000}{(18.8 \times 10)} \sqrt{\frac{10067}{10400}} = \mathbf{0.724}$$

$$\lambda_z = \sqrt{\frac{A_{eff} f_y}{N_{cr,z}}} = \frac{L_{cr,z}}{i_z} \sqrt{\frac{A_{eff}}{A}} = \frac{6000}{(4.23 \times 10)} \sqrt{\frac{10067}{10400}} = \mathbf{1.608} > 0.724$$

Buckling will occur about the minor (z) axis. For a rolled UB section (with h/b > 1.2 and t_f ≤ 40 mm), buckling about the z-axis, use buckling curve (b) with α = 0.34

$$\Phi_z = 0.5 [1 + 0.34 (1.608 - 0.2) + 1.608^2] = \mathbf{2.032}$$

$$\chi_z = \frac{1}{2.032 + \sqrt{2.032^2 - 1.608^2}} = \mathbf{0.305}$$

$$N_{b,z,Rd} = \frac{\chi_{A_{eff}} f_y}{\gamma_{M1}} = \frac{0.305 \times 10067 \times 275}{1.0} = \mathbf{844 \text{ KN}} > 561 \text{ KN} = N_{Ed}$$

And so the member is satisfactory.

= 845.80 kN.

(). Check ratio of buckling resistance ($N_{Ed}/N_{b,Rd}$).

-. $N_{b,Rd} = \text{MIN}[N_{b,Rdy}, N_{b,Rdz}] = 845.80 \text{ kN}$.

N_{Ed} 561.00

-. $\frac{N_{Ed}}{N_{b,Rd}} = \frac{561.00}{845.80} = 0.663 < 1.000 \text{ ---> O.K.}$

[Reference]

N.S. Trahair, M.A. Bradford, D.A.Nethercot,
and L.Gardner, The behavior and Design of
Steel Structures to EC3, Taylor & Francis, 89-91
(Example 3.12.1)

3.8 Designing a UC compression member

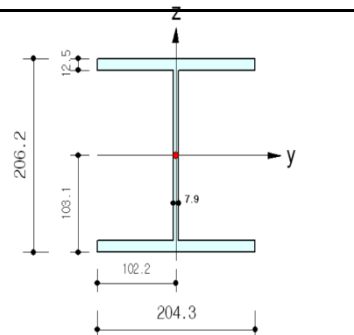
Design suitable UC of S355 steel to resist a factored axial compressive load corresponding to a nominal dead load of 160kN and a nominal imposed load of 230 kN.

3.8.1 Material Properties

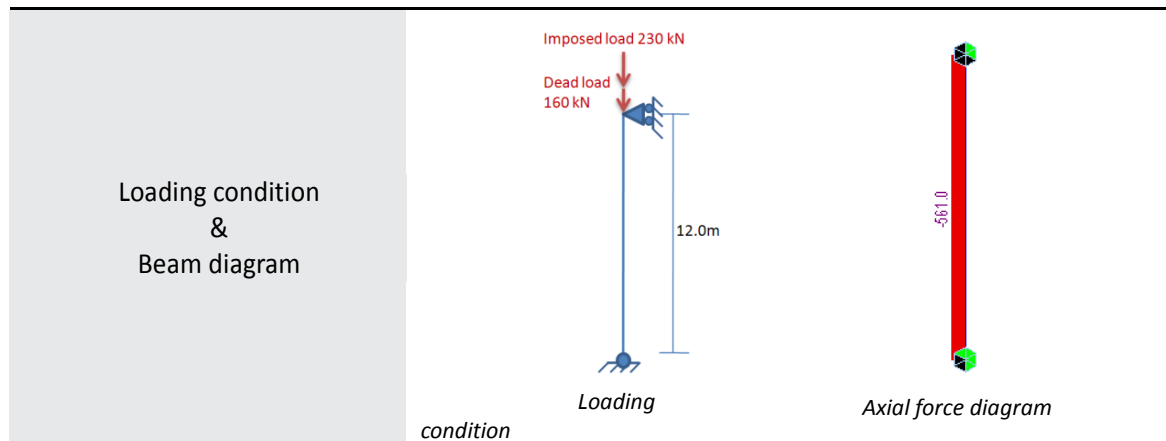
Material	S355	$f_y = 355 \text{ N/mm}^2$	$E_s = 210 \text{ GPa}$
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3.8.2 Section Properties

Section Name	152 x152 UC
Thickness (T)	206.2 mm
Width (B)	204.3 mm
Flange Thickness (T_f)	12.5 mm
Web Thickness (T_w)	7.9mm
Gross sectional area (A)	6630.0 mm ²
Shear area (A_{sz})	1876.25 mm ²



3.8.3 Analysis Model



3.8.4 Comparison of Design Results

	midas Gen	Example book	Error (%)
Buckling resistance	615.16kN	615.00kN	0.03%

3.8.5 Detailed comparison

midas Gen	Example book
<p>1. Cross-section classification</p> <p>(). Determine classification of compression outstand flanges.</p> <p>[Eurocode3:05 Table 5.2 (Sheet 2 of 3), EN 1993-1-5]</p> <ul style="list-style-type: none"> - $e = \text{SQRT}(235/f_y) = 0.81$ - $b/t = \text{BTR} = 7.04$ - $\sigma_1 = 0.085 \text{ kN/mm}^2$ - $\sigma_2 = 0.085 \text{ kN/mm}^2$ - $\text{BTR} < 9 \cdot e$ (Class 1 : Plastic). <p>(). Determine classification of compression Internal Parts.</p> <p>[Eurocode3:05 Table 5.2 (Sheet 1 of 3), EN 1993-1-5]</p> <ul style="list-style-type: none"> - $e = \text{SQRT}(235/f_y) = 0.81$ - $d/t = \text{HTR} = 20.35$ - $\sigma_1 = 0.085 \text{ kN/mm}^2$ - $\sigma_2 = 0.085 \text{ kN/mm}^2$ - $\text{HTR} < 33 \cdot e$ (Class 1 : Plastic). <p>2. CHECK AXIAL RESISTANCE.</p> <p>(). Check slenderness ratio of axial compression member (Kl/i).</p> <p>[Eurocode3:05 6.3.1]</p> <ul style="list-style-type: none"> - $Kl/i = 134.7 < 200.0 \rightarrow \text{O.K.}$ <p>(). Calculate axial compressive resistance (Nc_Rd).</p> <p>[Eurocode3:05 6.1, 6.2.4]</p> <ul style="list-style-type: none"> - $N_{c_Rd} = f_y \cdot \text{Area} / \text{Gamma_M0} = 2353.65 \text{ kN.}$ <p>(). Check ratio of axial resistance (N_Ed/Nc_Rd).</p> $\frac{N_{Ed}}{N_{c_Rd}} = \frac{561.00}{2353.65} = 0.238 < 1.000 \rightarrow \text{O.K.}$ <p>(). Calculate buckling resistance of compression member (Nb_Rdy, Nb_Rdz). [Eurocode3:05 6.3.1.1, 6.3.1.2]</p> <ul style="list-style-type: none"> - $\text{Beta_A} = A_{eff} / \text{Area} = 1.000$ - $\text{Lambda1} = \pi \cdot \text{SQRT}(E_s/f_y) = 76.409$ - $\text{Lambda_by} = \{(Kl_y/i_y)/\text{Lambda1}\} \cdot \text{SQRT}(\text{Beta_A}) = 1.763$ - $N_{cry} = \pi^2 \cdot E_s \cdot I_{yy} / (Kl_y)^2 = 757.08 \text{ kN.}$ - $\text{Lambda_by} > 0.2$ and $N_{Ed}/N_{cry} > 0.04 \rightarrow \text{Need to check.}$ - $\text{Alphay} = 0.340$ - $\text{Phiy} = 0.5 \cdot [1 + \text{Alphay} \cdot (\text{Lambda_by} - 0.2) + \text{Lambda_by}^2] = 2.319$ - $\text{Xiy} = \text{MIN} [1 / [\text{Phiy} + \text{SQRT}(\text{Phiy}^2 - \text{Lambda_by}^2)], 1.0] = 0.261$ - $N_{b_Rdy} = \text{Xiy} \cdot \text{Beta_A} \cdot \text{Area} \cdot f_y / \text{Gamma_M1} = 615.16 \text{ kN.}$ 	<p>Target area and first section choice.</p> <p>Assume $f_y = 355 \text{ N/mm}^2$ and $\chi = 0.5$</p> $A \geq 561 \times 10^3 / (0.5 \times 355) = 3161 \text{ mm}^2$ <p>Try a $152 \times 152 \text{ UC } 30$ with $A = 38.3 \text{ cm}^2$, $i_y = 6.76 \text{ cm}$, $i_z = 3.83 \text{ cm}$, $t_f = 9.4 \text{ mm}$. $\epsilon = (235/355)^{0.5} = 0.814$</p> $\lambda_y = \sqrt{\frac{A f_y}{N_{cr,y}}} = \frac{L_{cr,y}}{i_y} \frac{1}{\lambda_1} = \frac{12000}{(6.76 \times 10)} \frac{1}{93.9 \times 0.814} = 2.322$ $\lambda_z = \sqrt{\frac{A f_y}{N_{cr,z}}} = \frac{L_{cr,z}}{i_z} \frac{1}{\lambda_1} = \frac{6000}{(3.83 \times 10)} \frac{1}{93.9 \times 0.814} = 2.050 < 2.322$ <p>Buckling will occur about the major (y) axis. For a rolled UC section (with $h/b \leq 1.2$ and $t_f \leq 100 \text{ mm}$), buckling about the y-axis, use buckling curve (b) with $\alpha = 0.34$</p> $\Phi_y = 0.5 [1 + 0.34 (2.322 - 0.2) + 2.322^2] = 3.558$ $\chi_y = \frac{1}{3.558 + \sqrt{3.558^2 - 2.322^2}} = 0.160$ <p>which is much less than the guessed value of 0.5.</p> <p>Second section choice.</p> <p>Guess $\chi = (0.5 + 0.160)/2 = 0.33$</p> $A \geq 561 \times 10^3 / (0.33 \times 355) = 4789 \text{ mm}^2$ <p>Try a $203 \times 203 \text{ UC } 52$ with $A = 66.3 \text{ cm}^2$, $i_y = 8.91 \text{ cm}$, $t_f = 12.5 \text{ mm}$. For S255 steel with $t_f = 12.5 \text{ mm}$, $f_y = 355 \text{ N/mm}^2$ $\epsilon = (235/355)^{0.5} = 0.814$</p> $c_f / (t_f \epsilon) = [(204.3 - 7.9 - 2 \times 10.2) / 2] (12.5 \times 0.814) = 8.65 < 14$ $c_w / (t_w \epsilon) = (206.2 - 2 \times 12.5 - 2 \times 10.2) / (7.9 \times 0.814) = 25.0 > 42$ <p>and so the cross-section is fully effective.</p> $\lambda_y = \sqrt{\frac{A f_y}{N_{cr,y}}} = \frac{L_{cr,y}}{i_y} \frac{1}{\lambda_1} = \frac{12000}{(8.91 \times 10)} \frac{1}{93.9 \times 0.814} = 1.763$ <p>For a rolled UC section (with $h/b > 1.2$ and $t_f \leq 100 \text{ mm}$), buckling about the y-axis, use buckling curve (b) with $\alpha = 0.34$</p> $\Phi_y = 0.5 [1 + 0.34 (1.763 - 0.2) + 1.763^2] = 2.320$

(). Check ratio of buckling resistance ($N_{Ed}/N_{b,Rd}$).

-. $N_{b,Rd} = \text{MIN}[N_{b,Rdy}, N_{b,Rdz}] = 615.16 \text{ kN}$.

$$\therefore \frac{N_{Ed}}{N_{b,Rd}} = \frac{561.00}{615.16} = 0.912 < 1.000 \rightarrow \text{O.K.}$$

$$\chi_y = \frac{1}{2.032 + \sqrt{2.032^2 - 1.763^2}} = \mathbf{0.261}$$

$$N_{b,y,Rd} = \frac{\chi_y A f_y}{\gamma_{M1}} = \frac{0.261 \times 66.3 \times 10^2 \times 355}{1.0} \\ = \mathbf{615 \text{ KN}} > 561 \text{ KN} = N_{Ed}$$

and so the $203 \times 203 \text{ UC } 52$ is satisfactory.

[Reference]

N.S. Trahair, M.A. Bradford, D.A. Nethercot, and L. Gardner, The behavior and Design of Steel Structures to EC3, Taylor & Francis, 91-92 (Example 3.12.2)

3.9 Design an RHS compression

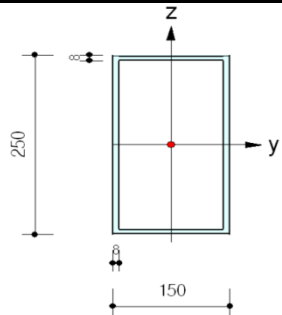
Design a suitable hot – finished RHS of S355 steel to resist a factored axial compressive load corresponding to a nominal dead load of 160kN and a nominal imposed load of 230 kN.

3.9.1 Material Properties

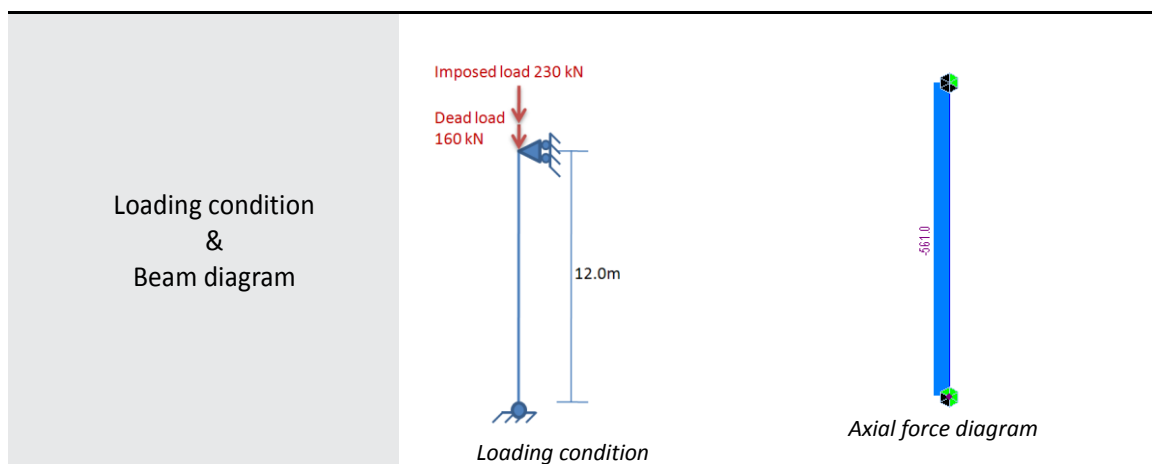
Material	S275	$f_y = 275 \text{ N/mm}^2$	$E_s = 210 \text{ GPa}$
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3.9.2 Section Properties

Section Name	250 X 150 X 8 RHS
Depth (H)	250.0 mm
Width (B)	150.0 mm
Flange Thickness (T_f)	8.0 mm
Web Thickness (T_w)	8.0 mm
Gross sectional area (A)	6080.0 mm ²
i_y	91.7mm



3.9.3 Analysis Model



3.9.4 Comparison of Design Results

	midas Gen	Example book	Error (%)
Buckling resistance	610.0kN	640.0kN	4.92%

3.9.5 Detailed comparison

midas Gen	Example book
<p>1. Cross-section classification</p> <p>(). Determine classification of compression Internal Parts. [Eurocode3:05 Table 5.2 (Sheet 1 of 3), EN 1993-1-5]</p> <ul style="list-style-type: none"> - $e = \text{SQRT}(235/f_y) = 0.81$ - $d/t = \text{HTR} = 28.25$ - $\sigma_1 = 0.095 \text{ kN/mm}^2$ - $\sigma_2 = 0.095 \text{ kN/mm}^2$ - $\text{HTR} < 38 \cdot e$ (Class 2 : Compact). <p>2. Check axial resistance.</p> <p>(). Check slenderness ratio of axial compression member (Kl/i). [Eurocode3:05 6.3.1]</p> <ul style="list-style-type: none"> - $Kl/i = 132.2 < 200.0 \rightarrow \text{O.K.}$ <p>(). Calculate axial compressive resistance (Nc_Rd). [Eurocode3:05 6.1, 6.2.4]</p> <ul style="list-style-type: none"> - $N_{c_Rd} = f_y \cdot \text{Area} / \text{Gamma_M0} = 2101.60 \text{ kN.}$ <p>(). Check ratio of axial resistance (N_Ed/Nc_Rd).</p> $\frac{N_{Ed}}{N_{c_Rd}} = \frac{561.00}{2101.60} = 0.267 < 1.000 \rightarrow \text{O.K.}$ <p>(). Calculate buckling resistance of compression member (Nb_Rdy, Nb_Rdz). [Eurocode3:05 6.3.1.1, 6.3.1.2]</p> <ul style="list-style-type: none"> - $\text{Beta_A} = A_{eff} / \text{Area} = 1.000$ - $\text{Lambda1} = \pi \cdot \text{SQRT}(E_s/f_y) = 76.409$ - $\text{Lambda_by} = \{(Kl_y/i_y)/\text{Lambda1}\} \cdot \text{SQRT}(\text{Beta_A})$ $= 1.730$ - $N_{cry} = \pi^2 \cdot E_s \cdot R_{yy} / Kl_y^2 = 703.83 \text{ kN.}$ - $\text{Lambda_by} > 0.2$ and $N_{Ed}/N_{cry} > 0.04$ $\rightarrow \text{Need to check.}$ - $\text{Alphay} = 0.210$ - $\text{Phiy} = 0.5 \cdot [1 + \text{Alphay} \cdot (\text{Lambda_by} - 0.2) + \text{Lambda_by}^2] = 2.156$ - $\text{Xiy} = \text{MIN} [1 / [\text{Phiy} + \text{SQRT}(\text{Phiy}^2 - \text{Lambda_by}^2)], 1.0] = 0.290$ - $\text{Nb_Rdy} = \text{Xiy} \cdot \text{Beta_A} \cdot \text{Area} \cdot f_y / \text{Gamma_M1}$ $= 610.18 \text{ kN.}$ - $\text{Lambda_bz} = \{(Kl_z/i_z)/\text{Lambda1}\} \cdot \text{SQRT}(\text{Beta_A})$ $= 1.283$ <p>(). Check ratio of buckling resistance (N_Ed/Nb_Rd).</p> <ul style="list-style-type: none"> - $\text{Nb_Rd} = \text{MIN} [\text{Nb_Rdy}, \text{Nb_Rdz}] = 610.18 \text{ kN.}$ - $\frac{N_{Ed}}{\text{Nb_Rd}} = \frac{561.00}{610.18} = 0.919 < 1.000 \rightarrow \text{O.K.}$ 	<p>Guess $\chi = 0.3$</p> $A \geq 561 \times 10^3 / (0.3 \times 355) = 5268 \text{ mm}^2$ <p>Try a $250 \times 150 \times 8 \text{ RHS}$, with $A = 60.8 \text{ cm}^2$, $i_y = 9.17 \text{ cm}$, $i_z = 6.15 \text{ cm}$, $t = 8.0 \text{ mm}$. For S355 steel with $t = 8 \text{ mm}$, $f_y = 355 \text{ N/mm}^2$ EN 10025-2</p> $\varepsilon = (235/355)^{0.5} = 0.814$ $c_w/(t\varepsilon) = \frac{(250.0 - 2 \times 8.0 - 2 \times 4.0)}{(8.0 \times 0.814)} = 34.7 < 42 \quad T5.2$ <p>And so the cross-section is fully effective.</p> $\bar{\lambda}_y = \sqrt{\frac{Af_y}{N_{cr,y}}} = \frac{L_{cr,y}}{i_y} \frac{1}{\lambda_1}$ $= \frac{12000}{(9.18 \times 10)} \frac{1}{93.9 \times 0.814} = 1.710$ $\bar{\lambda}_z = \sqrt{\frac{Af_y}{N_{cr,z}}} = \frac{L_{cr,z}}{i_z} \frac{1}{\lambda_1}$ $= \frac{6000}{(6.15 \times 10)} \frac{1}{93.9 \times 0.814} = 1.276$ <p>Buckling will occur about the major (y) axis. For a hot-finished RHS, use buckling curve (a) with $\alpha=0.21$</p> $\phi_y = 0.5[1 + 0.21(0.710 - 0.2) + 1.710^2] = 2.121 \geq 156$ $\chi_y = \frac{1}{2.121 + \sqrt{2.121^2 - 1.710^2}} = 0.296$ $N_{b,y,Rd} = \frac{\chi A f_y}{\gamma_{M1}} = \frac{0.296 \times 60.8 \times 10^3 \times 355}{1.0} = 640 \text{ kN} > 561 \text{ kN} = N_{Ed}$ <p>and so the $250 \times 150 > 8 \text{ RHS}$ is satisfactory</p>

Note.

The difference in buckling resistance occurred since currently midas Gen does not consider 'r' value for rolled box section. This can be improved in the future version.

[Reference]

N.S. Trahair, M.A. Bradford, D.A.Nethercot, and L.Gardner, The behavior and Design of Steel Structures to EC3, Taylor & Francis, 92-93 (Example 3.12.3)

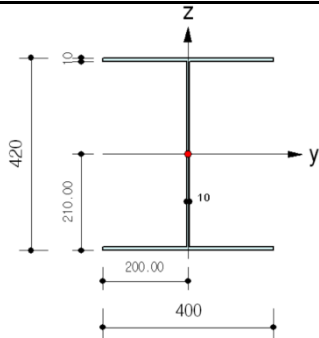
3.10 Compression resistance of a Class 4 compression member

Determine the compression resistance of the cross-section of the member shown in Figure the figure below.

3.10.1 Material Properties

Material	S275	$f_y = 275 \text{ N/mm}^2$	$E_s = 210 \text{ GPa}$
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3.10.2 Section Properties

Section Name	420 X 400	
Depth (H)	420.0 mm	
Width (B)	400.0 mm	
Flange Thickness (T_f)	10.0 mm	
Web Thickness (T_w)	10.0 mm	
Gross sectional area (A)	12054.9 mm ²	
Effective area (A_{eff})	9216.0 mm ²	

3.10.3 Comparison of Design Results

	midas Gen	Example book	Error (%)
Axial resistance	3271.45kN	3272.00kN	0.02%

3.10.4 Detailed comparison

midas Gen	Example book
1. Cross-section classification (). Determine classification of compression outstand flanges. [Eurocode3:05 Table 5.2 (Sheet 2 of 3), EN 1993-1-5] -. $e = \text{SQRT}(235/f_y) = 0.81$ -. $b/t = \text{BTR} = 18.70$ -. $\sigma_1 = 0.047 \text{ kN/mm}^2$. -. $\sigma_2 = 0.047 \text{ kN/mm}^2$. -. $\text{BTR} > 14 \cdot e$ (Class 4 : Slender). (). Determine classification of compression Internal Parts. [Eurocode3:05 Table 5.2 (Sheet 1 of 3), EN 1993-1-5] -. $e = \text{SQRT}(235/f_y) = 0.81$ -. $d/t = \text{HTR} = 38.40$ -. $\sigma_1 = 0.047 \text{ kN/mm}^2$. -. $\sigma_2 = 0.047 \text{ kN/mm}^2$. -. $\text{HTR} > 42 \cdot e$ (Class 4 : Slender). 2. Calculate Effective Area (). Calculate effective cross-section properties of left-top	Classifying the section plate elements. $t_f = 10 \text{ mm}$, $t_w = 10 \text{ mm}$, $f_y = 355 \text{ N/mm}^2$ En 10025-2 $\epsilon = (235/355)^{0.5} = 0.814$ $c_f / (t_f \epsilon) = (400/2 - 10/2 - 8) / (10 \times 0.814) = 23.0 > 14$ and so the flange is Class 4 . $c_w / (t_w \epsilon) = (420 - 2 \times 10 - 2 \times 8) / (10 \times 0.814) = 47.2 > 42$ and so the web is Class 4 . Effective flange area. $k_{\sigma f} = 0.43$ $\lambda_{pf} = \frac{(\frac{400}{2} - \frac{10}{2} - 8)/10}{28.4 \times 0.814 \times \sqrt{0.43}} = \mathbf{1.23} > 0.748$ $\rho_f = (1.23 - 0.188) / 1.23^2 = \mathbf{0.687}$ $A_{eff f} = 0.687 \times 4 \times (400/2 - 10/2 - 8) \times 10 + (10 + 2 \times 8) \times 10 \times 2 = \mathbf{5658 \text{ mm}^2}$

flange of Class 4 (Outstand element).

[Eurocode3 Part 1-5 4.4, Table 4.1, 4.2]

- RatT = 18.7000
- $\Lambda_p = \text{RatT} / [28.4 \cdot \epsilon \cdot \sqrt{k_{\sigma}}] =$
1.2342
- $\rho = \text{MIN} [(\Lambda_p - 0.188) / \Lambda_p^2, 1.0] =$
0.6868
- $\sigma_{\max} = \text{MAX} (\sigma_1, \sigma_2) = 0.047 \text{ kN/mm}^2$.
- $\sigma_{\min} = \text{MIN} (\sigma_1, \sigma_2) = 0.047 \text{ kN/mm}^2$.
- $r = 13.000 \text{ mm}$.
- $bc = 187.000 \text{ mm}$.
- $b_{\text{eff}} = \rho \cdot bc + r = 141.439 \text{ mm}$.
- $A_{\text{eff}} = b_{\text{eff}} \cdot t_f = \mathbf{1414.395 \text{ mm}^2}$.
- $y_{\text{eff}} = b_{\text{eff}} / 2 = 70.720 \text{ mm}$.

Effective flange area

- $A_{\text{eff}} \cdot 4 = \mathbf{5657.58 \text{ mm}^2}$

(). Calculate effective cross-section properties of web of Class 4 (Internal element).

[Eurocode3 Part 1-5 4.4, Table 4.1, 4.2]

- RatT = 38.4000
- $\Lambda_p = \text{RatT} / [28.4 \cdot \epsilon \cdot \sqrt{k_{\sigma}}] = \mathbf{0.8309}$
- $\rho = \text{MIN} [(\Lambda_p - 0.055 \cdot (3 + \psi)) / \Lambda_p^2, 1.0] = \mathbf{0.8848}$
- $\sigma_{\max} = \text{MAX} (\sigma_1, \sigma_2) = 0.047 \text{ kN/mm}^2$.
- $\sigma_{\min} = \text{MIN} (\sigma_1, \sigma_2) = 0.047 \text{ kN/mm}^2$.
- $r = 8.000 \text{ mm}$.
- $A_r = 0.000 \text{ mm}^2$.
- $dc = 384.000 \text{ mm}$.
- $d_{\text{eff1}} = 2 \cdot (\rho \cdot dc) / [5 - \sigma_{\min} / \sigma_{\max}] + r = 177.889 \text{ mm}$.
- $A_{\text{eff1}} = d_{\text{eff1}} \cdot t_w + 2 \cdot A_r = 1778.888 \text{ mm}^2$.
- $z_{\text{eff1}} = d_{\text{eff1}} / 2 + t_f = 98.944 \text{ mm}$.
- $d_{\text{eff2}} = (\rho \cdot dc) - d_{\text{eff1}} + r = 177.889 \text{ mm}$.
- $A_{\text{eff2}} = d_{\text{eff2}} \cdot t_w + 2 \cdot A_r = \mathbf{1778.888 \text{ mm}^2}$.
- $z_{\text{eff2}} = (h + 2 \cdot r) - d_{\text{eff2}} / 2 + t_f = 321.056 \text{ mm}$.

(). Calculated effective cross-section properties of Class4 cross-section.

- $A_{\text{eff}} = \mathbf{9215.3548 \text{ mm}^2}$. (for calculating axial resistance)

3. Check Axial Resistance**(). Check slenderness ratio of axial compression member (Kl/i).** [Eurocode3:05 6.3.1]

- $Kl/i = 53.1 < 200.0 \rightarrow \text{O.K.}$

(). Calculate axial compressive resistance (Nc_Rd).

[Eurocode3:05 6.1, 6.2.4]

- $N_{c,Rd} = f_y \cdot A_{\text{eff}} / \gamma_{M0} = \mathbf{3271.45 \text{ kN}}$.

Effective web area.

$$k_{\sigma,w} = 4.0$$

$$\lambda_{p,w} = \frac{(420 - 2 \times 10 - 2 \times 8) / 10}{28.4 \times 0.814 \times \sqrt{4.0}} = \mathbf{0.831} > 0.673$$

$$\rho_w = \{0.831 - 0.055 \cdot (3 + \psi)\} / 0.831^2 = \mathbf{0.885}$$

$$A_{\text{eff},w} = 0.885 \cdot (420 - 2 \cdot 10 - 2 \cdot 8) \cdot (10 + 8 \cdot 10 \cdot 2) = 3558 \text{ mm}^2$$

compression resistance.

$$A_{\text{eff}} = 5658 + 3558 = \mathbf{9216 \text{ mm}^2}$$

$$N_{c,Rd} = 9216 \cdot 355 / 1.0 \text{ N} = \mathbf{3272 \text{ kN}}$$

[Reference]

N.S. Trahair, M.A. Bradford, D.A. Nethercot, and L. Gardner, The behavior and Design of Steel Structures to EC3, Taylor & Francis, 141-142 (Example 4.9.1)

3.11 Section moment resistance of a Class 3 I-beam

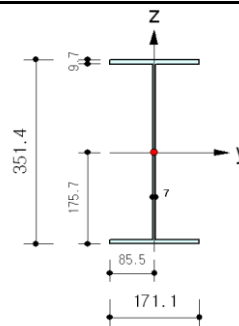
Determine the section moment resistance and examine the suitability for plastic design of the 356 X 171 UB 45 of S355 steel shown in the figure below.

3.11.1 Material Properties

Material	S355	$f_y = 355 \text{ N/mm}^2$	$E_s = 210 \text{ GPa}$
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3.11.2 Section Properties

Section Name	356 X 171 UB 45
Depth (H)	351.4 mm
Width (B)	171.1 mm
Flange Thickness (T_f)	9.7 mm
Web Thickness (T_w)	7.0 mm
Gross sectional area (A)	573,000 mm ²
Plastic section modulus (W_{pl})	775.0 cm ³



3.11.3 Comparison of Design Results

	midas Gen	Example book	Error (%)
Moment resistance	275.12kNm	275.10kNm	0.01%

3.11.4 Detailed comparison

midas Gen	Example book
<p>1. Cross-section classification</p> <p>(). Determine classification of compression outstand flanges.</p> <p>[Eurocode3:05 Table 5.2 (Sheet 2 of 3), EN 1993-1-5]</p> <p>-. $e = \text{SQRT}(235/f_y) = 0.81$</p> <p>-. $b/t = \text{BTR} = 7.41$</p> <p>-. $\sigma_1 = 358215.065 \text{ KPa}$.</p> <p>-. $\sigma_2 = 358215.065 \text{ KPa}$.</p> <p>-. $\text{BTR} < 10 \cdot e$ (Class 2 : Compact).</p> <p>(). Determine classification of bending Internal Parts.</p> <p>[Eurocode3:05 Table 5.2 (Sheet 1 of 3), EN 1993-1-5]</p> <p>-. $e = \text{SQRT}(235/f_y) = 0.81$</p> <p>-. $d/t = \text{HTR} = 44.51$</p>	<p>Classifying the section- plate elements.</p> <p>$t_f = 9.7 \text{ mm}$, $t_w = 7.0 \text{ mm}$, $f_y = 355 \text{ N/mm}^2$</p> <p>En 10025-2</p> <p>$\epsilon = \sqrt{235/355}^{0.5} = 0.814$</p> <p>$c_f / (t_f \epsilon) = (171.1/2 - 7.0/2 - 10.2) (9.7 \times 0.814)$</p> <p>$= 9.1 > 9$ and so the flange is Class 2.</p> <p>$c_w / (t_w \epsilon) = (351.4 - 2 \times 9.7 - 2 \times 10.2)$</p> <p>$/ (7.0 \times 0.814)$</p> <p>$= 54.7 > 72$ and so the web is Class 1.</p>

- $\sigma_1 = 652365.952 \text{ KPa}$.
- $\sigma_2 = -652365.952 \text{ KPa}$.
- $HTR < 72 \cdot e$ (**Class 1 : Plastic**).

2. Check Bending Moment Resistance About Major Axis.

(). Calculate plastic resistance moment about major axis.

[Eurocode3:05 6.1, 6.2.5]

- $W_{ply} = 0.0008 \text{ m}^3$.
- $M_{c,Rd} = W_{ply} \cdot f_y / \gamma_{M0} = \mathbf{275.12 \text{ kN-m}}$.

section moment resistance

The cross-section is Class 2 and therefore unsuitable for plastic design.

$$M_{c,Rd} = 775 \times 10^3 \times 355 / 1.0 \text{ N} = \mathbf{275.1 \text{ kNm}}$$

[Reference]

N.S. Trahair, M.A. Bradford, D.A.Nethercot, and L.Gardner, The behavior and Design of Steel Structures to EC3, Taylor & Francis, 142-143 (Example 4.9.2)

3.12 Section moment resistance of a Class 4 box beam

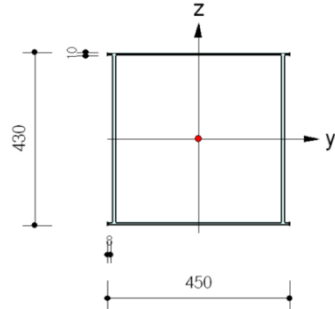
Determine the section moment resistance of the welded-box section beam of S355 steel shown in the figure below. The weld size is 6 mm.

3.12.1 Material Properties

Material	S355	$f_y = 355 \text{ N/mm}^2$	$E_s = 210 \text{ GPa}$
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3.12.2 Section Properties

Section Name	RHS 430 X 450
Depth (H)	430.0 mm
Width (B)	450.0 mm
Flange Thickness (T_f)	10.0 mm
Web Thickness (T_w)	8.0 mm
Gross sectional area (A)	15560.0 mm ²
Shear area (A_{sz})	6880.00 mm ²



3.12.3 Comparison of Design Results

	midas Gen	Example book	Error (%)
Moment resistance	729.99kN	729.90kNm	0.01%

3.12.4 Detailed comparison

midas Gen	Example book
1. Cross-section classification (). Determine classification of compression Internal Parts. [Eurocode3:05 Table 5.2 (Sheet 1 of 3), EN 1993-1-5] -. $e = \text{SQRT}(235/f_y) = 0.81$ -. $d/t = \text{HTR} = 41.00$ -. $\sigma_1 = 0.108 \text{ kN/mm}^2$. -. $\sigma_2 = 0.108 \text{ kN/mm}^2$. -. $\text{HTR} > 42 \cdot e$ (Class 4 : Slender). (). Determine classification of bending Internal Parts. [Eurocode3:05 Table 5.2 (Sheet 1 of 3), EN 1993-1-5] -. $e = \text{SQRT}(235/f_y) = 0.81$ -. $d/t = \text{HTR} = 51.75$ -. $\sigma_1 = 0.099 \text{ kN/mm}^2$. -. $\sigma_2 = -0.099 \text{ kN/mm}^2$. -. $\text{HTR} < 72 \cdot e$ (Class 1 : Plastic).	Classifying the section- plate elements. $t_f = 10 \text{ mm}$, $t_w = 8 \text{ mm}$, $f_y = 355 \text{ N/mm}^2$ En 10025-2 $\epsilon = \sqrt{235/355} = 0.814$ $c_f / (t_f \epsilon) = 410 (10 \times 0.814)$ $= 50.4 > 42$ and so the flange is Class 4 . $c_w / (t_w \epsilon) = (430 - 2 \times 10 - 2 \times 6) / (8 \times 0.814)$ $= 61.1 > 72$ and so the web is Class 1 . The cross-section is therefore Class 4 since the flange is Class 4 .

2. Calculate Effective Section Modulus About Major Axis.**(). Calculate buckling factor of internal compression element.**

[Eurocode3 Part 1-5 4.4, Table 4.1]

-. In case of $\Psi = 1.0$ -. $k_{\sigma} = 4.0000$ **(). Calculate effective cross-section properties of top flange of Class 4 (Internal element).**

[Eurocode3 Part 1-5 4.4, Table 4.1, 4.2]

-. $RatT = 41.0000$ -. $\lambda_{p} = RatT / [28.4 * \epsilon * \sqrt{k_{\sigma}}] = 0.8872$ -. $\rho = \min[(\lambda_{p} - 0.055 * (3 + \psi)) / (\lambda_{p}^2 - 1.0)] = 0.8477$ -. $\sigma_{max} = \max(\sigma_1, \sigma_2) = 0.108 \text{ kN/mm}^2$ -. $\sigma_{min} = \min(\sigma_1, \sigma_2) = 0.108 \text{ kN/mm}^2$ -. $r = 40.000 \text{ mm}$ -. $bc = 410.000 \text{ mm}$ -. $b_{eff} = \rho * bc + r = 387.537 \text{ mm}$ -. $A_{eff} = b_{eff} * t_f = 3875.367 \text{ mm}^2$ -. $y_{eff} = b_{eff} / 2 = 193.768 \text{ mm}$ **(). Calculate cross-section properties of bottom flange.**-. $r = 40.000 \text{ mm}$ -. $bc = 410.000 \text{ mm}$ -. $b_{eff} = bc + r = 450.000 \text{ mm}$ -. $A_{eff} = b_{eff} * t_f = 4500.000 \text{ mm}^2$ -. $y_{eff} = b_{eff} / 2 = 225.000 \text{ mm}$ **(). Calculate cross-section properties of left web.**-. $r = 0.000 \text{ mm}$ -. $A_r = 0.000 \text{ mm}^2$ -. $dc = 410.000 \text{ mm}$ -. $d_{eff} = dc + r = 410.000 \text{ mm}$ -. $A_{eff} = d_{eff} * t_w + 4 * A_r = 3280.000 \text{ mm}^2$ -. $z_{eff} = (h + 2 * r) - d_{eff} / 2 = 215.000 \text{ mm}$ **(). Calculate cross-section properties of right web.**-. $r = 0.000 \text{ mm}$ -. $A_r = 0.000 \text{ mm}^2$ -. $dc = 410.000 \text{ mm}$ -. $d_{eff} = dc + r = 410.000 \text{ mm}$ -. $A_{eff} = d_{eff} * t_w + 4 * A_r = 3280.000 \text{ mm}^2$ -. $z_{eff} = (h + 2 * r) - d_{eff} / 2 = 215.000 \text{ mm}$ **(). Calculated effective cross-section properties of Class4 cross-section.**-. $A_{effy} = 14935.3672 \text{ mm}^2$ -. $W_{effy} = 2056307.7227 \text{ mm}^3$ **Effective cross-section** $k_{\sigma} = 4.0$ $\lambda_p = \frac{410}{10 \times 28.4 \times 0.814 \times \sqrt{4.0}} = 0.887 > 0.673$ $\psi = 1$ $\rho = (0.887 - 0.055 \times (3 + 1)) / 0.887^2 = 0.848$ $b_{c,eff} = 0.848 \times 410 = 347.5 \text{ mm}$ $A_{eff} = (450 - 410 + 347.5) \times 10 + (450 \times 10) + 2 \times (430 - 2 \times 10) \times 8 = 14935 \text{ mm}^2$ $14935 \times z_c = (450 - 410 + 347.5) \times 10 \times (430 - 10/2) + 450 \times 10 \times 10/2 + 2 \times (430 - 2 \times 10) \times 8 \times 430/2$ $z_c = 206.2 \text{ mm}$ $I_{eff} = (450 - 410 + 347.5) \times 10 \times (430 - 10/2 - 206.2)^2 + 450 \times 10 \times (206.2 - 10/2)^2 + 2 \times (430 - 2 \times 10)^3 \times 8/12 + 2 \times (430 - 2 \times 10) \times 8 \times (430/2 - 206.2)^2$
 mm^4
 $= 460.1 \times 10^6 \text{ mm}^4$

4. CHECK BENDING MOMENT RESISTANCE ABOUT MAJOR AXIS.

(). Calculate local buckling resistance moment about major axis. [Eurocode3:05 6.1, 6.2.5]

$$- W_{effy} = 2056307.7227 \text{ mm}^3.$$

$$- M_{c,Rd} = W_{effy} * f_y / \gamma_{M1} = 729989.24 \text{ kN-mm}.$$

Section moment resistance

$$W_{eff, min} = 460.1 \times 10^6 / (430 - 206.2) = 2.056 \times 10^6 \text{ mm}^3$$

$$M_{c,Rd} = 2.056 \times 10^6 \times 355 / 1.0 \text{ N} = 729.9 \text{ KNm}.$$

[Reference]

N.S. Trahair, M.A. Bradford, D.A.Nethercot, and L.Gardner, The behavior and Design of Steel Structures to EC3, Taylor & Francis, 143-144 (Example 4.9.3)

3.13 Section moment resistance of a slender plate girder

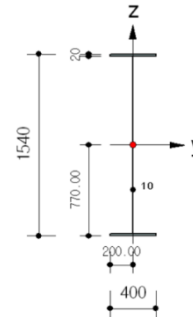
Determine the section moment resistance of the welded plate girder of S355 steel shown in the figure below. The weld size is 6 mm.

3.13.1 Material Properties

Material	S355	$f_y = 355 \text{ N/mm}^2$	$E_s = 210 \text{ GPa}$
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3.13.2 Section Properties

Section Name	1540x400
Depth (H)	1540.0 mm
Width (B)	400.0 mm
Flange Thickness (T_f)	20.0 mm
Web Thickness (T_w)	10.0 mm
Gross sectional area (A)	31030.9 mm^2
Effective area (A_{eff})	$14.48 \times 10^6 \text{ mm}^2$



3.13.3 Comparison of Design Results

	midas Gen	Example book	Error (%)
Moment resistance	4996.42kNm	4996.00kNm	0.01%

3.13.4 Detailed comparison

midas Gen	Example book
1. Cross-section classification (). Determine classification of compression outstand flanges. [Eurocode3:05 Table 5.2 (Sheet 2 of 3), EN 1993-1-5] -. $e = \text{SQRT}(235/f_y) = 0.83$ -. $b/t = \text{BTR} = 9.45$ -. $\sigma_1 = 0.016 \text{ kN/mm}^2$. -. $\sigma_2 = 0.016 \text{ kN/mm}^2$. -. $\text{BTR} < 14 * e$ (Class 3 : Semi-compact). (). Determine classification of bending Internal Parts. [Eurocode3:05 Table 5.2 (Sheet 1 of 3), EN 1993-1-5] -. $e = \text{SQRT}(235/f_y) = 0.83$ -. $d/t = \text{HTR} = 148.80$ -. $\sigma_1 = 0.015 \text{ kN/mm}^2$. -. $\sigma_2 = -0.015 \text{ kN/mm}^2$. -. $\text{HTR} > 124 * e$ (Class 4 : Slender)	$t_f = 20 \text{ mm}$, $t_w = 10 \text{ mm}$, $f_y = 345 \text{ N/mm}^2$ $\epsilon = \sqrt{(235/345)^{0.5}} = 0.825$ $c_f / (t_f \epsilon) = (400/2 - 10/2 - 6) / (20 \times 0.825)$ $= 11.5 > 10$ but < 14 , and so the flange is Class 3. $c_w / (t_w \epsilon) = (1540 - 2 \times 20 - 2 \times 6) / (10 \times 0.825)$ $= 180.3 > 124$ and so the web is Class 4. A conservative approximation for the cross-section moment resistance may be obtained by ignoring the web completely, so that $M_{c,Rd} = M_f = (400 \times 20) \times (1540 - 20) \times 345 / 1.0 \text{ N}$ $= 4195 \text{ kNm}$. A higher resistance may be calculated by determining the

2. Calculate Effective Section Modulus About Major Axis.

(). Calculate cross-section properties of left-top flange.

[Eurocode3 Part 1-5 4.4, Table 4.1, 4.2]

- . $r = 11.000 \text{ mm.}$
- . $bc = 189.000 \text{ mm.}$
- . $beff = bc + r = 200.000 \text{ mm.}$
- . $A_{eff} = beff * tf = 4000.000 \text{ mm}^2.$
- . $yeff = beff/2 = 100.000 \text{ mm.}$

(). Calculate cross-section properties of right-top flange.

- . $beff = bc + r = 200.000 \text{ mm.}$
- . $A_{eff} = beff * tf = 4000.000 \text{ mm}^2.$
- . $yeff = beff/2 = 100.000 \text{ mm.}$

(). Calculate cross-section properties of left-bottom flange.

- . $beff = bc + r = 200.000 \text{ mm.}$
- . $A_{eff} = beff * tf = 4000.000 \text{ mm}^2.$
- . $yeff = beff/2 = 100.000 \text{ mm.}$

(). Calculate cross-section properties of right-bottom flange.

- . $beff = bc + r = 200.000 \text{ mm.}$
- . $A_{eff} = beff * tf = 4000.000 \text{ mm}^2.$
- . $yeff = beff/2 = 100.000 \text{ mm.}$

(). Calculate buckling factor of internal compression element.

- . In case of $\Psi = -1.0$
- . $k_{\sigma} = 23.9000$

(). Calculate effective cross-section properties of web

- . $RatT = 148.8000$
- . $\Lambda_p = RatT / [28.4 * \epsilon * \sqrt{k_{\sigma}}] = 1.2986$
- . $\rho = \min[(\Lambda_p - 0.055 * (3 + \psi)) / \Lambda_p^2, 1.0] = 0.7049$
- . $\sigma_{max} = \max(\sigma_1, \sigma_2) = 0.015 \text{ kN/mm}^2.$
- . $\sigma_{min} = \min(\sigma_1, \sigma_2) = -0.015 \text{ kN/mm}^2.$
- . $r = 6.000 \text{ mm.}$
- . $Ar = 0.000 \text{ mm}^2.$
- . $dc = (h * \sigma_{max}) / (\sigma_{max} - \sigma_{min}) = 744.0 \text{ mm.}$
- . $deff1 = 0.4 * \rho * dc + r = 215.764 \text{ mm.}$

effective width of the web.

$$\psi = 1$$

$$k_{\sigma} = 23.9$$

$$\lambda_p = \frac{(1540 - 2 \times 20 - 2 \times 6) / 10}{28.4 \times 0.825 \times \sqrt{23.9}} = 1.299$$

$$\rho = (1.299 - 0.055 \times (3 - 1)) / 1.299^2 = 0.705$$

$$b_c = (1540 - 2 \times 20 - 2 \times 6) / \{1 - (-1)\} = 744.0 \text{ mm}$$

$$b_{eff} = 0.705 \times 744.0 = 524.4 \text{ mm}$$

$$b_{e1} = 0.4 \times 524.4 = 209.8 \text{ mm}$$

$$b_{e2} = 0.6 \times 524.4 = 314.6 \text{ mm}$$

and the ineffective width of the web is

$$b_c - b_{e1} - b_{e2} = 744.0 - 209.8 - 314.6 = 219.6 \text{ mm}$$

$$A_{eff} = (1540 - 2 \times 20 - 219.6) \times 10 + 2 \times 400 \times 20 = 28804 \text{ mm}^2$$

$$28804 \times z_c = (2 \times 400 \times 20 + (1540 - 2 \times 20) \times 10) \times ((1540 / 2) - 219.6 \times 10 \times (1540 - 20 - 6 - 209.8 - 219.6 / 2))$$

$$z_c = 737.6 \text{ mm}$$

$$I_{eff} = (400 \times 20) \times (1540 - 10 - 737.6)^2 + (400 \times 20) \times (737.6 - 10)^2 + (1540 - 2 \times 20)^3 \times 10 / 12 + (1540 - 2 \times 20) \times 10 \times (1540 / 2 - 737.6)^2 - 219.6^3 \times 10 / 12 - 219.6 \times 10 \times (1540 - 20 - 6 - 209.8 - 219.6 / 2 - 737.6)^2 \text{ mm}^4$$

$$= 11.62 \times 10^9 \text{ mm}^4$$

$$W_{eff} = 11.62 \times 10^9 / (1540 - 737.6) = 14.48 \times 10^6 \text{ mm}^3$$

$$M_{c,Rd} = 14.48 \times 10^6 \times 345 / 1.0 \text{ N} = 4996 \text{ kNm.}$$

$$\begin{aligned}
 -. A_{eff1} &= d_{eff1} * t_w + 2 * A_r = \mathbf{2157.639 \text{ mm}^2}. \\
 -. z_{eff1} &= (h + 2 * r) - d_{eff1} / 2 + t_f = 1412.118 \text{ mm}. \\
 -. d_{eff2} &= 0.6 * R_{ho} * d_c + (h - d_c) + r = 1064.646 \text{ mm}. \\
 -. A_{eff2} &= d_{eff2} * t_w + 2 * A_r = \mathbf{10646.458 \text{ mm}^2}. \\
 -. z_{eff2} &= d_{eff2} / 2 + t_f = 552.323 \text{ mm}.
 \end{aligned}$$

(). Calculated effective cross-section properties of Class4 cross-section.

$$\begin{aligned}
 -. A_{effy} &= \mathbf{28804.0968 \text{ mm}^2}. \\
 -. W_{effy} &= \mathbf{14482394.1334 \text{ mm}^3}.
 \end{aligned}$$

4. Check Bending Moment Resistance About Major Axis

(). Calculate local buckling resistance moment about major axis. [Eurocode3:05 6.1, 6.2.5]

$$\begin{aligned}
 -. W_{effy} &= 14482394.1334 \text{ mm}^3. \\
 -. M_{c_Rdy} &= W_{effy} * f_y / \Gamma_{M1} \\
 &= \mathbf{4996425.98 \text{ kN-mm}}.
 \end{aligned}$$

[Reference]

N.S. Trahair, M.A. Bradford, D.A.Nethercot, and L.Gardner, The behavior and Design of Steel Structures to EC3, Taylor & Francis, 144-145 (Example 4.9.4)

3.14 Shear buckling resistance of an unstiffened plate girder web

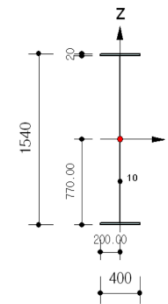
Determine the shear buckling resistance of the unstiffened plate girder web of S355 steel shown in the figure below

3.14.1 Material Properties

Material	S355	$f_y = 355 \text{ N/mm}^2$	$E_s = 210 \text{ GPa}$
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3.14.2 Section Properties

Section Name	1540x400
Depth (H)	1540.0 mm
Width (B)	400.0 mm
Flange Thickness (T_f)	20.0 mm
Web Thickness (T_w)	10.0 mm
Gross sectional area (A)	31030.9 mm^2
Effective area (A_{eff})	$14.48 \times 10^6 \text{ mm}^2$



3.14.3 Comparison of Design Results

	midas Gen	Example book	Error (%)
Shear resistance	1195.86kN	1196.00kN	0.01%

3.14.4 Detailed comparison

midas Gen	Example book
1. Cross-section classification (). Determine classification of compression outstand flanges. [Eurocode3:05 Table 5.2 (Sheet 2 of 3), EN 1993-1-5] -. $e = \text{SQRT}(235/f_y) = 0.81$ -. $b/t = \text{BTR} = 9.45$ -. $\sigma_1 = 0.016 \text{ kN/mm}^2$ -. $\sigma_2 = 0.016 \text{ kN/mm}^2$ -. $\text{BTR} < 14 \cdot e$ (Class 3 : Semi-compact).	$t_f = 20 \text{ mm}$, $t_w = 10 \text{ mm}$, $f_y = 345 \text{ N/mm}^2$ $\epsilon = \sqrt{235/355} = 0.814$ $\eta = 1.2$ $h_w = 1540 - 2 \times 20 = 1500 \text{ mm}$ $\eta h_w / (t_w \epsilon) = 1.2 \times 1500 / (10 \times 0.814) = 221.2 > 72$ and so the web is slender
(). Determine classification of bending Internal Parts. [Eurocode3:05 Table 5.2 (Sheet 1 of 3), EN 1993-1-5] -. $e = \text{SQRT}(235/f_y) = 0.81$ -. $d/t = \text{HTR} = 148.80$ -. $\sigma_1 = 0.015 \text{ kN/mm}^2$ -. $\sigma_2 = -0.015 \text{ kN/mm}^2$	$\alpha / h_w = \infty / h_w = \infty$, $k_{tst} = 0$ $k_t = 5.34$ $\tau_{cr} = 5.34 \times 190000 \times (10/1500)^2 = 45.1 \text{ N/mm}^2$ $\lambda_w = 0.76 \times \sqrt{355/45.1} = 2.132 > 1.08$ Assuming that there is a non-rigid end post, then $\chi_w = 0.83 / 2.132 = 0.389$

-. $HTR > 124 \cdot e$ (Class 4 : Slender)

2. Check Shear Resistance.

(). Calculate shear buckling resistance in local-z direction (V_{bl_Rdz}). [Eurocode3:05 6.1, 6.2.6, EN 1993-1-5:2004 5.2]

-. $\eta = 1.20$

-. $\lambda_w = h_w / (86.4 \cdot t_w \cdot e) = 2.1338$

-. $\chi_w = 0.83 / \lambda_w = 0.39$

-. $V_{bw_Rdz} = \chi_w \cdot f_y \cdot h_w \cdot t_w / [\sqrt{3} \cdot \gamma_{M1}]$
 $= 1195.86 \text{ kN.}$

Neglecting any contribution from the flanges,

$$V_{b,Rd} = V_{bw,Rd} = \frac{(0.389 \times 355 \times 1500 \times 10)}{\sqrt{3} \times 1.0} \text{ N} = 1196 \text{ KN}$$

[Reference]

N.S. Trahair, M.A. Bradford, D.A.Nethercot, and L.Gardner, The behavior and Design of Steel Structures to EC3, Taylor & Francis, 145-146 (Example 4.9.5)

3.15 Checking a simply supported beam

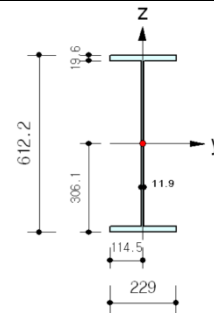
The simply supported 610 X 229 UB 125 of S275 steel shown in the right figure has a span of 6.0m and is laterally braced at 1.5m intervals. Check the adequacy of the beam for a nominal uniformly distributed dead load of 60 kNm together with a nominal uniformly distributed imposed load of 70 kNm.

3.15.1 Material Properties

Material	S275	$f_y = 265 \text{ N/mm}^2$	$E_s = 210 \text{ GPa}$
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3.15.2 Section Properties

Section Name	UB 610x229x125
Depth (H)	612.2 mm
Width (B)	229.0 mm
Flange Thickness (T_f)	19.6 mm
Web Thickness (T_w)	11.9 mm
Gross sectional area (A)	15900.0 mm ²
Plastic section modulus ($W_{pl,y}$)	3676.0 cm ³



3.15.3 Analysis Model

Loading condition		
Beam Diagram	SF	
	BM	

3.15.4 Comparison of Design Results

	midas Gen	Example book	Error (%)
Shear resistance	1251.9kN	1171.00kN	6.46%
Bending resistance	975.2kNm	974.00kNm	0.12%

Note.

Shear resistance is calculated with an error of 6.46% due to the difference in shear area, A_v . In the example book, the minimum value of shear area ' ηh_{wt_w} ' was not considered whereas it was considered in midas Gen. (6.2.6 (3) EN 1993-1-1:2005)

3.15.5 Detailed comparison

midas Gen	Example book
<p>1. Cross-section classification</p> <p>(). Determine classification of compression outstand flanges.</p> <p>[Eurocode3:05 Table 5.2 (Sheet 2 of 3), EN 1993-1-5]</p> <ul style="list-style-type: none"> - $e = \text{SQRT}(235/f_y) = 0.94$ - $b/t = BTR = 4.89$ - $\sigma_1 = 0.260 \text{ kN/mm}^2$. - $\sigma_2 = 0.260 \text{ kN/mm}^2$. - $BTR < 9 \cdot e$ (Class 1 : Plastic). <p>(). Determine classification of bending internal parts.</p> <p>[Eurocode3:05 Table 5.2 (Sheet 1 of 3), EN 1993-1-5]</p> <ul style="list-style-type: none"> - $e = \text{SQRT}(235/f_y) = 0.94$ - $d/t = HTR = 46.02$ - $\sigma_1 = 0.622 \text{ kN/mm}^2$. - $\sigma_2 = -0.622 \text{ kN/mm}^2$. - $HTR < 72 \cdot e$ (Class 1 : Plastic). <p>2. Check Bending Moment Resistance About Major Axis</p> <p>(). Calculate plastic resistance moment about major axis.</p> <p>[Eurocode3:05 6.1, 6.2.5]</p> <ul style="list-style-type: none"> - $W_{ply} = 3680000.0000 \text{ mm}^3$. - $M_{c,Rd} = W_{ply} \cdot f_y / \text{Gamma}_{M0}$ = 975.20 kN-m. <p>(). Check ratio of moment resistance ($M_{Edy}/M_{c,Rd}$).</p> <p>$M_{Edy} \quad 837.0$</p> <p>- $\frac{\quad}{M_{c,Rd} \quad 975.2} = \frac{\quad}{\quad} = 0.858 < 1.000 \rightarrow \text{O.K.}$</p> <p>3. Check Shear Resistance.</p> <p>(). Calculate shear area.</p> <p>[Eurocode3:05 6.2.6, EN1993-1-5:04 5.1 NOTE 2]</p> <ul style="list-style-type: none"> - $\eta = 1.2$ ($F_y < 460 \text{ MPa}$.) - $r = 12.7000 \text{ mm}$. - $A_{v1} = \text{Area} - h_w \cdot t_w = 9081.3000 \text{ mm}^2$. - $A_{vz1} = \eta \cdot h_w \cdot t_w = \mathbf{8182.4400 \text{ mm}^2}$. - $A_{vz2} = \text{Area} - 2 \cdot B \cdot t_f + (t_w + 2 \cdot r) \cdot t_f = \mathbf{7654.2800 \text{ mm}^2}$. - $A_{vz} = \text{MAX}[A_{vz1}, A_{vz2}] = \mathbf{8182.4400 \text{ mm}^2}$. <p>(). Calculate plastic shear resistance in local-z direction ($V_{pl,Rdz}$). [Eurocode3:05 6.1, 6.2.6]</p> <ul style="list-style-type: none"> - $V_{pl,Rdz} = [A_{vz} \cdot f_y / \text{SQRT}(3)] / \text{Gamma}_{M0} = \mathbf{1251.90}$ 	<p>Classifying the section.</p> <p>$t_f = 19.6 \text{ mm}$, $f_y = 265 \text{ N/mm}^2$ En 10025-2</p> <p>$\epsilon = \sqrt{235/265}^{0.5} = 0.942$</p> <p>$c_f / (t_f \epsilon) = (229/2 - 11.9/2 - 12.7) (19.6 \times 0.942)$ = $5.19 < 9$ and the flange is Class 1.</p> <p>$c_w / (t_w \epsilon) = (612.2 - 2 \times 19.6 - 2 \times 12.7) / (11.9 \times 0.942)$ = $48.9 > 72$ and the web is Class 1.</p> <p>(Note the general use of the minimum f_y obtained for the flange.)</p> <p>Checking for moment.</p> <p>$q_{Ed} = (1.35 \times 60) + (1.5 \times 70) = 186 \text{ KNm}$</p> <p>$M_{Ed} = 186 \times 6^2 / 8 = 837 \text{ KNm}$</p> <p>$M_{c,Rd} = 3676 \times 10^3 \times 265 / 1.0 \text{ Nmm}$ = 975 KNm $> 837 \text{ KNm} = M_{Ed}$</p> <p>Which is satisfactory.</p> <p>Checking for shear.</p> <p>$V_{Ed} = 186 \times \frac{6}{2} = 558 \text{ KN}$</p> <p>$A_v = 159 \times 10^2 - 2 \times 229 \times 19.6 + (11.9 + 2 \times 12.7) \times 19.6 = \mathbf{7654 \text{ mm}^2}$</p> <p>$V_{c,Rd} = 7654 \times (265 / \sqrt{3}) / 1.0 \text{ N} = \mathbf{1171 \text{ KN}} > 558 \text{ KN} = V_{Ed}$</p> <p>Which is satisfactory.</p> <p>Checking for bending and shear.</p>

kN.

(). Check ratio of shear resistance (V_{Edz}/V_{pl_Rdz}).

(LCB = 1, POS = J)

-. Applied shear force : $V_{Edz} = 558.00$ kN.

$V_{Edz} \quad 558.00$

-. $\frac{V_{Edz}}{V_{pl_Rdz}} = \frac{558.00}{1251.90} = 0.446 < 1.000 \rightarrow$ O.K.

$V_{pl_Rdz} \quad 1251.90$

Note.

The difference in shear resistance occurred since the midas Gen consider the additional condition when calculating shear area as per EN1993-1-1:2005, sub clause 6.2.6(3) a).

$$A_v = A - 2bt_f + (t_w + 2r)t_f \text{ but not less than } \eta h_w t_w$$

The maximum M_{Ed} occurs at mid-span where $V_{Ed} = 0$, and the maximum V_{Ed} occurs at the support where $M_{Ed} = 0$, and so there is no need to check for combined bending and shear. (Note that in any case, $0.5V_{c,Rd} = 0.5$

$$\times 1171 = 585.5 \text{ kN}$$

$> 558 \text{ kN} = V_{Ed}$ and so the combined bending and shear condition does not operate.)

[Reference]

N.S. Trahair, M.A. Bradford, D.A. Nethercot, and L. Gardner, The behavior and Design of Steel Structures to EC3, Taylor & Francis, 209-211 (Example 5.12.5)

3.16 Serviceability of a simply supported beam

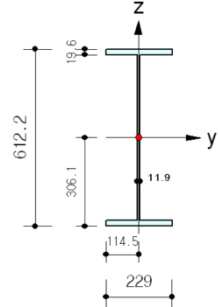
Check the imposed load deflection of the 610 X 229 UB 125 of right figure for a serviceability limit of $L/360$.

3.16.1 Material Properties

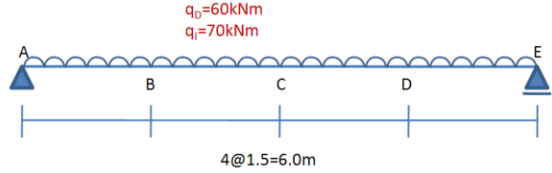
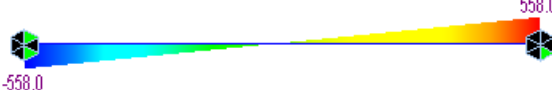

Material	S275	$f_y = 275 \text{ N/mm}^2$	$E_s = 210 \text{ GPa}$
----------	------	----------------------------	-------------------------

3.16.2 Section Properties

Section Name	UB 610x229x125
Depth (H)	612.2 mm
Width (B)	229.0 mm
Flange Thickness (T_f)	19.6 mm
Web Thickness (T_w)	11.9 mm
Gross sectional area (A)	15900.0 mm ²
Plastic section modulus ($W_{pl,y}$)	3676.0 cm ³



3.16.3 Analysis Model

Loading condition		
Beam Diagram	SF	
	BM	

3.16.4 Comparison of Design Results

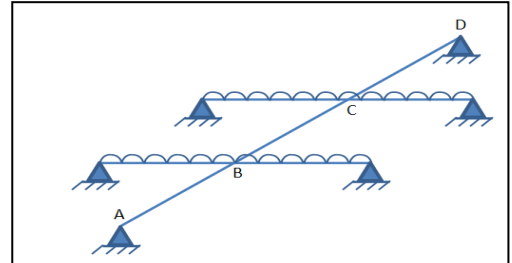
	midas Gen	Example book	Error (%)
Deflection (w_c)	5.705mm	5.700mm	0.09%

3.16.5 Detailed comparison

midas Gen	Example book
<p>1. Check Deflection.</p> <p>(). Compute Maximum Deflection.</p> <ul style="list-style-type: none"> - LCB = 1 - DAF = 1.000 (Deflection Amplification Factor). - Position = 3000.000mm From i-end(Node 1). - Def = -5.705 * DAF = -5.705mm (Global Z) - Def_Lim = 16.667mm <p>Def < Def_Lim ----> O.K !</p>	<p>The central deflection ω_c of a simply supported beam with uniformly distributed load q can be calculated using</p> $\omega_c = \frac{5qL^4}{384EI_y}$ $= \frac{5 \times 70 \times 6000^4}{384 \times 210000 \times 98610 \times 10^4}$ $= \mathbf{5.7 \text{ mm.}}$ <p>(The same result can be obtained using Figure 5.3.)</p> <p>$L/360 = 6000/360 = \mathbf{16.7 \text{ mm}} > 5.7 \text{ mm} = \omega_c$ and so the beam is satisfactory.</p> <p>[Reference] N.S. Trahair, M.A. Bradford, D.A.Nethercot, and L.Gardner, The behavior and Design of Steel Structures to EC3, Taylor & Francis, 223 (Example 5.12.18)</p>

3.17 Checking the major axis in-plane resistance

The 9 m long simply supported beam-column shown in Figure has a factored design axial compression force of 200 kN and a design concentrated load of 20 kN (which includes an allowance for self-weight) acting in the major principal plane at mid-span. The beam-column is the 254 X 146 UB 37 of S275 steel shown in Figure 7.19a. The beam-column is continuously braced against lateral deflections v and twist rotations ϕ . Check the adequacy of the beam-column.

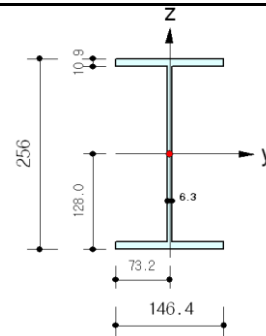


3.17.1 Material Properties

Material	S275	$f_y = 275 \text{ N/mm}^2$	$E_s = 210 \text{ GPa}$
----------	------	----------------------------	-------------------------

3.17.2 Section Properties

Section Name	254x146 UB 37
Depth (H)	256.0 mm
Width (B)	146.4 mm
Flange Thickness (T_f)	10.9 mm
Web Thickness (T_w)	6.3 mm
Gross sectional area (A)	22000.0 mm ²
Shear area (A_{sz})	11500.2 mm ²



3.17.3 Analysis Model

Loading condition		
Beam Diagram	SF	
	BM	

3.17.4 Comparison of Design Results

	midas Gen	Example book	Error (%)
Shear resistance	900.13kN	900.00kN	0.01%
Bending resistance	132.82kNm	132.80kNm	0.02%

3.17.5 Detailed comparison

midas Gen	Example book
<p>1. Cross-section classification</p> <p>(). Determine classification of compression outstand flanges.</p> <p>[Eurocode3:05 Table 5.2 (Sheet 2 of 3), EN 1993-1-5]</p> <ul style="list-style-type: none"> - $e = \text{SQRT}(235/f_y) = 0.92$ - $b/t = \text{BTR} = 5.73$ - $\sigma_1 = 146298.978 \text{ KPa}$. - $\sigma_2 = 146298.978 \text{ KPa}$. - $\text{BTR} < 9 \cdot e$ (Class 1 : Plastic). <p>(). Determine classification of bending and compression Internal Parts.</p> <p>[Eurocode3:05 Table 5.2 (Sheet 1 of 3), EN 1993-1-5]</p> <ul style="list-style-type: none"> - $e = \text{SQRT}(235/f_y) = 0.92$ - $d/t = \text{HTR} = 34.76$ - $\sigma_1 = 197836.100 \text{ KPa}$. - $\sigma_2 = -113090.338 \text{ KPa}$. - $\text{Psi} = [2 \cdot (\text{Nsd}/A) \cdot (1/f_y)] - 1 = -0.692$ - $\text{Alpha} = 0.746 > 0.5$ - $\text{HTR} < 396 \cdot e / (13 \cdot \text{Alpha} - 1)$ (Class 1 : Plastic). <p>2. CHECK AXIAL RESISTANCE</p> <p>(). Check slenderness ratio of axial compression member (Kl/i) [Eurocode3:05 6.3.1]</p> <ul style="list-style-type: none"> - $\text{Kl}/i = 83.3 < 200.0 \rightarrow \text{O.K.}$ <p>(). Calculate axial compressive resistance (Nc_Rd).</p> <p>[Eurocode3:05 6.1, 6.2.4]</p> <ul style="list-style-type: none"> - $\text{Nc_Rd} = f_y \cdot \text{Area} / \text{Gamma_M0} = 1298.00 \text{ kN}$. <p>(). Check ratio of axial resistance (N_Ed/Nc_Rd).</p> $\frac{\text{N_Ed}}{\text{Nc_Rd}} = \frac{200.00}{1298.00} = 0.154 < 1.000 \rightarrow \text{O.K.}$ <p>(). Calculate buckling resistance of compression member (Nb_Rdy, Nb_Rdz). [Eurocode3:05 6.3.1.1, 6.3.1.2]</p> <ul style="list-style-type: none"> - $\text{Beta_A} = A_{\text{eff}} / \text{Area} = 1.000$ - $\text{Lambda1} = \text{Pi} \cdot \text{SQRT}(E_s/f_y) = 86.815$ - $\text{Lambda_by} = \{(\text{KLy}/i_y)/\text{Lambda1}\} \cdot \text{SQRT}(\text{Beta_A}) = 0.960$ 	<p>Simplified approach for cross-section resistance.</p> <p>$t_f = 10.9 \text{ mm}$, $f_y = 275 \text{ N/mm}^2$ En 10025-2</p> <p>$\epsilon = \sqrt{235/275}^{0.5} = 0.924$</p> <p>$c_f/(t_f \epsilon) = ((146.4 - 6.3 - 2 \times 7.6) / 2) / (10.9 \times 0.924) = 6.20 < 9$</p> <p>and the flange is Class 1.</p> <p>$c_w = 256.0 - (2 \times 10.9) - (2 \times 7.6) = 219.0 \text{ mm}$</p> <p>The compression proportion of web is</p> $\alpha = \left(\frac{h}{2} - (t_f + r) + \frac{1}{2} \frac{\text{N}_{\text{Ed}}}{t_f f_y} \right) / c_w$ $= \left(\frac{256}{2} - (10.9 + 7.6) + \frac{1}{2} \frac{200 \times 10^3}{6.3 \times 275} \right) / 219.0$ $= 0.76 > 0.5$ <p>$c_w / t_w = 219.0 / 6.3 = 34.8 < 41.3 = \frac{396 \epsilon}{13 \alpha - 1}$</p> <p>and the web is Class 1.</p> <p>$M_{c,y,Rd} = 275 \times 483 \times 10^3 / 1.0 \text{ Nmm} = 132.8 \text{ KNm}$</p> <p>$M_{y,Ed} = 20 \times 9/4 = 45.0 \text{ KNm}$</p> $\frac{200 \times 10^3}{47.2 \times 10^2 \times 275 / 1.0} + \frac{45.0}{132.8} = 0.493 \leq 1$ <p>And the cross-section resistance is adequate.</p> <p>Alternative approach for cross-section resistance.</p> <p>Because the section is Class 1, Clause 6.2.9.1 can be used.</p> <p>No reduction in plastic moment resistance is required provided both</p> <p>$\text{N}_{\text{Ed}} = 200 \text{ KN} < 324.5 \text{ KN}$</p> $= (0.25 \times 47.2 \times 10^2 \times 275 / 1.0) / 10^3$ <p>$= 0.25 \text{N}_{\text{pl,Rd}}$ and</p> <p>$\text{N}_{\text{Ed}} = 200 \text{ KN} < 202.9 \text{ KN}$</p> $= \frac{0.5 \times (256.0 - 2 \times 10.9) \times 6.3 \times 275}{1.0 \times 10^3}$ $= \frac{0.5 h_w t_w f_y}{\gamma_{M0}}$ <p>And so no reduction in the plastic moment resistance is required.</p>

- $N_{cry} = \pi^2 E_s R_{yy} / K L_y^2 = 1417.57 \text{ kN}$.
- $\lambda_{b,y} > 0.2$ and $N_{Ed}/N_{cry} > 0.04 \rightarrow$ Need to check.
- $\alpha_{ph,y} = 0.210$
- $\phi_{iy} = 0.5 \cdot [1 + \alpha_{ph,y}(\lambda_{b,y} - 0.2) + \lambda_{b,y}^2] = 1.040$
- $\chi_{iy} = \min [1 / [\phi_{iy} + \sqrt{\phi_{iy}^2 - \lambda_{b,y}^2}], 1.0] = 0.693$
- $N_{b,Rdy} = \chi_{iy} \beta_A A_s f_y / \gamma_{M1} = 900.13 \text{ kN}$.
- $\lambda_{b,z} = \{(K L_z / i_z) / \lambda_{b,y}\} \cdot \sqrt{\beta_A} = 3.310e-004$
- $N_{crz} = \pi^2 E_s R_{zz} / K L_z^2 = 11834642637.35 \text{ kN}$.
- $\lambda_{b,z} < 0.2$ or $N_{Ed}/N_{crz} < 0.04$
 \rightarrow No need to check.

(). Check ratio of buckling resistance ($N_{Ed}/N_{b,Rd}$).

$$N_{b,Rd} = \min [N_{b,Rdy}, N_{b,Rdz}] = 900.13 \text{ kN}$$

$$\frac{N_{Ed}}{N_{b,Rd}} = \frac{200.00}{900.13} = 0.222 < 1.000 \rightarrow \text{O.K.}$$

3. CHECK SHEAR RESISTANCE.

(). Calculate shear area.

[Eurocode3:05 6.2.6, EN1993-1-5:04 5.1 NOTE 2]

- $\eta = 1.2$ ($F_y < 460 \text{ MPa}$.)
- $r = 0.0076 \text{ m}$.
- $A_{vy} = A_s - h w \cdot t_w = 0.0032 \text{ m}^2$.
- $A_{vz1} = \eta \cdot h w \cdot t_w = 0.0018 \text{ m}^2$.
- $A_{vz2} = A_s - 2 \cdot B \cdot t_f + (t_w + 2 \cdot r) \cdot t_f = 0.0018 \text{ m}^2$.
- $A_{vz} = \max [A_{vz1}, A_{vz2}] = 0.0018 \text{ m}^2$.

(). Calculate plastic shear resistance in local-z direction ($V_{pl,Rdz}$). [Eurocode3:05 6.1, 6.2.6]

$$V_{pl,Rdz} = [A_{vz} \cdot f_y / \sqrt{3}] / \gamma_{M0} = 281.11 \text{ kN}$$

(). Shear Buckling Check. [Eurocode3:05 6.2.6]

- $HTR < 72 \cdot \eta / \lambda_{b,y} \rightarrow$ No need to check!

(). Check ratio of shear resistance ($V_{Edz}/V_{pl,Rdz}$). (LCB = 1, POS = J)

$$V_{Edz} = 10.00 \text{ kN}$$

$$\frac{V_{Edz}}{V_{pl,Rdz}} = \frac{10.00}{281.11} = 0.036 < 1.000 \rightarrow \text{O.K.}$$

4. CHECK BENDING MOMENT RESISTANCE ABOUT MAJOR AXIS

(). Calculate plastic resistance moment about major axis.

[Eurocode3:05 6.1, 6.2.5]

- $W_{ply} = 0.0005 \text{ m}^3$.
- $M_{c,Rdy} = W_{ply} \cdot f_y / \gamma_{M0} = 132.82 \text{ kN-m}$.

$$M_{N,y,Rd} = M_{pl,y,Rd} = 132.9 \text{ kNm} > 45.0 \text{ kNm}$$

$$= M_{y,Ed}$$

And the cross-section resistance is adequate.
 Compression member buckling resistance.

Because the member is continuously braced, beam lateral buckling and column minor axis buckling need not be considered.

$$\lambda_y = \sqrt{\frac{A f_y}{N_{cr,y}}} = \frac{L_{cr,y}}{i_y} \cdot \frac{1}{\lambda_1} = \frac{9000}{(10.8 \times 10)} \cdot \frac{1}{93.9 \times 0.924} = 0.960$$

For a rolled UB section (with $h/b > 1.2$ and $t_f \leq 40 \text{ mm}$), buckling about the y-axis, use buckling curve (a) with $\alpha = 0.21$

$$\Phi_y = 0.5 [1 + 0.21 (0.960 - 0.2) + 0.960^2] = 1.041$$

$$\chi_y = \frac{1}{1.041 + \sqrt{1.041^2 - 0.960^2}} = 0.693$$

$$N_{b,y,Rd} = \frac{\chi_y A f_y}{\gamma_{M1}} = \frac{0.693 \times 47.2 \times 10^2 \times 275}{1.0} = 900 \text{ kN} > 200 \text{ kN} = N_{Ed}$$

Beam-column member resistance – more exact approach (Annex A)

$$\lambda_{max} = \lambda_y = 0.960$$

$$N_{cr,y} = \frac{\pi^2 EI}{L_{cr}^2} = \frac{\pi^2 \times 210000 \times 55370000}{9000^2} = 1470 \times 10^3$$

$$= 1470 \text{ kN}$$

Since there is no lateral buckling, $\lambda_0 = 0$, $b_{LT} = 0$,

$$C_{mLT} = 1.0$$

$$C_{my} = C_{my,0} = 1 - 0.18 N_{Ed} / N_{cr,y} = 1 - 0.18 \times 200 / 1417$$

$$= 0.975$$

$$W_y = \frac{W_{pl,y}}{W_{el,y}} = \frac{483}{433} = 1.115,$$

$$\eta_{pl} = \frac{N_{Ed}}{N_{RK} / \gamma_{M1}} = \frac{200 \times 10^3}{47.2 \times 10^2 \times 275 / 1.0} = 0.154$$

$$C_{yy} = 1 + (W_y - 1)$$

(). Check ratio of moment resistance (M_Edy/Mc_Rdy).

$$\frac{M_{Edy}}{Mc_{Rdy}} = \frac{45.00}{132.82} = 0.339 < 1.000 \rightarrow \text{O.K.}$$

(). Calculate plastic resistance moment about minor axis.

[Eurocode3:05 6.1, 6.2.5]

$$\begin{aligned} \therefore W_{plz} &= 0.0001 \text{ m}^3. \\ \therefore Mc_{Rdz} &= W_{plz} \cdot f_y / \gamma_{M0} = 32.73 \text{ kN-m.} \end{aligned}$$

(). Check ratio of moment resistance (M_Edz/Mc_Rdz).

$$\frac{M_{Edz}}{Mc_{Rdz}} = \frac{0.00}{32.73} = 0.000 < 1.000 \rightarrow \text{O.K.}$$

5. CHECK INTERACTION OF COMBINED RESISTANCE**(). Calculate Major reduced design resistance of bending and shear.** [Eurocode3:05 6.2.8 (6.30)]

$$\begin{aligned} \therefore \text{In case of } V_{Edy} / V_{pl,Rdy} &< 0.5 \\ \therefore M_{y,Rd} &= Mc_{Rdy} = 132.82 \text{ kN-m.} \end{aligned}$$

(). Calculate Minor reduced design resistance of bending and shear. [Eurocode3:05 6.2.8 (6.30)]

$$\begin{aligned} \therefore \text{In case of } V_{Edy} / V_{pl,Rdy} &< 0.5 \\ \therefore M_{z,Rd} &= Mc_{Rdz} = 32.73 \text{ kN-m.} \end{aligned}$$

(). Check general interaction ratio.

[Eurocode3:05 6.2.1 (6.2)] - Class1 or Class2

$$\begin{aligned} \frac{N_{Ed}}{N_{Rd}} + \frac{M_{Edy}}{M_{y,Rd}} + \frac{M_{Edz}}{M_{z,Rd}} &= 0.493 < 1.000 \rightarrow \text{O.K.} \end{aligned}$$

(). Check interaction ratio of bending and axial force member.

[Eurocode3:05 6.2.9 (6.31 ~ 6.41)] - Class1 or Class2

$$\begin{aligned} \therefore n &= N_{Ed} / N_{pl,Rd} = 0.154 \\ \therefore a &= \min[(Area - 2b \cdot t_f) / Area, 0.5] = 0.324 \\ \therefore \alpha &= 2.000 \\ \therefore \beta &= \max[5 \cdot n, 1.0] = 1.000 \\ \therefore N_{Ed} &< 0.25 \cdot N_{pl,Rd} = 225.03 \text{ kN.} \\ \therefore N_{Ed} &< 0.5 \cdot h_w \cdot t_w \cdot f_y / \gamma_{M0} = 202.88 \text{ kN.} \\ \text{Therefore, No allowance for the effect of axial force.} \\ \therefore M_{ny,Rd} &= M_{py,Rd} = 132.82 \text{ kN-m.} \\ \therefore R_{maxy} &= M_{Edy} / M_{ny,Rd} = 0.339 < 1.000 \rightarrow \text{O.K.} \\ \therefore N_{Ed} &< h_w \cdot t_w \cdot f_y / \gamma_{M0} = 702.01 \text{ kN.} \\ \text{Therefore, No allowance for the effect of axial force.} \\ \therefore M_{nz,Rd} &= M_{plz,Rd} = 32.73 \text{ kN-m.} \\ \therefore R_{maxz} &= M_{Edz} / M_{nz,Rd} = 0.000 < 1.000 \rightarrow \text{O.K.} \\ \therefore R_{max2} &= \max[R_{maxy}, R_{maxz}] = 0.339 < 1.000 \rightarrow \text{O.K.} \end{aligned}$$

$$\left[\left(2 - \frac{1.6}{W_y} C_{my}^2 \lambda_{\max}^2 - \frac{1.6}{W_y} C_{my}^2 \lambda_{\max}^2 \right) n_{pl} - b_{LT} \geq W_{pl,y} W_{el,y} \right]$$

$$= 1 + (1.115 - 1) \times$$

$$\begin{aligned} &\left(2 - \frac{1.6}{1.115} \times 0.975^2 \times 0.960 \right. \\ &\quad \left. - \frac{1.6}{1.115} \times 0.975^2 \times 0.960^2 \right) \\ &\times 0.154 - 0 = 0.990 > 0.896 = 1 / 1.115 \end{aligned}$$

$$\mu_y = \frac{1 - N_{ED} / N_{cr,y}}{1 - \chi_y N_{ED} / N_{cr,y}} = \frac{1 - 200 / 1417}{1 - 0.693 \times 200 / 1417} = 0.952$$

$$\begin{aligned} k_{yy} &= C_{my} C_{mLT} \frac{\mu_y}{1 - N_{ED} / N_{cr,y}} \frac{1}{C_{yy}} \\ &= 0.975 \times 1.0 \times \frac{0.952}{1 - 200 / 1417} \times \frac{1}{0.990} = 1.091 \end{aligned}$$

$$\begin{aligned} \frac{N_{Ed}}{N_{b,y,Rd}} + k_{yy} \frac{M_{y,Ed}}{M_{c,y,Rd}} &= \frac{200}{900} + 1.091 \times \frac{45.0}{132.8} \\ &= 0.222 + 0.370 = 0.592 < 1 \end{aligned}$$

And the member resistance is adequate.

(). Check interaction ratio of bending and axial compression member.

[Eurocode3:05 6.3.1, 6.2.9.3 (6.61, 6.62), Annex A]

- . $k_{yy} = 1.091$
- . $k_{yz} = 0.647$
- . $k_{zy} = 0.645$
- . $k_{zz} = 1.001$
- . $X_{iy} = 0.696$
- . $X_{iz} = 1.000$
- . $X_{iLT} = 1.000$
- . $N_{Rk} = A \cdot f_y = 1298.00 \text{ kN}$.
- . $M_{yRk} = W_{ply} \cdot f_y = 132.82 \text{ kN-m}$.
- . $M_{zRk} = W_{plz} \cdot f_y = 32.73 \text{ kN-m}$.
- . $N_{Ed} \cdot e_{Ny} = 0.0$ (Not Slender)
- . $N_{Ed} \cdot e_{Nz} = 0.0$ (Not Slender)

$$\begin{aligned}
 -. R_{max_LT1} &= \frac{N_{Ed}}{X_{iy} \cdot N_{Rk} / \Gamma_{M1}} \\
 &+ k_{yy} \cdot \frac{M_{Edy} + N_{Ed} \cdot e_{Ny}}{X_{iLT} \cdot M_{yRk} / \Gamma_{M1}} \\
 &+ k_{yz} \cdot \frac{M_{Edz} + N_{Ed} \cdot e_{Nz}}{M_{zRk} / \Gamma_{M1}} \\
 &= 0.591 < 1.000 \text{ ---> O.K.}
 \end{aligned}$$

$$\begin{aligned}
 -. R_{max_LT2} &= \frac{N_{Ed}}{X_{iz} \cdot N_{Rk} / \Gamma_{M1}} \\
 &+ k_{zy} \cdot \frac{M_{Edy} + N_{Ed} \cdot e_{Ny}}{X_{iLT} \cdot M_{yRk} / \Gamma_{M1}} \\
 &+ k_{zz} \cdot \frac{M_{Edz} + N_{Ed} \cdot e_{Nz}}{M_{zRk} / \Gamma_{M1}} \\
 &= 0.373 < 1.000 \text{ ---> O.K.}
 \end{aligned}$$

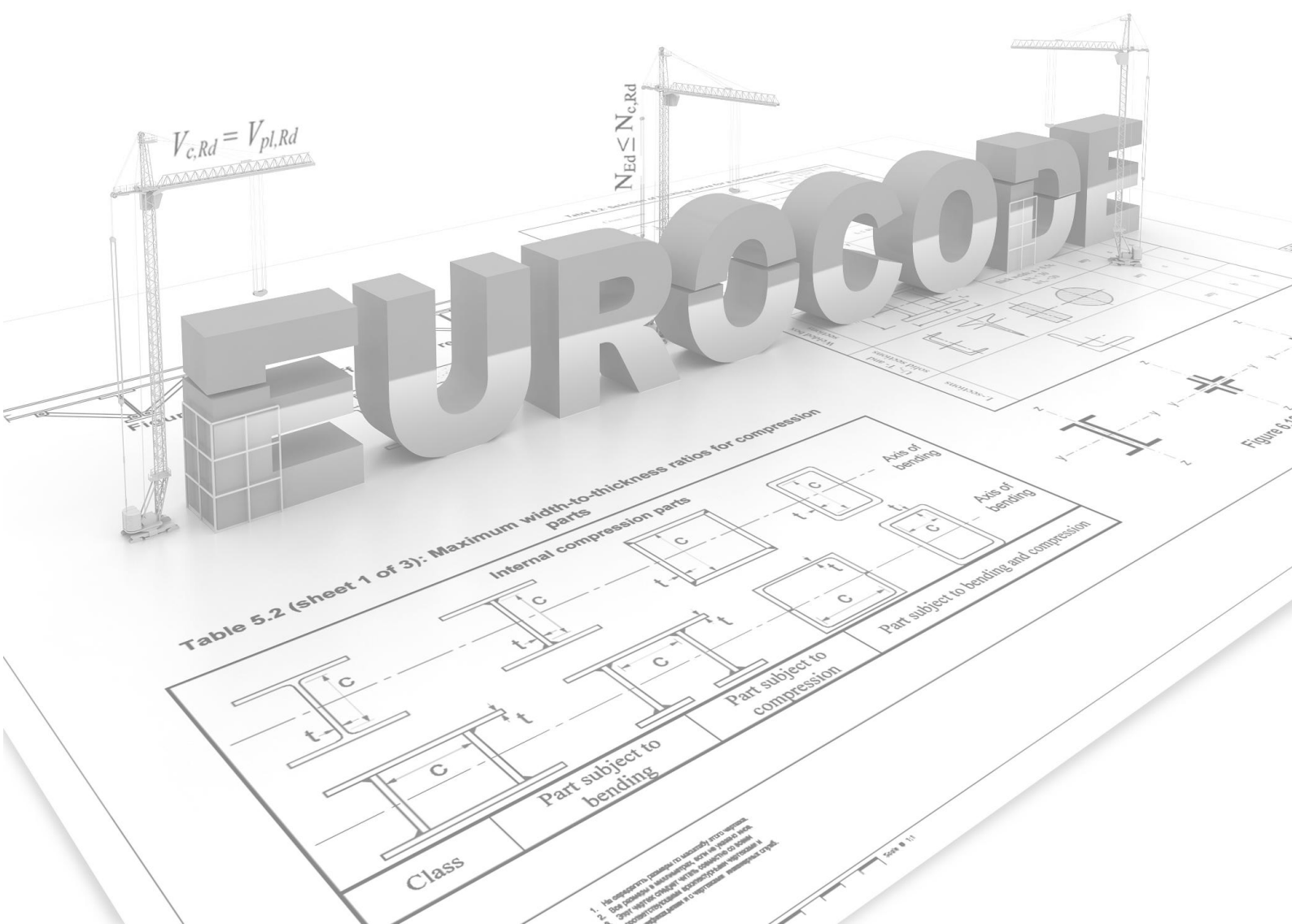
$$-. R_{max} = \text{MAX}[\text{MAX}(R_{max1}, R_{max2}), \text{MAX}(R_{max_LT1}, R_{max_LT2})] = 0.591 < 1.000 \text{ ---> O.K.}$$

[Reference]

N.S. Trahair, M.A. Bradford, D.A.Nethercot, and L.Gardner, The behavior and Design of Steel Structures to EC3, Taylor & Francis, 330-333 (Example 7.7.2)

Steel Design Tutorial

Design Examples using midas Gen to Eurocode3

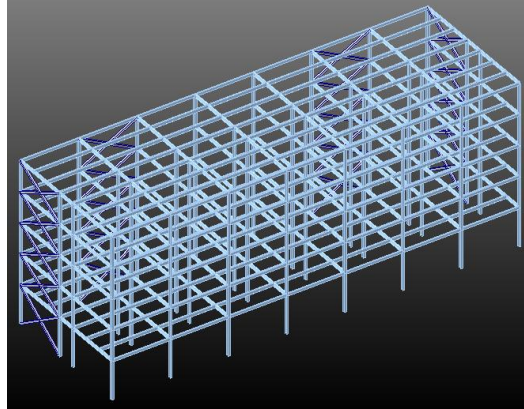


Step
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Contents

- **Step 1:** Analyze the model.
- **Step 2:** Select the design code.
- **Step 3:** Generate load combinations.
- **Step 4:** Enter design parameters (Unbraced Length, Moment Factor, etc).
- **Step 5:** Enter deflection limits.
- **Step 6:** Check design results.
- **Step 7:** Change and update the designed sections.

Eurocode 3 - Design of Multi-Story Steel Building



Step
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Overview

Eurocode 3 Steel Design Methods

midas Gen provides the following two methods:

1. The program finds optimal sections for gravity loads (Design > Steel Optimal Design) and also finds optimal sections for lateral loads (Design> Displacement Optimal Design). With the combined use of the two, the user should find optimal sections.
2. The program checks strength and serviceability based on the sections defined by the user and the design code selected by the user (Design > Steel Code Check). Also, the program searches and proposes sections which satisfy the design conditions entered by the user. Then the user can update the sections referring to the sections proposed by the program.

In this tutorial, method 2 is presented.

Step

00

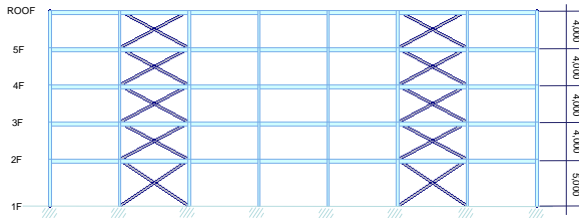
Overview - Details of the example building

Figure 1. Elevation (unit: mm)

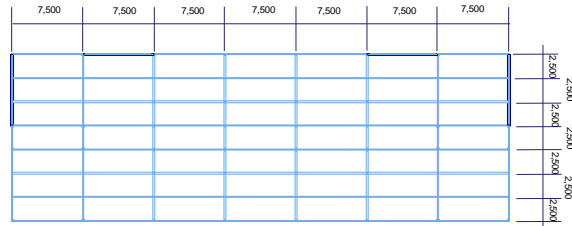


Figure 2. Structural Plan (2~Roof) (unit: mm)

Step

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Overview● **Applied Codes**

- Applied Wind Load: Eurocode 1 (2005)
- Applied Seismic Load: Eurocode 8 (2004)
- Steel Design Code: Eurocode 3 (2005)

● **Applied Loads****Self Weight****Floor loads**

- For floor 2~5
 - Superimposed Dead Load: 3.7 kN/m²
 - Live Load: 4 kN/m²
- For roof
 - Superimposed Dead Load: 5 kN/m²
 - Live Load: 1.5 kN/m²

Wind loads

- Basic Wind Velocity: 26 m/s
- Terrain Category: II

Seismic loads

- Ground Type: B

● **Structural System**

- Bracing system

● **Materials**

- Beam, Column and Brace: S275

Unit Load Cases

Load	Name	Details
Static Load Cases	1	Self Weight Self Weight
	2	SID Superimposed Dead Load
	3	Live Load Live Load
	4	Wind X-dir Wind Load (in the global X-direction)
	5	Wind Y-dir Wind Load (in the global Y-direction)
Response Spectrum Load Cases	6	RX Seismic Load (in the global X-direction)
	7	RY Seismic Load (in the global Y-direction)

Step

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Overview

- **Applied Sections**

These are the sections assumed before design updates.

- **Beam**

Section ID	DB	Section Size
1	UNI	IPE 500
2	UNI	IPE 600
3	UNI	IPE 450

- **Column**

Section ID	DB	Section Size
4	UNI	HEB 240
5	UNI	HEB 300

- **Brace**

Section ID	DB	Section Size
6	UNI	HEA 260

Step

01

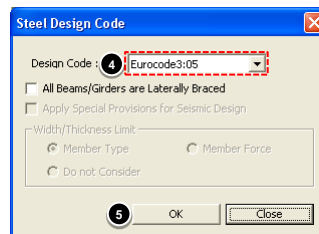
Step . 1 Open the model file and perform analysis & Steel Design Code

Procedure**Step1. Open the model file and perform analysis**

- 1 Open "EC3 design_start model.mgb"
- 2 Analysis > Perform Analysis

Step2. Steel Design Code

- 3 Design > Steel Design
Parameter > Design Code
- 4 Design Code: "Eurocode3:05"
- 5 Click on "OK" button.



Step

02

Step . 2 Generate Load Combinations

Procedure

Generate Load Combinations

The program automatically creates design load combinations which can be also modified or deleted by the user.

- 1 Result > Combinations
- 2 Click on "Steel Design" Tab.
- 3 Click "Auto Generation" button.
- 4 Option: "Add"
- 5 Code Selection: "Steel"
- 6 Design Code: "Eurocode3:05"
- 7 Gamma G: 1.35, Gamma Q: 1.5
- 8 Click on "OK" button.
- 9 Click on "Close" button.

Automatic Generation of Load Combinations

Option: ☒ Add ☐ Replace

Code Selection: ☒ Steel ☐ Concrete ☐ SRC ☐ Floating

Design Code: Eurocode3:05

Scale Up of Response Spectrum Load Cases: Scale Up Factor: 1 RX

Manipulation of Construction Stage Load Case: ST Only ☒ CS Only ☐ ST+CS ☐

Consider Orthogonal Effect: ☐ Set Load Cases for Orthogonal Effect...

Factors for variable actions: Psi0: 0.7 Psi1: 0.5 Psi2: 0.3

Partial factors for actions: Gamma G: 1.35 Gamma Q: 1.5

OK Cancel

Load Combinations

No	Name	Active	Type	Description
1	ALCB1	Stren	Add	1.350 + 1.5(1.0Live Load)
2	ALCB2	Stren	Add	1.350 + 1.5(1.0Live Load) + 1.5
3	ALCB3	Stren	Add	1.350 + 1.5(1.0Live Load) + 1.5
4	ALCB4	Stren	Add	1.350 + 1.5(0.7Live Load) + 1.5
5	ALCB5	Stren	Add	1.350 + 1.5(0.7Live Load) + 1.5
6	ALCB6	Stren	Add	1.350 + 1.5(1.0Live Load) + 1.5
7	ALCB7	Stren	Add	1.350 + 1.5(1.0Live Load) + 1.5
8	ALCB8	Stren	Add	1.350 + 1.5(0.7Live Load) + 1.5
9	ALCB9	Stren	Add	1.350 + 1.5(0.7Live Load) + 1.5
10	ALCB10	Stren	Add	1.00 + 1.0(0.3L + 1.0(1.0RX)
11	ALCB11	Stren	Add	1.00 + 1.0(0.3L + 1.0(1.0RY)
12	ALCB12	Stren	Add	1.00 + 1.0(0.3L + 1.0(1.0RY)
13	ALCB13	Stren	Add	1.00 + 1.0(0.3L + 1.0(1.0RY)
14	ALCB14	Semic	Add	SERV 1.00 + 1.0Live Load + 0
15	ALCB15	Semic	Add	SERV 1.00 + 1.0Live Load + 0
16	ALCB16	Semic	Add	SERV 1.00 + 1.0Live Load + 0
17	ALCB17	Semic	Add	SERV 1.00 + 1.0Live Load + 0
18	ALCB18	Semic	Add	SERV 1.00 + 1.0Live Load + 0
19	ALCB19	Semic	Add	SERV 1.00 + 0.7Live Load + 1
20	ALCB20	Semic	Add	SERV 1.00 + 0.7Live Load + 1
21	ALCB21	Semic	Add	SERV 1.00 + 0.7Live Load + 1

Load Case	Factor
Self Weight	1.3500
Dead Load	1.3500
Live Load	1.5000

File Name: \\W:\Documents\WEC3 Tutorial\WEC3 design_Short.mw Browse File Load Combination Sheet Close

Step

03

Step . 3 Enter Unbraced Length

Procedure

Enter Unbraced Length

- 1 View > Select > Identity
- 2 Select Type: "Section"
- 3 Select "1: IPE 500" & "IPE 600."
- 4 Click on "Add" button and "Close" button.
- 5 Design > General Design Parameter > Unbraced Length
- 6 Option: "Add/Replace"
- 7 Laterally Unbraced Length, Lb = 2.5
- 8 Click on "Apply" button and "Close" button.

Select Identity

All None Inverse Prev

☐ Nodes

☒ Elements: 29to52 181to204 333to356 485to500

Select Type: Section

1: IPE500 2: IPE600 3: IPE450 4: HEB340 5: HEB300 6: HEA260

Add Delete Replace Intersect

Multiple Close

General Steel Concrete SRC

Unbraced Length(Ly, Lz)

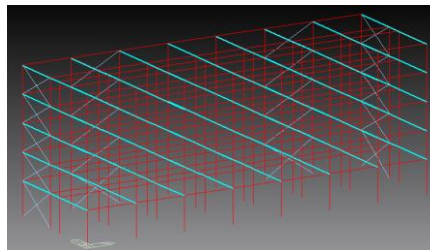
Option: ☒ Add/Replace ☐ Delete

Unbraced Length: Ly: 0 m Lz: 0 m

Laterally Unbraced Length: Lb: 2.5 m

☐ Do not consider

Apply Close



Step

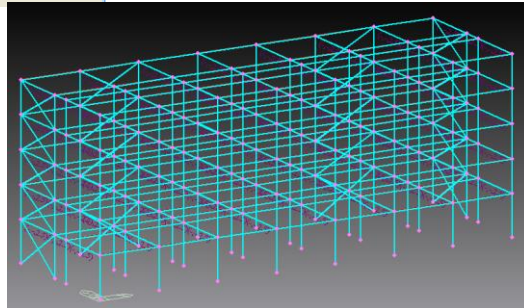
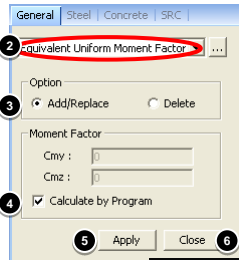
04

Step . 4 Enter Equivalent Uniform Moment Factor (Cmy, Cmz)

Procedure

Enter Equivalent Uniform Moment Factor (Cmy, Cmz)

- 1 View > Select > Select All
- 2 Design > General Design Parameter > Equivalent Uniform Moment Factor
- 3 Option: "Add/Replace"
- 4 Check on "Calculate by Program"
- 5 Click on "Apply" button
- 6 Click on "Close" button.



Step

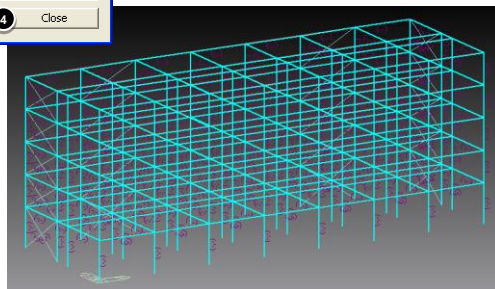
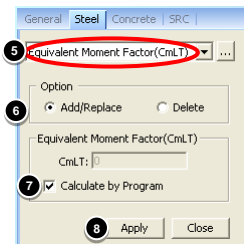
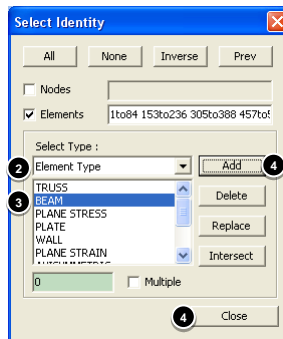
05

Step . 5 Enter Equivalent Moment Factor (CmLT)

Procedure

Enter Equivalent Moment Factor (CmLT)

- 1 View > Select > Identity
- 2 Select Type: "Element Type"
- 3 Select "BEAM".
- 4 Click on "Add" button and "Close" button.
- 5 Design > Steel Design Parameter > Equivalent Moment Factor
- 6 Option: "Add/Replace"
- 7 Check on "Calculate by Program."
- 8 Click on "Apply" button and "Close" button.

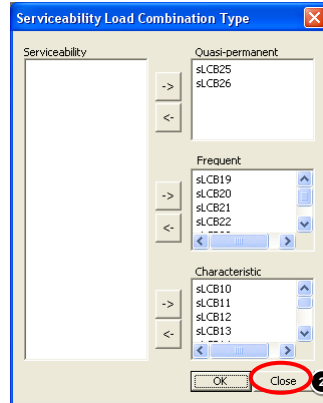


Step

06

Step . 6 Assign/Confirm Serviceability Load Combination Type**Procedure****Assign/Confirm Serviceability Load Combination Type**

- ① Design > General Design
Parameter > Serviceability
Load Combination Type
- ② Click on "Close" button.

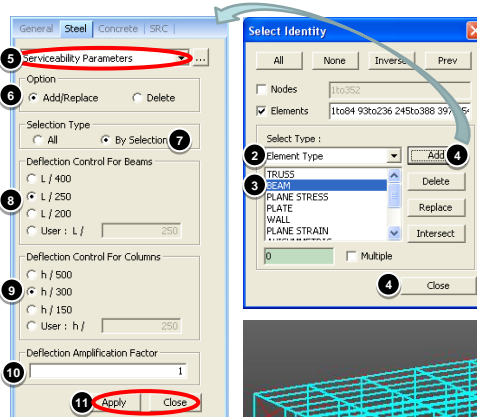


Step

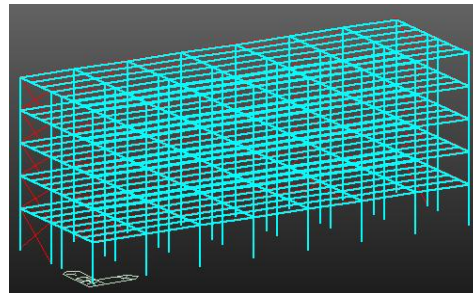
07

Step . 7 Enter Serviceability Parameters**Procedure****Enter Serviceability Parameters**

- ① View > Select > Identity
- ② Select Type: "Element Type"
- ③ Select "BEAM."
- ④ Click on "Add" button and "Close" button.
- ⑤ Design > Steel Design
Parameter > Serviceability
Parameters
- ⑥ Option: "Add/Replace"
- ⑦ Selection Type: "By Selection"
- ⑧ Deflection Control For Beams: "L / 250"
- ⑨ Deflection Control For Columns: "h / 300"
- ⑩ Deflection Amplification Factor: "1"
- ⑪ Click on "Apply" button and "Close" button.



If the element's local x-axis is parallel to the global Z-axis, the element is considered as a column. If the element's local x-axis is parallel to global X-Y plane, the element is considered as beam. All other elements except for columns and beams are considered to be braces.




Step

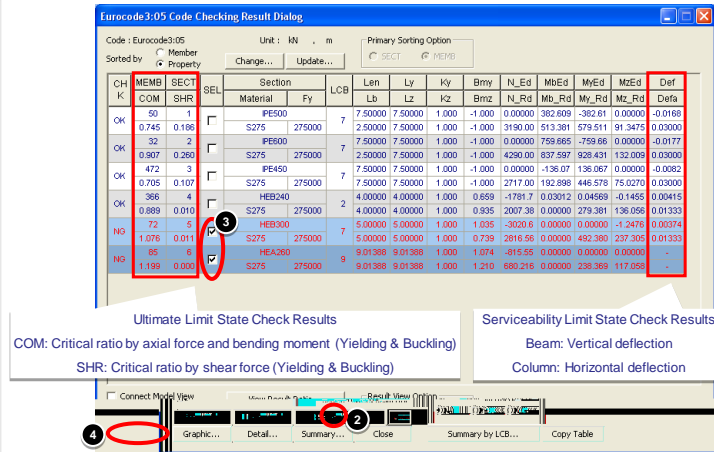
08

Step . 8-1 Steel Code Checking

Procedure

Steel Code Checking (1)

- 1 Design > Steel Code Check
- 2 Click on  button.
- 3 Select "SECT 5" & "SECT 6."
- 4 Click on "Graphic" button.



Step

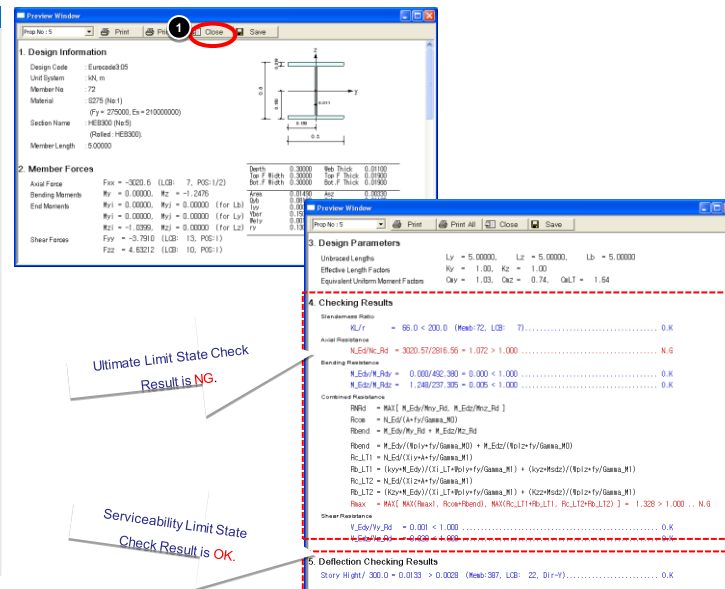
08

Step . 8-2 Steel Code Checking

Procedure

Steel Code Checking (2)

- 1 Click on "Close" button.



Step

9

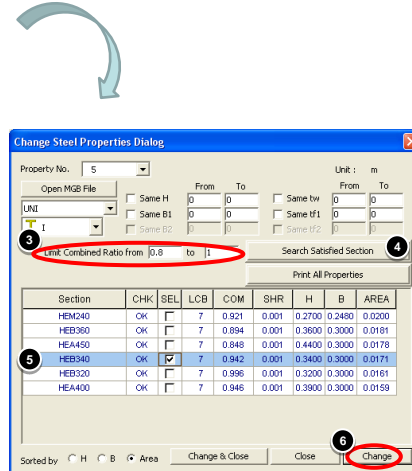
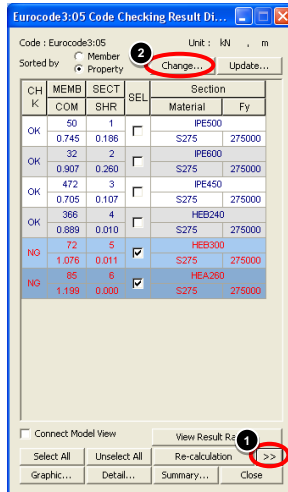
Step . 9-1 Change the NG sections

Procedure

Change the NG sections (1)

"Change" command will verify the strength for the user-selected section and save the design results until re-analysis is performed.

- 1 Click on - 2 Click on "Change" button.
- 3 Limit Combined Ratio from "0.8" to "1."
- 4 Click on "Search Satisfied Section."
- 5 Select "HEB340."
- 6 Click on "Change" button.



Step

9

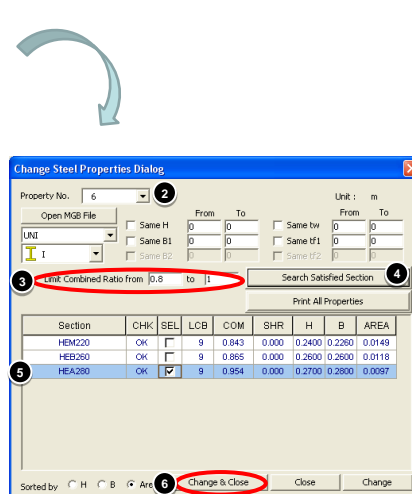
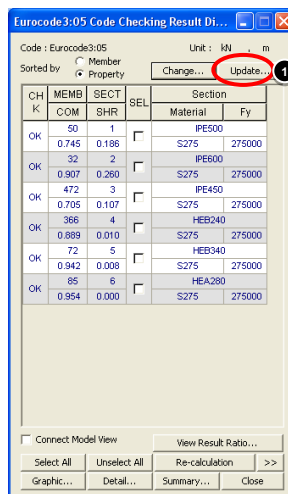
Step . 9-2 Change the NG sections

Procedure

Change the NG sections (2)

"Update" command will allow the user to update the section and re-analyze.

- 1 Click on update button.
- 2 Select Property No. 6.
- 3 Limit Combined Ratio from "0.8" to "1."
- 4 Click on "Search Satisfied Section."
- 5 Select "HEA280."
- 6 Click on "Change & Close" button.



Step
9

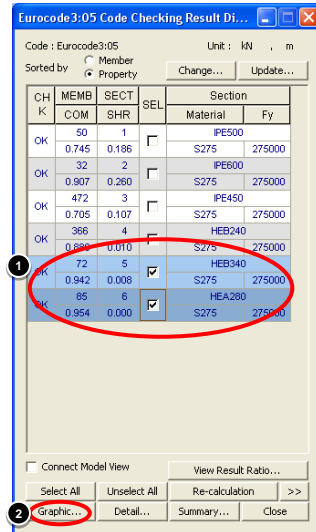
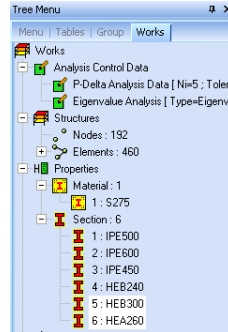
Step . 9-3 Change the NG sections

Procedure

Change the NG sections (3)

Only the section for design review has been changed. The section in the model has not been changed as seen in the Works Tree.

- 1 Select "SECT 6."
- 2 Click on "Graphic" button.



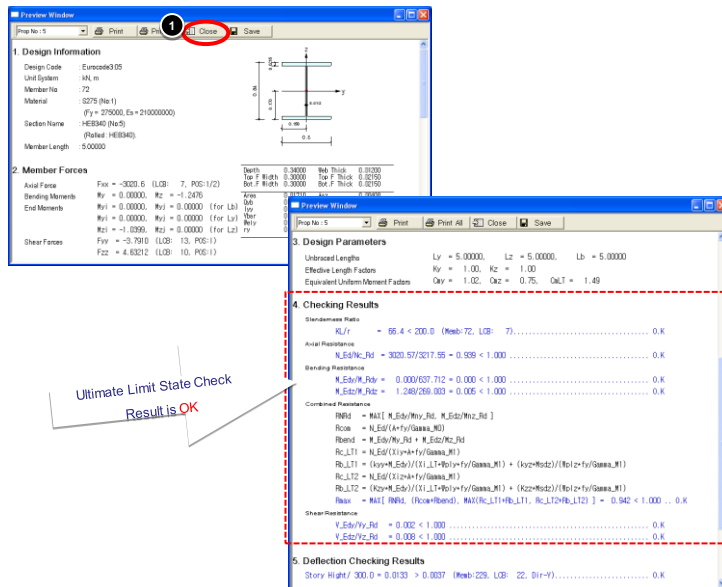
Step
9

Step . 9-4 Change the NG sections

Procedure

Change the NG sections (4)

- 1 Click on "Close" button.

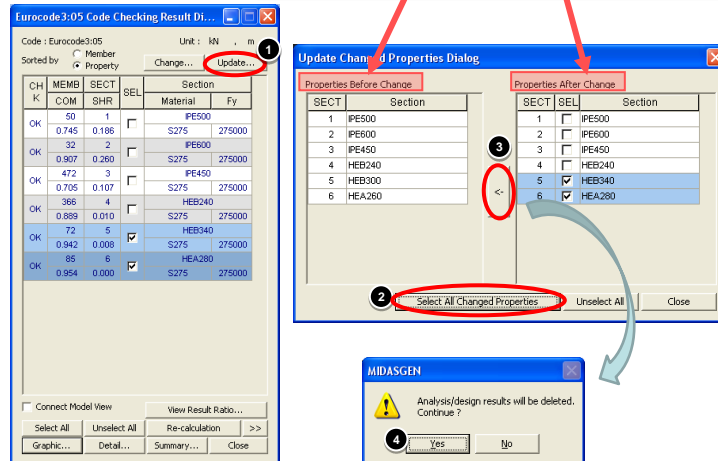


Step 10 Step . 10-1 Updated the Design Sections

Procedure

Updated the Design Sections(1)

- 1 Click on "Update" button.
- 2 Click on "Select All Changed Properties" button.
- 3 Click on "<" button.
- 4 Click on "Yes" button.

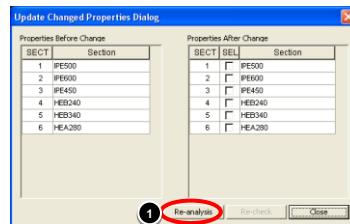


Step 10 Step . 10-2 Updated the Design Sections

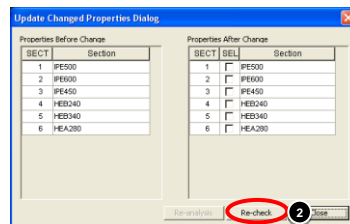
Procedure

Updated the Design Sections(2)

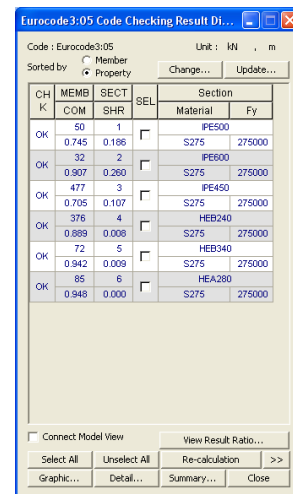
- 1 Click on "Re-analysis" button.
- 2 Click on "Re-check" button.



Re-analyze the model.



Re-do the steel code check.

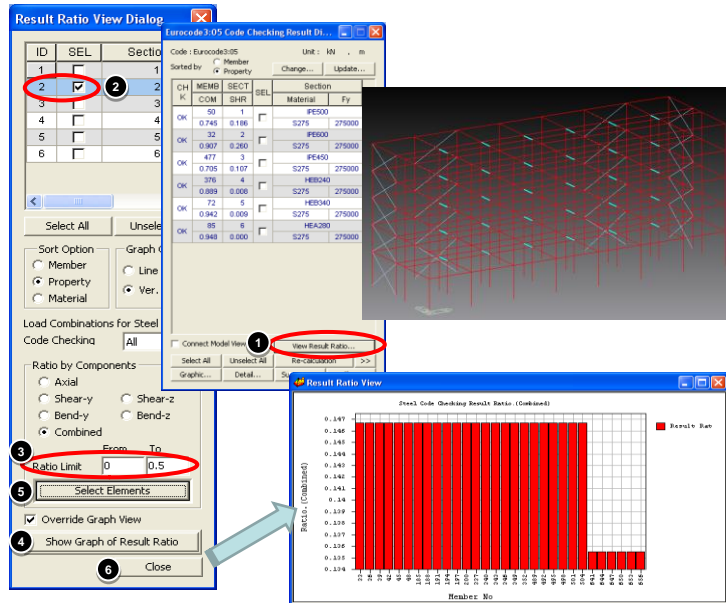


Final design results

Step

11**Step . 11-1 Change the Section with Low Ratio****Procedure****Change the Section with Low Ratio (1)**

- ① Click on "View Result Ratio" button.
- ② Select "ID: 2."
- ③ Ratio Limit: From "0", To "0.5"
- ④ Click on "Show Graph of Result Ratio" button.
- ⑤ Click on "Select Elements" button.
- ⑥ Click on "Close" button.

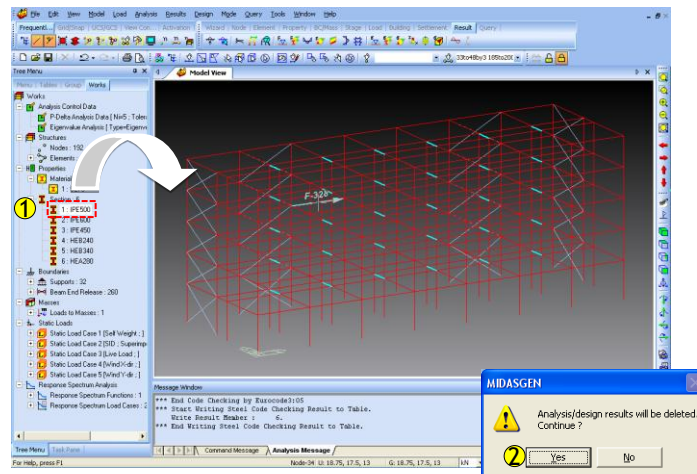


Step

12**Step . 12-2 Change the Section with Low Ratio****Procedure****Change the Section with Low Ratio (2)**

Among the elements assigned with IPE600, the elements whose combined resistance ratio is less than 0.5 are changed into a smaller section IPE500.

- ① Drag & Drop "1: IPE500" into the Model View.
- ② Click on "Yes" button.



Step

12**Step . 12-3 Change the Section with Low Ratio****Procedure****Change the Section with Low Ratio (3)**

- ❶ Analysis > Perform Analysis
- ❷ Design > Steel Code Check
- ❸ Click on "View Result Ratio" button.
- ❹ Select "ID: 2."
- ❺ Ratio Limit: From "0", To "1"
- ❻ Click on "Show Graph of Result Ratio" button.
- ❼ Click on "Close" button.

Result Ratio View Dialog

ID	SEL	Section No
1	<input type="checkbox"/>	1
2	<input checked="" type="checkbox"/>	2
3	<input type="checkbox"/>	3
4	<input type="checkbox"/>	4
5	<input type="checkbox"/>	5
6	<input type="checkbox"/>	6

Sort Option: ☐ Member ☒ Property ☐ Material
 Graph Option: ☐ Line ☒ Ver. Bar

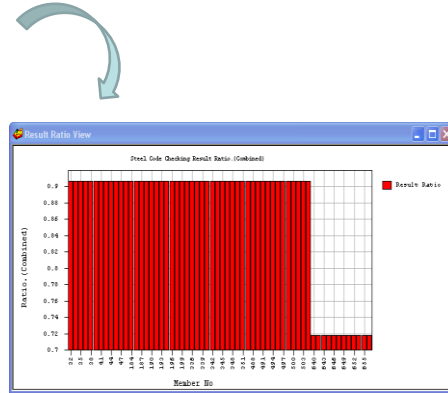
Load Combinations for Steel:

Code Checking:

Ratio by Components: ☐ Axial ☐ Shear-y ☐ Bend-y ☐ Shear-z ☐ Bend-z ☒ Combined

Ratio Limit: From To

☒ Override Graph View



Combined resistance ratios of
Section ID. 2 are all above 0.5.